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EXACT RELAXATION TIMES AND DYNAMIC FUNCTIONS FOR DILUTE POLYMER SOLUTIONS FROM THE BEAD/SPRING MODEL OF ROUSE AND ZIMM

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Wisconsin University

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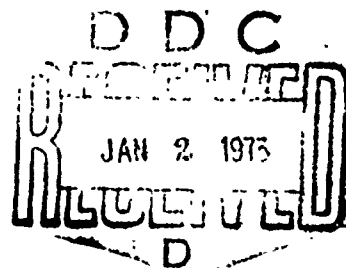
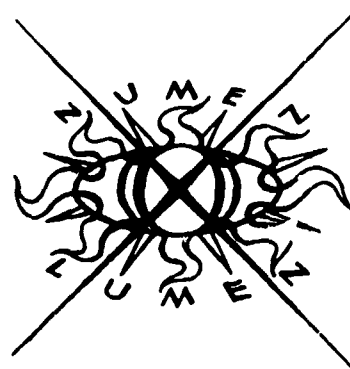
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ABSTRACT

A UNIVAC 1108 Computer has been used to obtain exact values for λ_p ($p = 1, 2, \dots, N$), the non-zero characteristic values of Zimm's matrix HA , for values of N (the number of Gaussian springs per molecule) up to 300; values previously published did not go above $N = 15$ (Thurston and Morrison). For future comparison with elastic and viscous properties of very dilute polymer solutions measured in steady and in oscillatory shear flow, several useful functions of the λ_p are computed and tabulated for parameter values in the ranges $2 \leq N \leq 300$, $0.05 \leq h^* \leq 0.3$, where $h^* (= hN^{-1/2})$ is a dimensionless "friction constant"; h denotes the "hydrodynamic interaction parameter" of Zimm. For selected parameter values, certain of the functions are compared graphically with the corresponding functions given by Tschoegl on the basis of approximate calculations using an indefinitely large value for N . The present calculations differ from those of Zimm and Tschoegl in only two ways: finite values of N are used (instead of $N = \infty$), and exact values of λ_p are computed from an $N \times N$ matrix equation (instead of approximate values from an approximate integro-differential equation). An important new result of the present computation is that, for the particular value $h^* = 0.262$, Flory's intrinsic viscosity function Φ is substantially independent of N in the range $50 \leq N \leq 300$ and there has the value 2.85×10^{23} ml/g; this equals the value given by Zimm's original approximate calculation for the case $N = \infty$, $h \gg 1$. This suggests that the interpretation of intrinsic viscosity data in terms of the well-known 'non-free-draining' concept should be reconsidered.

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EXACT RELAXATION TIMES AND DYNAMIC FUNCTIONS FOR DILUTE POLYMER SOLUTIONS FROM THE BEAD/SPRING MODEL OF ROUSE AND ZIMM^{*}

A. S. Lodge and Yeen-Jing Wu

1. Introduction

In the well-known theories of Rouse (1) and Zimm (2) for very dilute solutions of long-chain ('linear polymer') molecules, each polymer molecule is represented by N equal 'thermal motion' 'Gaussian' springs connected end-to-end; the solvent is treated as a constant-temperature environment for the polymer molecules and also as a Newtonian incompressible liquid, of viscosity η_s , which interacts with each polymer molecule only at $N + 1$ point centers ('beads') situated at the ends of the N springs. Each bead has the same 'friction constant' f_0 (which would be equal to $6\pi a\eta_s$ if the bead were a rigid sphere of radius a treated according to Stokes' law). Each spring has the same root-mean-square end-to-end distance b when the solution is not flowing.

Compared with earlier theories (3) in which equal friction constants were assigned to each atom on the 'backbone' of a polymer molecule, the bead/spring theory of Rouse and Zimm involves an extra artificial feature, namely, the concentration of polymer-solvent hydrodynamic interaction at the $N + 1$ fictitious beads. The advantages arising from the simpler mathematics involved, however, are considerable: the dynamic viscosity η' and dynamic rigidity G'

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as functions of angular frequency ω , for oscillatory small-amplitude shear, have been calculated (1, 2, 4) and compared rather extensively with experimental data (5); more recently, the (macroscopic) constitutive equations, from which all rheological properties in isothermal homogeneous flows can be calculated, have been derived by Lodge and Wu (6), who also list all the assumptions involved in the theory. Precise calculation of the dynamic functions $\eta'(\omega)$, $G'(\omega)$ has recently assumed added importance because improvements in experimental techniques have made possible the extrapolation to zero polymer concentration of the data obtained (7, 8); such 'intrinsic' data can thus properly be compared with the predictions of the bead/spring theory which is based on neglect of interactions between different polymer molecules.

In order to compute the functions $\eta'(\omega)$, $G'(\omega)$, it is necessary to compute the characteristic values λ_p ($p = 1, 2, \dots, N$) of the symmetric matrix $N \times N$ $B = [B_{pq}]$ whose elements B_{pq} are given by the equations

$$B_{pq} = H_{pq} + H_{p-1,q-1} - H_{p-1,q} - H_{p,q-1} \quad (p, q = 1, 2, \dots, N), \quad [1.1]$$

where

$$H_{ij} = \begin{cases} 1 & (i = j) \\ 2^{1/2} h^* |i-j|^{-1/2} & (i, j = 0, 1, 2, \dots, N), \\ & (i \neq j) \end{cases} \quad [1.2]$$

$$h^* = f_0 / [(12\pi^3)^{1/2} \eta_s b] \quad [1.3]$$

The matrix B has been introduced by Lodge and Wu (6) as a more convenient alternative to Zimm's singular, non-symmetric, matrix HA which has the characteristic values $0, \lambda_1, \lambda_2, \dots, \lambda_N$ (6); $H = [H_{ij}]$, and A is defined in equation (11) of Zimm (2).

The object of the present paper is to present the results of computing 'exact' characteristic values $\lambda_1, \lambda_2, \dots, \lambda_N$ of the matrix B , together with various functions of the λ_p of interest for comparison with experimental data obtained in steady- and oscillatory-shear flow. Available computer storage facilities have enabled us to use values of N up to 300, which may well prove to be sufficient for the highest-molecular-weight polymers available. The only other published exact computations (for non-zero h^*) are those of Thurston and Morrison (9), whose restriction $N \leq 15$ is rather severe.

We call our values for λ_p 'exact' to distinguish between them and the approximate values obtained by Zimm, Roe, and Epstein (10), Hearst (11), and Tschoegl (4) (Table 1), who replaced the discrete eigenvalue problem (associated with matrix equations involving B or HA) by a discrete eigenvalue problem associated with an integro-differential equation (equation (71) of Zimm (2)) regarded as an approximation to the actual matrix equation given by the Zimm model. The approximation involved here has been thought to be reliable when N is large; recently, however, partly as a result of comparing our exact values for λ_p with those obtained from the Zimm integro-differential equation, Osaki (12) has noted that Zimm's equation is incorrectly derived from the matrix equation, and that the corrected equation is the following:

$$\alpha(r)(1 - 4h^*) + h \int_{-1}^1 \alpha''(s) |r - s|^{-1/2} ds = -N^2 \lambda \alpha(r) / 4. \quad [1.4]$$

Zimm's equation omits the term $-4h^* \alpha(r)$. Zimm's parameter h is given by the equation

$$h = h^* N^{1/2}. \quad [1.5]$$

In Table 1, the notation $h \gg 1$ (used by Zimm) means that, on the left-hand side of [1.4], the integral term alone is retained; as Osaki (12) has observed, this case really corresponds to the value $h^* = 0.25$ (and N large) when the correct approximate equation [1.4] is used.

TABLE 1: Calculations of characteristic values λ_p for the bead/spring theory of Rouse and Zimm

	N	h	h^*	
1. Rouse (1)	1 to ∞	0	0	exact
2. Zimm, Roe, and Epstein (10)	large	$\gg 1$		approximate
3. Hearst (11)	large	> 0		approximate
4. Tschoegl (4)	large	> 0		approximate
5. Thurston and Morrison (9)	1 to 15		0 to 0.4	exact
6. Wu (13)	1 to 222		0.05 to 0.3	exact
7. Lodge and Wu (this paper)	2 to 300		0.05 to 0.3	exact

In view of the idealization inherent in the bead/spring model and various approximations used in Zimm's analysis of this model (on which our

present calculations and all the calculations of Table 1 are based), it might be argued that the present computations amount to hair splitting; we recognize the weaknesses that remain, but consider that it is worth while making the present computations if only to eliminate any easily avoidable approximations in the analysis of the model and so render it more open to critical examination. Pyun and Fixman (14) have made certain calculations based on the bead/spring model without using one of Zimm's assumptions (namely, that the Oseen hydrodynamic interaction tensor can be replaced by its value averaged in the solution at rest); Wu (13) has compared results of Pyun and Fixman's calculations with the results of the present paper.

The characteristic values λ_p are dimensionless functions of the parameters N, h^* . Certain constants τ_p , called 'relaxation times', defined by the equations

$$\tau_p \lambda_p = (\pi^3/3)^{1/2} \eta_s b^3 h^* / (kT) \quad (p = 1, 2, \dots, N), \quad [1.6]$$

where k and T denote Boltzmann's constant and absolute temperature, play a fundamental role in the theory. The present report thus computes exact relaxation times in terms of three parameters, whose values are unknown a priori. The selection of these three parameters may be made in various ways, some of which are listed in Table 2.

TABLE 2. Selections of three basic parameters

1. N, f_0, b	N springs per molecule; f_0 = bead friction constant; b = r.m.s. spring length at rest;
2. N, h^*, b	$h^* = f_0 / [(12\pi^3)^{1/2} \eta_s b]$;
3. N, h^*, τ_1	$\tau_1 = f_0 b^2 / [6 kT \lambda_1(N, h^*)]$;
4. N, h, τ_1	$h = h^* N^{1/2}$;
5. N, h^*, τ_0	$\tau_0 = \sum_{p=1}^N \tau_p$;
6. m_1, h^*, b	$m_1 = M/N$ (M = polymer molecular weight).

We follow the usual notation according to which $\lambda_1 < \lambda_2 < \dots < \lambda_N$. λ_1 is thus the smallest characteristic value, and hence τ_1 is the greatest relaxation time.

2. Computation of $\lambda_1, \lambda_2, \dots, \lambda_N$.

$\lambda_1, \lambda_2, \dots, \lambda_N$ are the roots in λ of the equation

$$\det (B_{pq} - \lambda \delta_{pq}) = 0. \quad [3.1]$$

When $h^* = 0$, the roots are given by the equations

$$\lambda_p = 4 \sin^2 [p\pi/2(N+1)] \quad (p = 1, 2, \dots, N) \quad [3.2]$$

given by Rouse (1). When $h^* \neq 0$, the roots for the cases $N = 1, 2$ are as follows:

$$\lambda_1 = 2(1 - 2^{1/2} h^*) \quad (N = 1) ;$$

[3.3]

$$\lambda_1 = 1 - h^*, \quad \lambda_2 = 3 + (1 - 2^{1/2} h^*) \quad (N = 2) .$$

For $h^* \neq 0$ and $N > 3$, we know of no method of obtaining a solution for the λ_p in closed form. To obtain solutions by numerical methods, a Fortran program was written in order to compute roots of [3.1] by means of a combination of Householder's method and the 'Q-R method'; the University of Wisconsin-Madison Computing Center's UNIVAC 1108 and 'BUMP 2' Library Subroutine were used; in this way, values of $\lambda_1, \lambda_2, \dots, \lambda_N$ were obtained for various values of h^* and for values of N up to 222 (13); computer storage limitations made it impossible to handle higher values of N using this program. Subsequently, use was made of the fact that B is symmetric, and a modified Miami University Program (H. J. Wertz version, dated 4/5/68) for handling packed matrices enabled the computations to be extended up to values of $N = 300$. To compute a complete set of characteristic values for a given value of N and a given value of h^* , the following times were required:

N:	25	50	100	200	300
Time in seconds:	0.3	1.6	10	70	235 .

These times do not vary much with h^* .

Table 3 contains the results of computing various functions of the λ_p . The values of λ_1 and λ_N are tabulated. Values of $\lambda_2, \lambda_3, \dots, \lambda_{N-1}$ have not been tabulated here, but are available on request to one of the authors (A. S. L.); some have been tabulated by Wu (13).

The following checks on the computation confirm the reliability of the results and indicate that the computational error in Table 3 entries should nowhere exceed unity in the fourth significant figure:

1. Values obtained for λ_p are consistent with the equation

$$\sum_{p=1}^N \lambda_p = \text{Trace } B; \quad [3.1]$$

2. For $N = 1, 2, \dots, 15$, and various values of h^* , the values obtained for λ_p agree with those computed by Thurston and Morrison (9);
3. For $N = 1, 2$, values of λ_p are consistent with [3.3];
4. For $N = 50, 100, 200$ and $h^* = 0.1, 0.2, 0.3$, most of the tabulated functions were computed using both programs referred to above; comparison of entries showed agreement to three significant figures and, in most cases examined, to four significant figures; a few entries showed differences of unity in the fourth significant figure.

A minor advantage in using h^* , rather than h , as a parameter in the tabulation is that h^* has an upper limit, while h does not (assuming that N could be indefinitely great). We have chosen values of h^* in the interval $0.05 \leq h^* \leq 0.3$. Thurston and Morrison (9) quote the value 0.471 for the upper bound of h^* , but do not give details of their derivation; in an attempt to follow their argument, we obtain the value 0.65. Alternatively, using the very crude argument that $f_0 = 6\pi a \eta_s$ for a rigid spherical bead of radius a , the inequality $2a < b$ yields the result $h^* < 0.49$. Because of

the artificiality inherent in the model, we do not place much weight on the actual value of the upper bound on h^* given by such arguments; it seems reasonable, however, to suppose that there is an upper bound. Independent arguments based on a comparison of the results of the present calculations with measured data on intrinsic viscosity of polymer solutions suggest that the useful range for h^* is $0 < h^* \leq 0.26$. This range is fairly well covered by the entries in Table 3. Thurston and Morrison (9) have noted that the condition $h^* < 0.65$ is sufficient to ensure that λ_p shall be positive for $N = 1, 2$ (cf. [3.3]).

3. Steady shear flow functions

In the usual notation, we express the intrinsic viscosity $[\eta]$ in the form

$$[\eta] := \lim_{c \rightarrow 0} \frac{\eta - \eta_s}{c\eta_s} = \Phi \langle r^2 \rangle^{3/2} M^{-1} \quad [3.1]**$$

where c is the polymer concentration in g/ml, η is the solution viscosity, and $\langle r^2 \rangle$ is the mean square end-to-end distance of a polymer molecule in the solution at rest. This equation may be regarded as a definition of the quantity Φ . The bead/spring theory gives the following equation for

$$\Phi = \Phi(N, h^*):$$

$$\Phi = (\pi^3/3)^{1/2} N_a h^* N^{-3/2} \sum_{p=1}^N \lambda_p^{-1}, \quad [3.2]$$

where $N_a = 6.0228 \times 10^{23}$ (Avogadro's number).

** The notation $A := B$ means "A is defined by the equation $A = B$ ".

In Table 3, values of Φ are tabulated for various values of N and h^* . For comparison with the approximate values calculated by Tschoegl for $N = \infty$, the values of Φ have been plotted as functions of $\log h$ in Figure 1. It is seen that the experimentally-interesting range of values for Φ , namely $2.5 \leq 10^{-23} \Phi \leq 2.9$, are obtained with values of N in the range $25 \leq N \leq 300$ and values of h^* near 0.25, when the exact characteristic values are used, and with large values of h when the approximate characteristic values (with $N = \infty$) are used. In particular, for the special value $h^* = 0.262$, Table 3 gives the following values for Φ (in g/ml):

N:	8	25	50	100	200	300	
							[3.3]
$10^{-23} \Phi$:	2.954	2.864	2.853	2.852	2.855	2.856	($h^* = 0.262$)

For $25 \leq N \leq 300$, it is seen that $\Phi(N, h^*)$ (with $h^* = 0.262$) is substantially independent of N and that its value is close to the value 2.84×10^{23} obtained by Zimm (2) from the approximate calculation based on the values $N = \infty$, $h \gg 1$.

The case $h \gg 1$ is described by Zimm (2) as the "non-free-draining case", presumably because a large value of h is associated with a predominating bead-bead hydrodynamic interaction term in the equations of motion for a bead/spring unit and this in turn is believed to imply that, within a surface enveloping the polymer molecule, there is a substantial region of solvent which is 'immobilized' by the polymer molecule in the sense that the solvent velocity

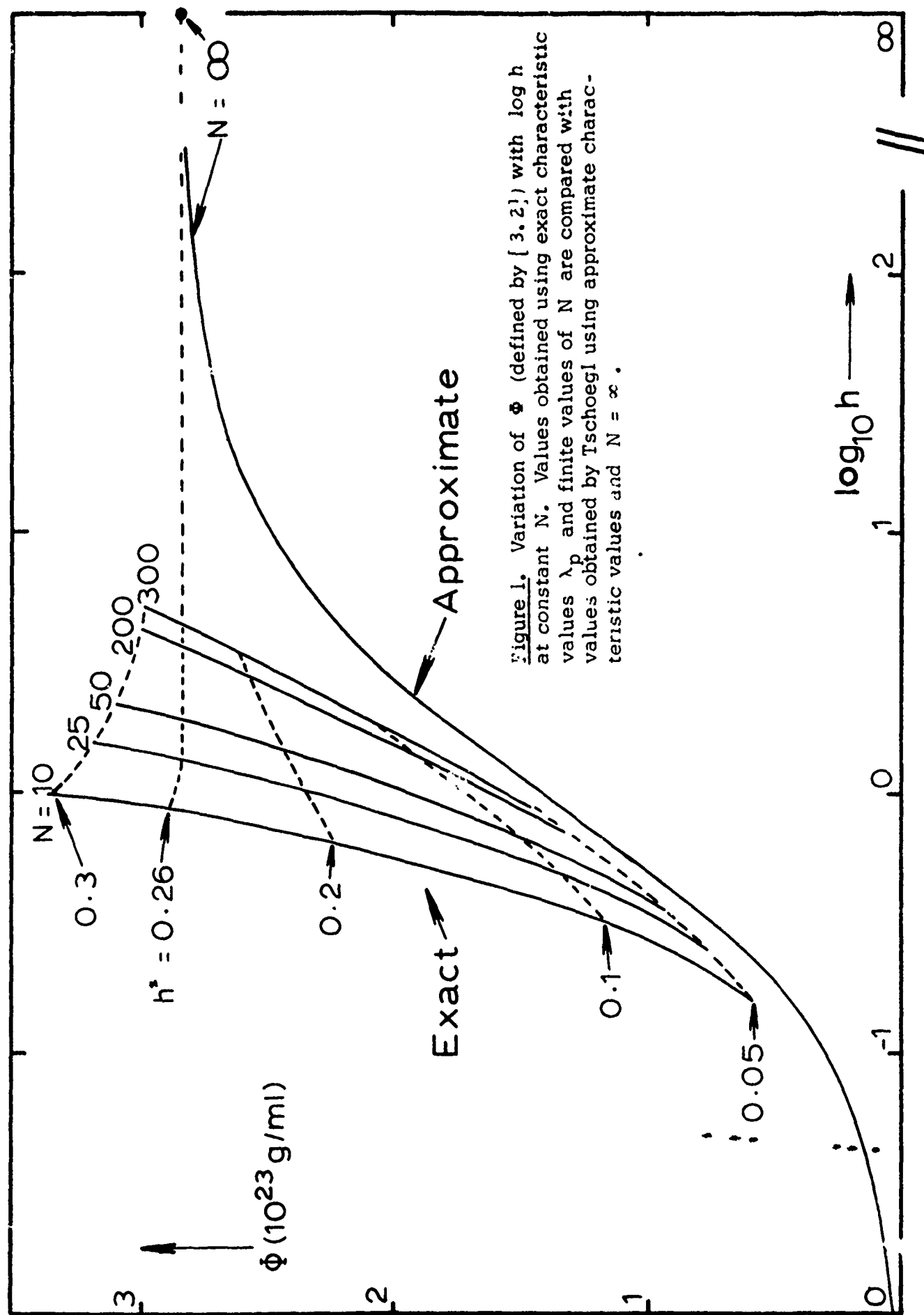


Figure 1. Variation of Φ (defined by [3.2]) with $\log h$ at constant N . Values obtained using exact characteristic values λ_p and finite values of N are compared with values obtained by Tschoegl using approximate characteristic values and $N = \infty$.

equals some average polymer molecule velocity. Whether or not this concept could be substantiated for the case $h \gg 1$ by calculation of solvent and polymer velocities using the equations of the Zimm theory, our present results suggest that the concept of the non-free-draining limit may not in fact be appropriate for dilute solutions of linear polymers for which Φ has a value near 2.85×10^{23} g/ml: using our exact characteristic values, such a value is obtained when $h^* = 0.262$, and there seems to be no a priori reason for thinking that this value of the dimensionless friction constant is so large that partial or complete 'solvent immobilization' should occur.

In Figure 2, the data are replotted to show the variation of $\log \Phi$ with h^* at constant N ; the fact that the curves for $N \geq 25$ pass approximately through a common point (whose abscissa is 0.262) reflects the results [3.3].

For comparison of the theory with the experimentally determined molecular weight dependence of the intrinsic viscosity, Thurston and Morrison (9) make the reasonable assumption that N is proportional to M . For limited ranges of M values, both $[\eta]$ and $\langle r^2 \rangle$ (determined from light-scattering data) vary approximately as powers of M . In this connection, it is of interest to note that, according to our calculations, Φ can be represented approximately by an equation of the form

$$\Phi(N, h^*) = a_1(h^*) N^{n_1(h^*)} \quad [3.4]$$

for limited ranges of values of N ; the dependence of the index n_1 on h^* is shown in Figure 3: the fact that two curves are given for different ranges of

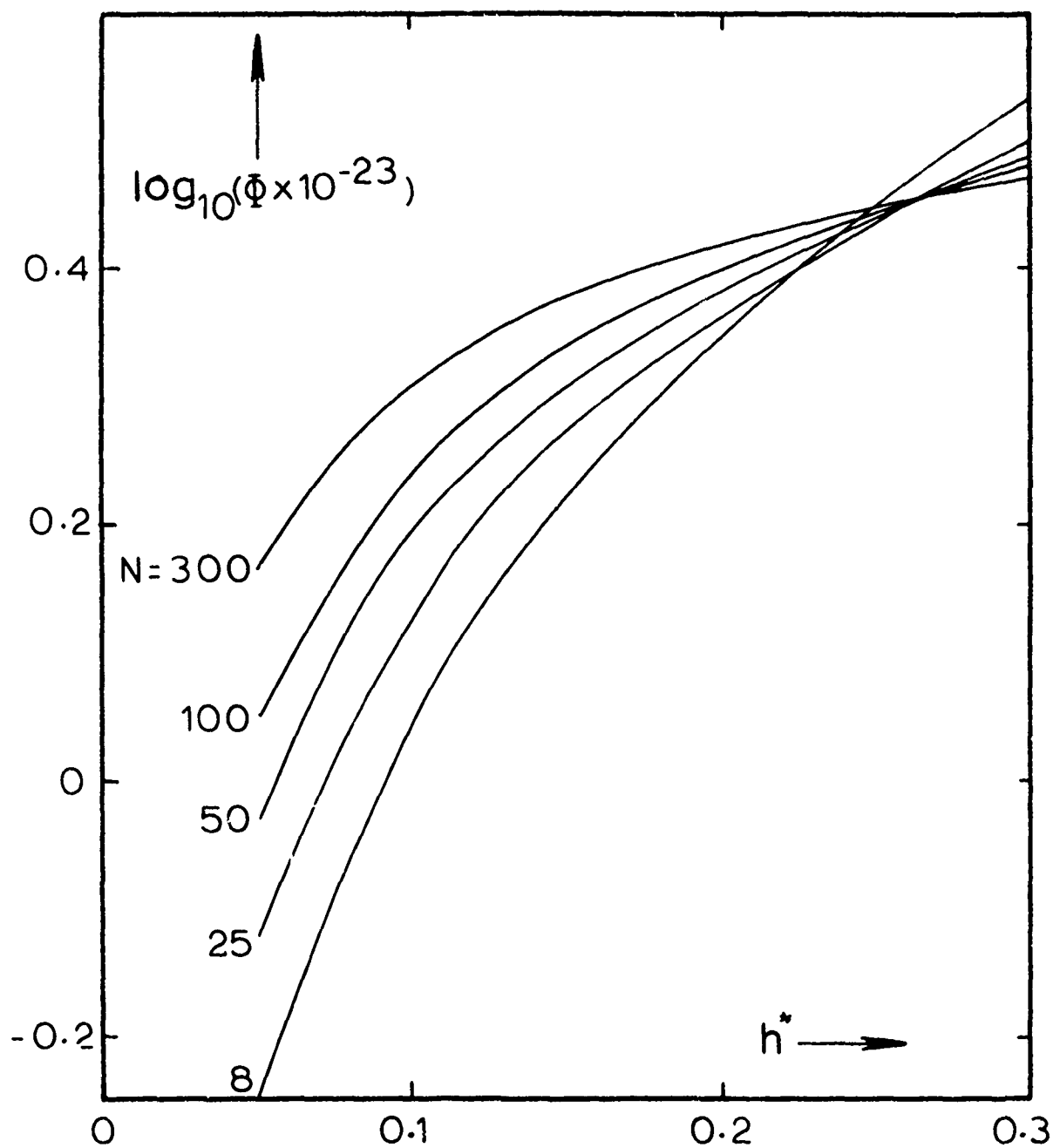


Figure 2. Variation of $\log \Phi$ with h^* at constant N calculated from [3.2] using exact characteristic values λ_p .

N reflects the fact that [3.4] is only an approximate representation of the dependence of Φ on N. Again, the fact that $n_1 = 0$ when $h^* = 0.262$ is a reflection of [3.3].

In Figures 4, 5, the quantities

$$\tau_0/\tau_1 = \frac{\sum_{p=1}^N \tau_p/\tau_1}{\sum_{p=1}^N \lambda_1/\lambda_p}, \quad [3.4]$$

$$J_{eR} = \frac{\sum_{p=1}^N \tau_p^2}{\left(\sum_{p=1}^N \tau_p\right)^2} = \frac{\sum_{p=1}^N \lambda_p^{-2}}{\left(\sum_{p=1}^N \lambda_p^{-1}\right)^2}, \quad [3.6]$$

are represented as functions of $\log h$ at constant values of N, and are compared with the corresponding quantities evaluated by Tschoegl (for $N \rightarrow \infty$) using approximate characteristic values.

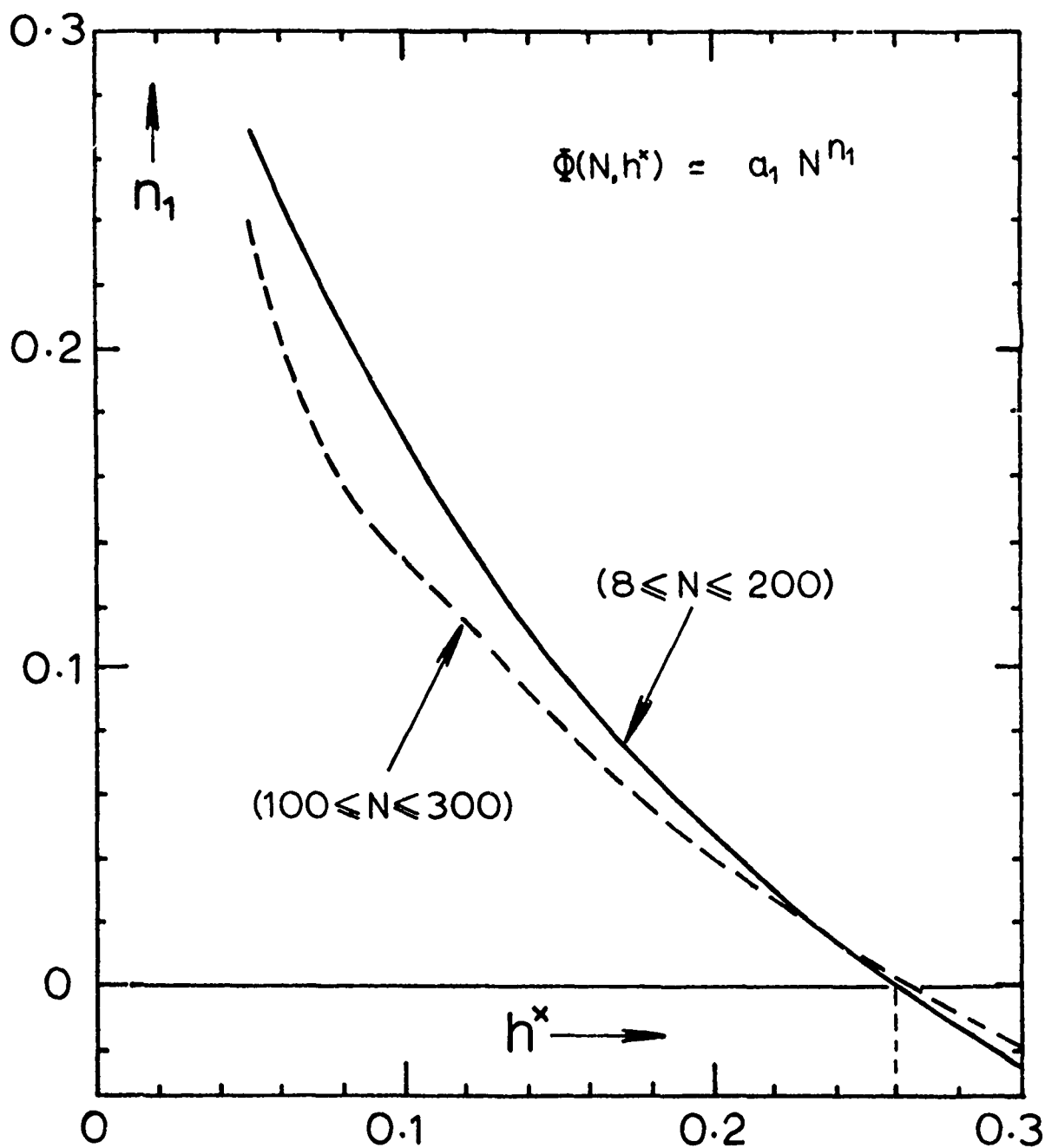


Figure 3. Dependence of index n_1 on h^* , where $\Phi(N, h^*)$, calculated from [3.2] using exact characteristic values λ_p , is represented approximately by [3.4].

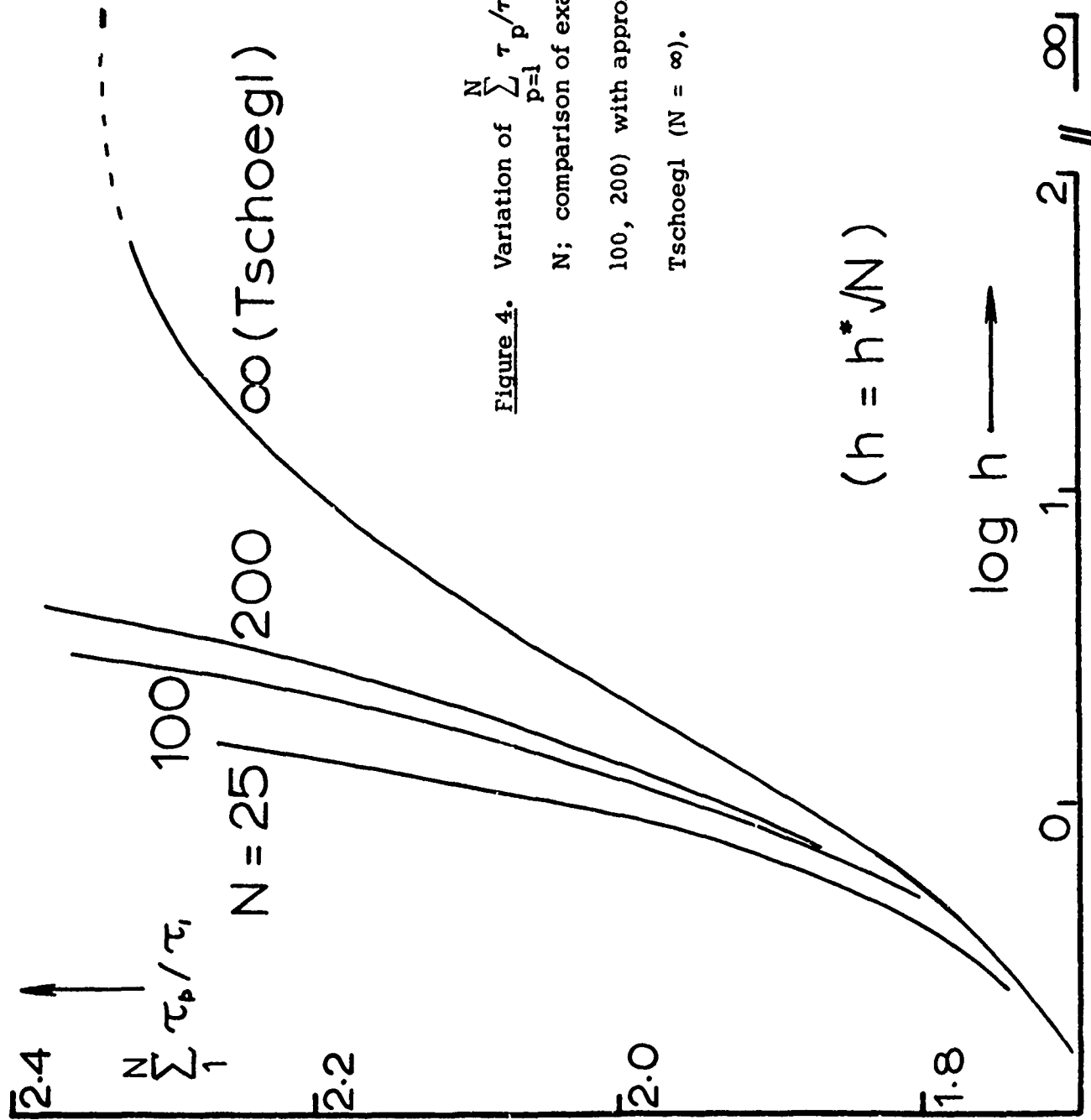
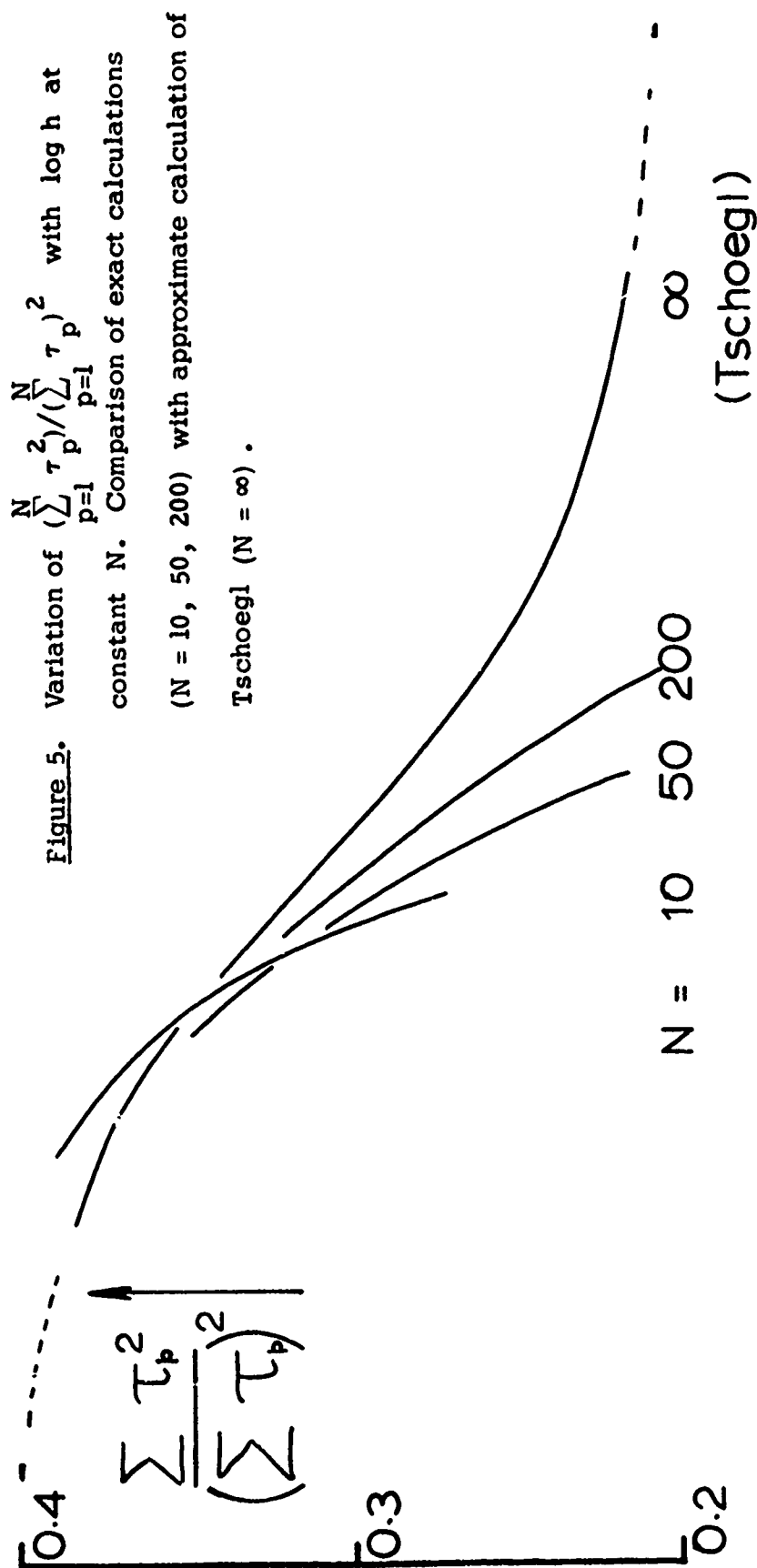


Figure 4. Variation of $\sum_{p=1}^N \tau_p / \tau_1$ with $\log h$ at constant N ; comparison of exact calculations ($N = 25, 100, 200$) with approximate calculations of Tschoegl ($N = \infty$).

$$(h = h^* \sqrt{N})$$



$$(h = \hbar^* \sqrt{N})$$

$$\log h \longrightarrow$$

4. Small-strain oscillatory shear

According to the bead/spring theory (2), the dynamic viscosity η' and dynamic rigidity G' in a state of steady sinusoidal oscillatory shear of small strain amplitude satisfy the equations

$$\lim_{c \rightarrow 0} \frac{\eta' - \eta_s}{c} = \frac{RT}{M} \tau_1 \eta'_R(N, h^*, \omega \tau_1), \quad [4.1]$$

$$\lim_{c \rightarrow 0} \frac{G'}{c\omega} = \frac{RT}{M} \tau_1 \eta''_R(N, h^*, \omega \tau_1), \quad [4.2]$$

where $R = kN_a$,

$$\eta'_R := \sum_{p=1}^N \frac{\lambda_1}{\lambda_p} \left\{ 1 + \left(\omega \tau_1 \frac{\lambda_1}{\lambda_p} \right)^2 \right\}^{-1}, \quad [4.3]$$

$$\eta''_R := \omega \tau_1 \sum_{p=1}^N \left(\frac{\lambda_1}{\lambda_p} \right)^2 \left\{ 1 + \left(\omega \tau_1 \frac{\lambda_1}{\lambda_p} \right)^2 \right\}^{-1}, \quad [4.4]$$

and ω denotes the angular frequency. The greatest relaxation time τ_1 , according to [1.6], is given by the equation

$$\tau_1 = \tau_1(N, h^*, b) = \left(\frac{\pi^3}{3} \right)^{1/2} \frac{\eta_s}{kT} \frac{b^3 h^*}{\lambda_1(N, h^*)}, \quad [4.5]$$

and is thus a function of the three parameters N, h^*, b .

Using the exact characteristic values, the functions $\eta'_R(N, h^*, \omega \tau_1)$ and $\eta''_R(N, h^*, \omega \tau_1)$ have been computed for values of N, h^* , and $\log_{10} \omega \tau_1$ in ranges of practical interest. The results, together with values of related functions of interest, are given in Table 3.

In figures 6-9, $\log \eta'_R$ and $\log \eta''_R$ are plotted as functions of $\log \omega \tau_0$, where τ_0 is defined by the equation

$$\tau_0 := \sum_{p=1}^N \tau_p. \quad [4.6]$$

τ_0 is a convenient dimensionless variable to choose for the abscissa when comparing dynamic functions η'_R and η''_R obtained using different values of parameters N , h^* and different methods of calculation (exact and approximate): from [4.1], [4.3] and the fact that $\eta = \eta'$ when $\omega = 0$, it follows that

$$[\eta] = \frac{RT}{M\eta_s} \tau_0. \quad [4.7]$$

Comparison of curves using the abscissa $\log \omega \tau_0$ thus amounts to comparison at constant $[\eta]$.

From Figure 6, it is seen that there is a small but significant difference between the exact and the approximate curves when $h = 2$; the differences at the largest values of $\log \omega \tau_0$ doubtless reflect the difference in values of N (100, ∞) used in the comparison (see also Figure 7); the difference in curves at lower frequencies is attributed to errors arising in the approximate calculation (based on the use of [1.4] without the term $-4h^* \alpha(r)$).

From Figure 7, it is seen that, when $h^* = 0.3$, a change in the value of N from 50 to 200 leaves the low-frequency behavior substantially unaltered but moves the point of intersection of the η'_R -curve and the η''_R -curve to higher frequencies.

Figures 8 and 9 compare the Zimm curves ($N = \infty$, $h \gg 1$) with the exact curves for high ($h^* = 0.3$) and low ($h^* = 0.1$) values of the friction constant.

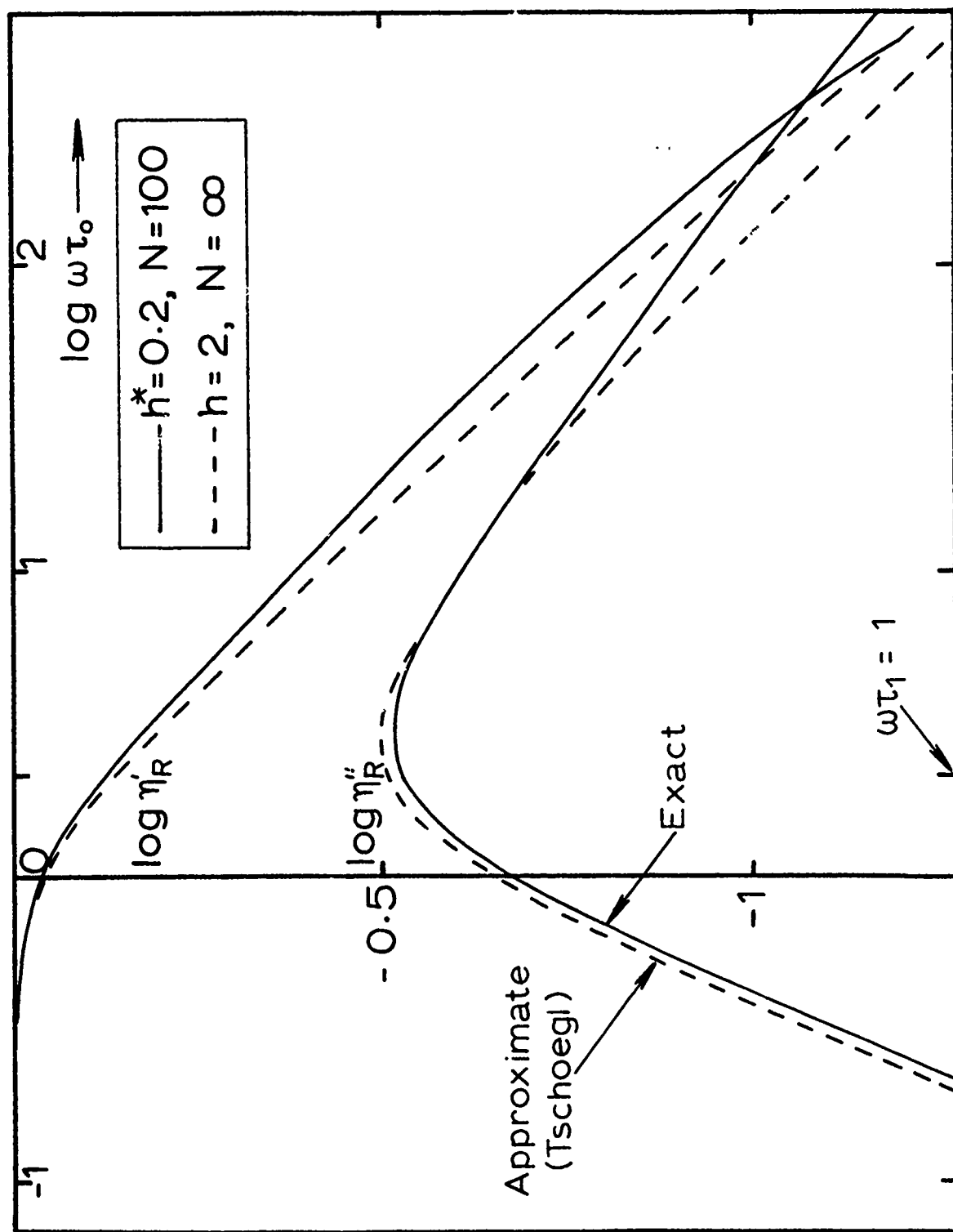


Figure 6. Reduced dynamic functions versus frequency. Comparison of exact calculation ($N = 100$) with approximate calculation ($N = \infty$) of Tschoegl for the case $h = 2$.

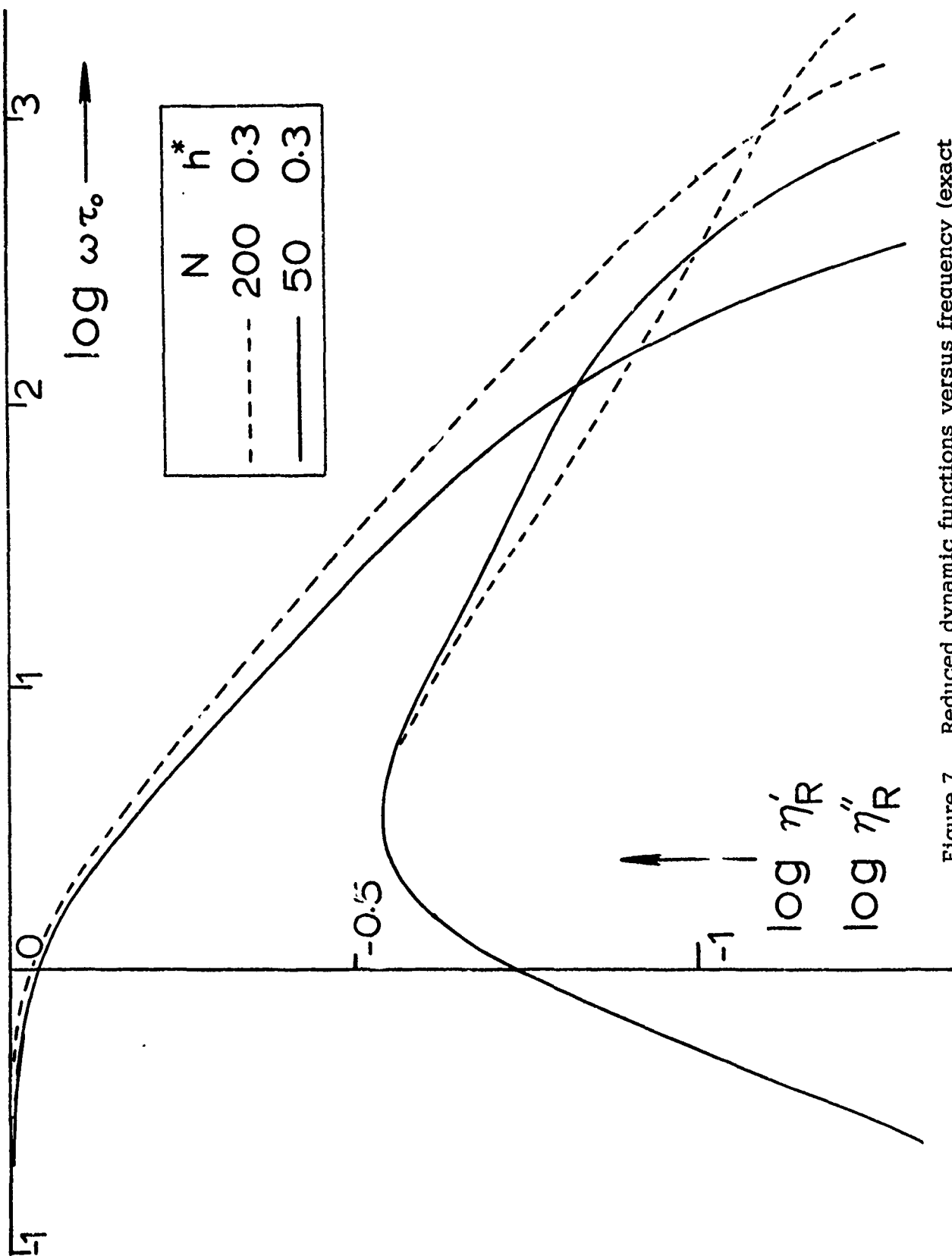


Figure 7. Reduced dynamic functions versus frequency (exact calculations). * Comparison of $N = 50$ and $N = 200$ for the case $h = 0.3$.

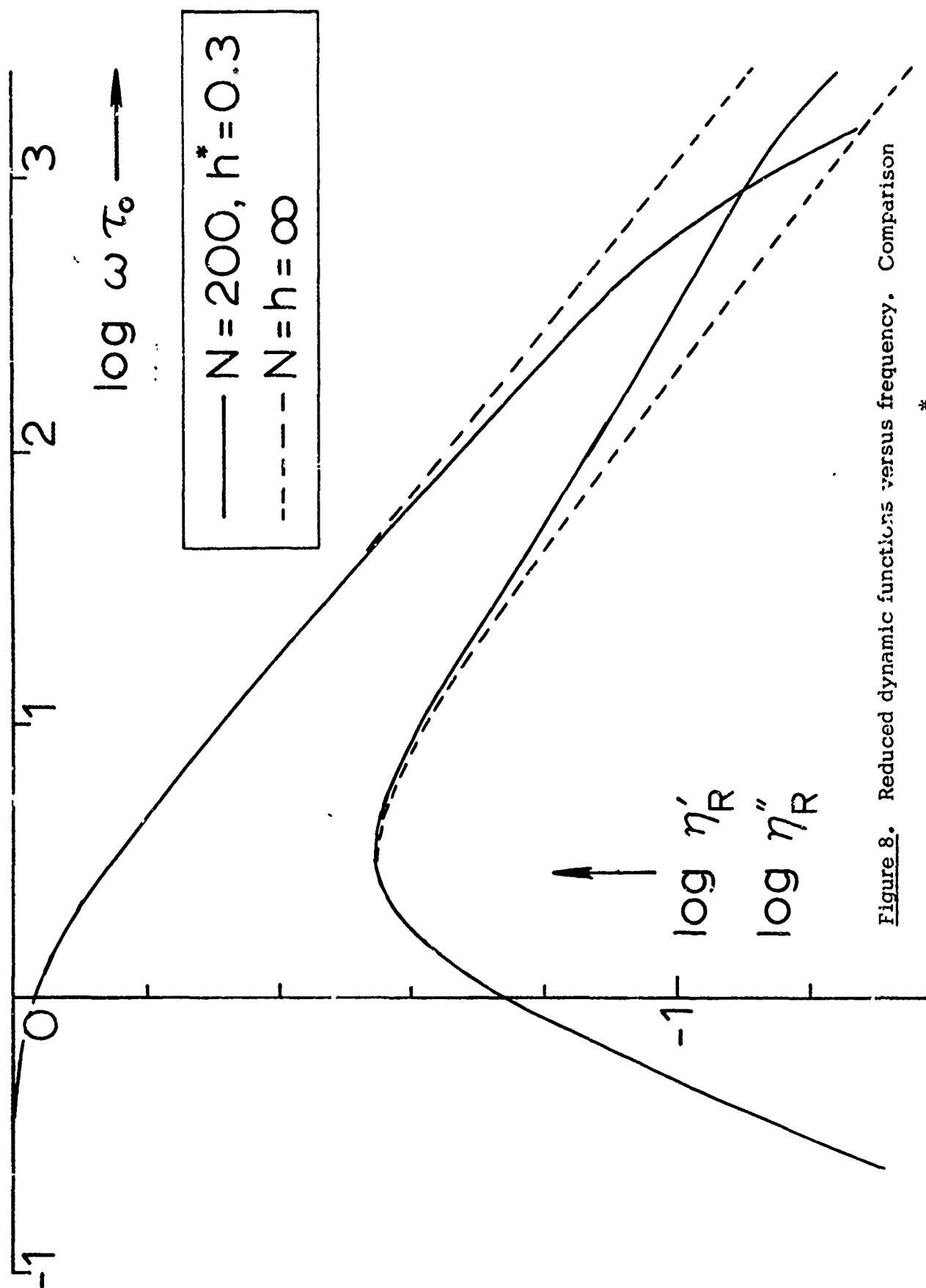


Figure 8. Reduced dynamic functions versus frequency. Comparison of exact calculations ($N = 200, h^* = 0.3$) with approximate calculations ($N = \infty, h \gg 1$) of Zimm.

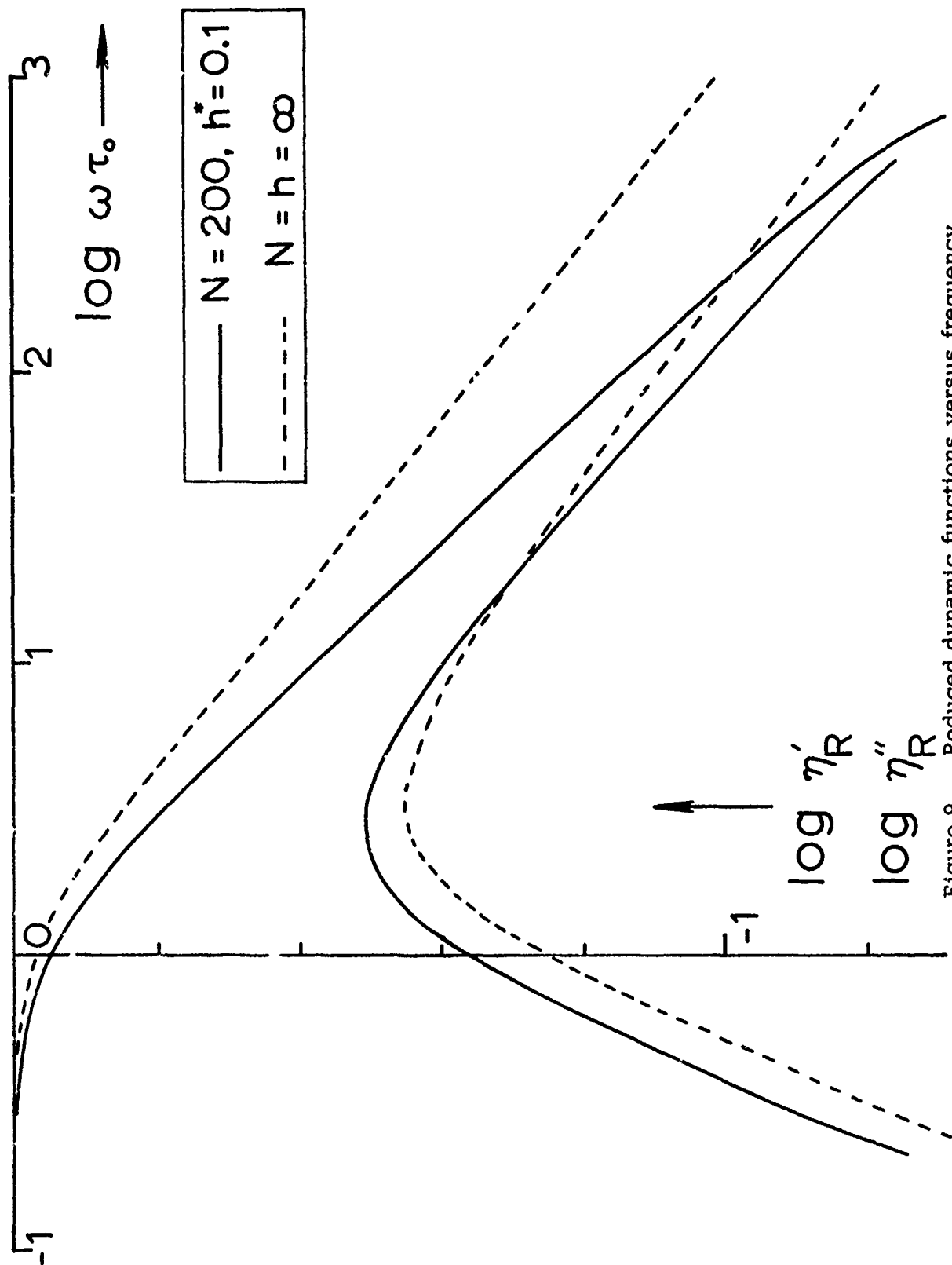


Figure 9. Reduced dynamic functions versus frequency.*
 Comparison of exact calculations ($N = 200, h^* = 0.1$)
 with approximate calculations ($N = \infty, h \gg 1$) of Zimm.

It is intended, in a future publication, to present results of a comparison of the present calculations with experimental data giving the variation of $[\eta]$ with M and of η' and G' with ω .

5. Discussion

The present calculations are simply an extension of the calculations of Thurston and Morrison (9) to values of N up to 300. In comparison with the earlier calculations of Zimm and Tschoegl, the importance of our calculations and those of Thurston and Morrison is twofold: (i) our calculations are exact (within the confines of the Zimm treatment of the bead/spring model); and (ii) N , the number of springs per polymer molecule, appears as an additional parameter whose value is at our disposal when we wish to compare theoretical predictions with experimental data on any given solution of linear polymer molecules of equal molecular weight.

It is possible that (ii) is more important, and more open to question, than (i). Thurston and Morrison (9) have already made use of (ii) in offering a possible interpretation of the dependence of $[\eta]$ on M , using the assumption that N is proportional to M for a given polymer/solvent system. Thurston and Schrag (15) have similarly interpreted their experimental data on oscillatory flow birefringence; for values of M down to 10^3 , they use values of N down to 1 for the polystyrene/Aroclors system.

We do not propose here to embark on a comprehensive discussion of the issues raised by the use of N as a parameter, but we do recognize that

this use is open to the criticism that N is too closely connected with the main artificial feature of the bead/spring model (namely, the arbitrary concentration of hydrodynamic interaction at discrete points on the Gaussian spring system) to provide a meaningful parameter having significance for any actual polymer solution. Awareness of this criticism no doubt influenced the early applications of the bead/spring theory (1, 2, 4, 5) in which the equations were cast in a form in which N did not appear: this was achieved partly taking $N = \infty$ in the upper limits of sums in equations such as [3.2], [3.4], and [3.6] and partly by the use of the integro-differential eigenvalue equation for the case of very large N . On the other hand, the use of very large values of N is itself open to criticism: for a given polymer molecule, a certain minimum number (perhaps not well-defined, but nonetheless real) of backbone bonds are required in order that the corresponding part of the molecule may be approximately treated as a Gaussian spring; furthermore, the fact that N may not appear in an equation does not, by itself, eliminate the dependence of the equation on the artificial feature of the model.

We are perhaps on safer ground if we confine applications of the bead/spring theory to properties for which the results predicted by the theory are insensitive to the value of N ; an example is furnished by the low-frequency behavior of the dynamic functions shown in Figure 7. On the other hand, it is just conceivable that a more fundamental treatment of polymer/solvent dynamics than that represented by the bead/spring idealization could furnish criteria for the validity of the bead/spring idealization (with finite N)

as an approximation. We hope that the calculation of the present report, when compared critically with suitable experimental data, might lead to a better understanding of the justification for and limitations of the bead/spring model.

Acknowledgments

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Table 3: Exact characteristic values and steady-and oscillatory-shear-flow functions

Key to entries

L1	LN	1/(LN)	SUM 1/(LP)	SUM L1/LP	RECIP ROCAL	SUM (1/LP)2	SUM(L1 /LP)2	JER	PHI -23
λ_1	λ_N	λ_N^{-1}	$\sum_{l=1}^N \lambda_p^{-1}$	$\sum_{l=1}^N \frac{\lambda_1}{\lambda_p}$	$(\sum_{l=1}^N \frac{\lambda_1}{\lambda_p})^{-1}$	$\sum_{l=1}^N \frac{1}{\lambda_p^2}$	$\sum_{l=1}^N (\frac{\lambda_1}{\lambda_p})^2$	J_{eR}	$\Phi \times 10^{-23} \text{ g/ml}$
[3.1]								[3.6]	[3.2]

LOG	OMTI	ETAIR	ETA2R	G1R	G2R	MOD ETAR	ARCTAN ETA2/1	H*
\log_{10}	$\omega \tau_1$	η'_R	η''_R	G'_R	G''_R	$ \eta'_R + i\eta''_R $	$\tan^{-1} \frac{\eta''_R}{\eta'_R}$	h^*
		[4.3]	[4.4]	$\omega \tau_1 \eta''_R$	$\omega \tau_1 \eta'_R$			

Exponential notation: .769-03 means 0.769×10^{-3} .

Parameter values

h^*	0.05	0.075	0.1	0.13	0.15	0.2	0.25	0.262	0.3
N									
2		X		X	X		X		
4		X	X	X	X	X	X		
8		X	X	X	X	X	X	X	
25	X	X	X	X	X	X	X	X	X
50	X	X	X	X	X	X	X	X	X
100	X	X	X	X	X	X	X	X	X
200	X	X	X	X	X	X	X	X	X
300	X	X	X	X	X	X	X	X	X

EXACT ZIMM EIGENVALUES
 LI LN LOG LN 1/(LN) SUM 1/(LP) RECIP SUM 1/(LP)2 JFR PH?
 .925+00 .265+01 .377+00 .145+01 1.349 .741 .131+01 1.1218 .616 .749

N= 2 H= .075

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD			ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	GIR	G2R	ETAR	ETA2/1
OMTI	ETAIR	ETA2R	GIR	G2P	ETAIR	ETA2R	GIR	G2R	ETAR	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1
-2.8	.130	-2.750	-5.550	-2.670	.135+01	.178-02	.282-05	.214-02	.135+01	.132-02	.132-02	.132-02	.132-02	.132-02
-2.0	.130	-1.950	-3.950	-1.870	.135+01	.112-01	.112-03	.135-01	.135+01	.832-02	.832-02	.832-02	.832-02	.832-02
-1.8	.130	-1.750	-3.550	-1.670	.135+01	.178-01	.282-03	.214-01	.135+01	.132-01	.132-01	.132-01	.132-01	.132-01
-1.4	.129	-1.351	-2.751	-1.271	.135+01	.446-01	.178-02	.536-01	.135+01	.331-01	.331-01	.331-01	.331-01	.331-01
-1.0	.127	-.954	-1.954	-.873	.134+01	.111+00	.111-01	.134+00	.134+01	.829-01	.829-01	.829-01	.829-01	.829-01
-.8	.122	-.760	-1.560	-.678	.132+01	.174+00	.276-01	.210+00	.133+01	.131+00	.131+00	.131+00	.131+00	.131+00
-.6	.110	-.574	-1.174	-.490	.129+01	.267+00	.670-01	.323+00	.131+01	.204+00	.204+00	.204+00	.204+00	.204+00
-.4	.081	-.408	-.808	-.319	.121+01	.391+00	.156+00	.480+00	.127+01	.314+00	.314+00	.314+00	.314+00	.314+00
-.2	.020	-.280	-.480	-.180	.105+01	.525+00	.331+00	.661+00	.117+01	.464+00	.464+00	.464+00	.464+00	.464+00
.0	-.091	-.216	-.216	-.091	.811+00	.609+00	.609+00	.811+00	.101+01	.644+00	.644+00	.644+00	.644+00	.644+00
.2	-.258	-.223	-.023	-.058	.552+00	.599+00	.949+00	.875+00	.815+00	.826+00	.826+00	.826+00	.826+00	.826+00
.4	-.476	-.287	.113	-.076	.334+00	.517+00	.130+01	.839+00	.615+00	.997+00	.997+00	.997+00	.997+00	.997+00
.6	-.748	-.396	.204	-.148	.178+00	.402+00	.160+01	.710+00	.440+00	.115+01	.115+01	.115+01	.115+01	.115+01
.8	-1.075	-.544	.256	-.275	.842-01	.206+00	.180+01	.531+00	.298+00	.128+01	.128+01	.128+01	.128+01	.128+01
1.0	-1.439	-.718	.282	-.439	.364-01	.191+00	.191+01	.364+00	.195+00	.138+01	.138+01	.138+01	.138+01	.138+01
1.2	-1.824	-.907	.293	-.624	.150-01	.124+00	.196+01	.238+00	.125+00	.145+01	.145+01	.145+01	.145+01	.145+01
1.4	-2.217	-1.102	.298	-.817	.607-02	.790-01	.199+01	.152+00	.793-01	.149+01	.149+01	.149+01	.149+01	.149+01
1.6	-2.615	-1.300	.300	-1.015	.243-02	.501-01	.193+01	.967-01	.502-01	.152+01	.152+01	.152+01	.152+01	.152+01
1.8	-3.013	-1.499	.301	-1.213	.969-03	.317-01	.200+01	.612-01	.317-01	.154+01	.154+01	.154+01	.154+01	.154+01
2.0	-3.413	-1.699	.301	-1.413	.386-03	.200-01	.200+01	.386-01	.200-01	.155+01	.155+01	.155+01	.155+01	.155+01
2.2	-3.813	-1.899	.301	-1.613	.154-03	.126-01	.200+01	.244-01	.126-01	.156+01	.156+01	.156+01	.156+01	.156+01
2.4	-4.213	-2.099	.301	-1.813	.613-04	.796-02	.200+01	.154-01	.796-02	.156+01	.156+01	.156+01	.156+01	.156+01
2.6	-4.613	-2.299	.301	-2.013	.244-04	.502-02	.200+01	.971-02	.502-02	.157+01	.157+01	.157+01	.157+01	.157+01
2.8	-5.013	-2.499	.301	-2.213	.971-05	.317-02	.200+01	.613-02	.317-02	.157+01	.157+01	.157+01	.157+01	.157+01
3.0	-5.413	-2.699	.301	-2.413	.387-05	.200-02	.200+01	.387-02	.200-02	.157+01	.157+01	.157+01	.157+01	.157+01
3.4	-6.213	-3.099	.301	-2.813	.613-06	.796-03	.200+01	.154-02	.796-03	.157+01	.157+01	.157+01	.157+01	.157+01
3.8	-7.013	-3.499	.301	-3.213	.971-07	.317-03	.200+01	.613-03	.317-03	.157+01	.157+01	.157+01	.157+01	.157+01
4.2	-7.813	-3.899	.301	-3.613	.154-07	.126-03	.200+01	.244-03	.126-03	.157+01	.157+01	.157+01	.157+01	.157+01
4.6	-8.613	-4.299	.301	-4.013	.244-08	.502-04	.200+01	.971-04	.502-04	.157+01	.157+01	.157+01	.157+01	.157+01
5.0	-9.413	-4.699	.301	-4.413	.387-09	.200-04	.200+01	.387-04	.200-04	.157+01	.157+01	.157+01	.157+01	.157+01

#1250

EXACT ZIMM EIGENVALUES
 LI LN I/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² /LP² PHI
 N= 2 H=.150
 .850+00 .230+01 .435+00 .161+01 1.369 .730 .157+01 1.1364 .606 1.654

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON			ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	G1R	G2R	ETAR	ETA2/1	
OMTI	FTAIR	ETA2R	G1R	G2R	ETA1P	ETA2R								
-2.8	.137	-2.744	-5.544	-2.663	.137+01	.180-02				.285-05	.217-02	.137+01	.132-02	
-2.0	.136	-1.945	-3.945	-1.864	.137+01	.114-01				.114-03	.137-01	.137+01	.830-02	
-1.8	.136	-1.745	-3.545	-1.664	.137+01	.190-01				.285-03	.217-01	.137+01	.132-01	
-1.4	.136	-1.345	-2.745	-1.264	.137+01	.452-01				.180-02	.544-01	.137+01	.330-01	
-1.0	.133	-.948	-1.948	-.867	.136+01	.113+00				.113-01	.136+00	.136+01	.827-01	
-.8	.128	-.754	-1.554	-.672	.134+01	.176+00				.279-01	.213+00	.136+01	.130+00	
-.6	.116	-.568	-1.168	-.484	.131+01	.270+00				.679-01	.328+00	.133+01	.204+00	
-.4	.088	-.401	-.801	-.312	.122+01	.397+00				.158+00	.499+00	.129+01	.313+00	
-.2	.028	-.273	-.473	-.172	.107+01	.573+00				.336+00	.672+00	.119+01	.464+00	
.0	-.084	-.208	-.208	-.084	.875+00	.620+00				.620+00	.825+00	.103+01	.644+00	
.2	-.252	-.213	-.013	-.052	.560+00	.612+00				.970+00	.897+00	.830+00	.830+00	
.4	-.475	-.278	.122	-.075	.335+00	.528+00				.133+01	.842+00	.625+00	.100+01	
.6	-.754	-.389	.211	-.154	.176+00	.408+00				.162+01	.701+00	.444+00	.116+01	
.8	-1.037	-.540	.260	-.287	.819-01	.288+00				.182+01	.517+00	.300+00	.129+01	
1.0	-1.454	-.716	.284	-.454	.351-01	.192+00				.192+01	.351+00	.195+00	.139+01	
1.2	-1.840	-.906	.294	-.640	.144-01	.124+00				.197+01	.229+00	.125+00	.146+01	
1.4	-2.235	-1.102	.298	-.835	.582-02	.791-01				.199+01	.146+00	.793-01	.150+01	
1.6	-2.632	-1.300	.300	-1.032	.233-02	.501-01				.199+01	.928-01	.502-01	.152+01	
1.8	-3.032	-1.499	.301	-1.232	.930-03	.317-01				.200+01	.587-01	.317-01	.154+01	
2.0	-3.431	-1.699	.301	-1.431	.371-03	.200-01				.200+01	.371-01	.200-01	.155+01	
2.2	-3.831	-1.899	.301	-1.631	.148-03	.126-01				.200+01	.234-01	.126-01	.156+01	
2.4	-4.231	-2.099	.301	-1.831	.588-04	.796-02				.200+01	.148-01	.796-02	.156+01	
2.6	-4.631	-2.299	.301	-2.031	.234-04	.502-02				.200+01	.931-02	.502-02	.157+01	
2.8	-5.031	-2.499	.301	-2.231	.931-05	.317-02				.200+01	.598-02	.317-02	.157+01	
3.0	-5.431	-2.699	.301	-2.431	.371-05	.200-02				.200+01	.371-02	.200-02	.157+01	
3.2	-5.831	-2.899	.301	-2.631	.588-06	.796-03				.200+01	.148-02	.796-03	.157+01	
3.4	-6.231	-3.099	.301	-2.831	.931-07	.317-03				.200+01	.588-03	.317-03	.157+01	
3.6	-6.631	-3.299	.301	-3.031	.148-07	.126-03				.200+01	.234-03	.126-03	.157+01	
3.8	-7.031	-3.499	.301	-3.231	.234-08	.502-04				.200+01	.931-04	.502-04	.157+01	
4.0	-7.431	-3.699	.301	-3.431	.371-09	.200-04				.200+01	.371-04	.200-04	.157+01	
4.2	-7.831	-3.899	.301	-3.631										
4.4	-8.231	-4.099	.301	-3.831										
4.6	-8.631	-4.299	.301	-4.031										
4.8	-9.031	-4.499	.301	-4.231										
5.0	-9.431	-4.699	.301	-4.431										

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² SUM(L1) JER PHI
 .750+00 .184+01 .545+00 .188+01 1.409 .710 .207+01 1.1669 .588 3.214

N= 2 H*= .250

REDUCED DYNAMIC VISCOSITY AND MODULUS														
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETA2R	GIR	G2R	ETA2R	ETA2R	ARCTAN
-2.8	.149	-2.733	-5.533	-2.651	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.131-02
-2.0	.149	-1.933	-3.933	-1.851	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.828-02
-1.8	.149	-1.733	-3.533	-1.651	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.131-01
-1.4	.148	-1.334	-2.734	-1.252	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.141+01	.330-01
-1.0	.145	-.937	-1.937	-.855	.140+01	.140+01	.140+01	.140+01	.140+01	.140+01	.140+01	.140+01	.140+01	.826-01
-.8	.141	-.742	-1.542	-.659	.138+01	.138+01	.138+01	.138+01	.138+01	.138+01	.138+01	.138+01	.138+01	.130+00
-.6	.129	-.556	-1.156	-.471	.134+01	.134+01	.134+01	.134+01	.134+01	.134+01	.134+01	.134+01	.134+01	.204+00
-.4	.101	-.389	-.789	-.299	.126+01	.126+01	.126+01	.126+01	.126+01	.126+01	.126+01	.126+01	.126+01	.313+00
-.2	.041	-.260	-.460	-.159	.110+01	.110+01	.110+01	.110+01	.110+01	.110+01	.110+01	.110+01	.110+01	.464+00
.0	-.071	-.192	-.192	-.071	.850+00	.850+00	.850+00	.850+00	.850+00	.850+00	.850+00	.850+00	.850+00	.648+00
.2	-.242	-.195	.005	-.042	.573+00	.573+00	.573+00	.573+00	.573+00	.573+00	.573+00	.573+00	.573+00	.839+00
.4	-.474	-.261	.139	-.074	.336+00	.336+00	.336+00	.336+00	.336+00	.336+00	.336+00	.336+00	.336+00	.102+01
.6	-.766	-.378	.222	-.166	.171+00	.171+00	.171+00	.171+00	.171+00	.171+00	.171+00	.171+00	.171+00	.118+01
.8	-1.108	-.534	.266	-.308	.779-01	.779-01	.779-01	.779-01	.779-01	.779-01	.779-01	.779-01	.779-01	.131+01
1.0	-1.482	-.714	.286	-.482	.330-01	.330-01	.330-01	.330-01	.330-01	.330-01	.330-01	.330-01	.330-01	.140+01
1.2	-1.870	-.905	.295	-.670	.135-01	.135-01	.135-01	.135-01	.135-01	.135-01	.135-01	.135-01	.135-01	.146+01
1.4	-2.266	-1.101	.299	-.866	.543-02	.543-02	.543-02	.543-02	.543-02	.543-02	.543-02	.543-02	.543-02	.150+01
1.6	-2.664	-1.300	.300	-1.064	.217-02	.217-02	.217-02	.217-02	.217-02	.217-02	.217-02	.217-02	.217-02	.153+01
1.8	-3.063	-1.499	.301	-1.263	.865-03	.865-03	.865-03	.865-03	.865-03	.865-03	.865-03	.865-03	.865-03	.154+01
2.0	-3.463	-1.699	.301	-1.463	.345-03	.345-03	.345-03	.345-03	.345-03	.345-03	.345-03	.345-03	.345-03	.155+01
2.2	-3.863	-1.899	.301	-1.663	.137-03	.137-03	.137-03	.137-03	.137-03	.137-03	.137-03	.137-03	.137-03	.156+01
2.4	-4.262	-2.099	.301	-1.862	.546-04	.546-04	.546-04	.546-04	.546-04	.546-04	.546-04	.546-04	.546-04	.156+01
2.6	-4.662	-2.299	.301	-2.062	.218-04	.218-04	.218-04	.218-04	.218-04	.218-04	.218-04	.218-04	.218-04	.157+01
2.8	-5.062	-2.499	.301	-2.262	.866-05	.866-05	.866-05	.866-05	.866-05	.866-05	.866-05	.866-05	.866-05	.157+01
3.0	-5.462	-2.699	.301	-2.462	.345-05	.345-05	.345-05	.345-05	.345-05	.345-05	.345-05	.345-05	.345-05	.157+01
3.4	-6.262	-3.099	.301	-2.862	.546-06	.546-06	.546-06	.546-06	.546-06	.546-06	.546-06	.546-06	.546-06	.157+01
3.8	-7.062	-3.499	.301	-3.262	.866-07	.866-07	.866-07	.866-07	.866-07	.866-07	.866-07	.866-07	.866-07	.157+01
4.2	-7.862	-3.899	.301	-3.662	.137-07	.137-07	.137-07	.137-07	.137-07	.137-07	.137-07	.137-07	.137-07	.157+01
4.6	-8.662	-4.299	.301	-4.062	.218-08	.218-08	.218-08	.218-08	.218-08	.218-08	.218-08	.218-08	.218-08	.157+01
5.0	-9.462	-4.699	.301	-4.462	.345-09	.345-09	.345-09	.345-09	.345-09	.345-09	.345-09	.345-09	.345-09	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 JER PHI
 .375+00 .317+01 .315+00 .420+01 1.573 .636 .802+01 1.1262 .455 .762

N= 4 H*= .075

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD			ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	GIR	G2R	ETAR	ETA2/1	
OMTI	FTAIR	ETA2R	GIR	ETAIR	ETA2R	G2R	ETAIR	ETA2R	GIR	G2R	ETAR	ETA2/1		
-2.8	.197	-2.748	-5.548	.157+01	.178-02	-2.603	.157+01	.178-02	.283-05	.249-02	.157+01	.113-02		
-2.0	.197	-1.948	-3.948	.157+01	.113-01	-1.803	.157+01	.113-01	.113-03	.157-01	.157+01	.716-02		
-1.8	.197	-1.748	-3.548	.157+01	.178-01	-1.603	.157+01	.178-01	.283-03	.249-01	.157+01	.113-01		
-1.4	.196	-1.349	-2.749	.157+01	.448-01	-1.204	.157+01	.448-01	.178-02	.626-01	.157+01	.285-01		
-1.0	.194	-.952	-1.952	.156+01	.112+00	-.806	.156+01	.112+00	.112-01	.156+00	.157+01	.713-01		
-.8	.190	-.756	-1.558	.155+01	.175+00	-.610	.155+01	.175+00	.277-01	.245+00	.156+01	.112+00		
-.6	.179	-.572	-1.172	.151+01	.268+00	-.421	.151+01	.268+00	.673-01	.380+00	.154+01	.175+00		
-.4	.156	-.405	-.805	.143+01	.393+00	-.244	.143+01	.393+00	.157+00	.570+00	.148+01	.268+00		
-.2	.106	-.277	-.477	.128+01	.529+00	-.094	.128+01	.529+00	.334+00	.805+00	.138+01	.393+00		
.0	.019	-.209	-.209	.104+01	.619+00	.019	.104+01	.619+00	.619+00	.104+01	.121+01	.535+00		
.2	-.102	-.205	-.005	.098	.791+00	.098	.791+00	.624+00	.988+00	.125+01	.101+01	.667+00		
.4	-.241	-.242	.158	.159	.574+00	.158	.574+00	.572+00	.144+01	.144+01	.810+00	.784+00		
.6	-.404	-.301	.299	.196	.394+00	.299	.394+00	.500+00	.199+01	.157+01	.637+00	.903+00		
.8	-.609	-.383	.417	.191	.246+00	.417	.246+00	.414+00	.261+01	.155+01	.482+00	.104+01		
1.0	-.871	-.496	.504	.129	.135+00	.504	.135+00	.319+00	.319+01	.135+01	.346+00	.117+01		
1.2	-1.190	-.644	.556	.010	.646-01	.556	.646-01	.227+00	.360+01	.102+01	.236+00	.129+01		
1.4	-1.550	-.818	.582	-.150	.282-01	.582	.282-01	.152+00	.382+01	.709+00	.155+00	.139+01		
1.6	-1.932	-1.006	.594	-.332	.117-01	.594	.117-01	.986-01	.393+01	.466+00	.993-01	.145+01		
1.8	-2.324	-1.201	.599	-.524	.474-02	.599	.474-02	.629-01	.397+01	.299+00	.631-01	.150+01		
2.0	-2.721	-1.399	.601	-.721	.190-02	.601	.190-02	.399-01	.399+01	.190+00	.399-01	.152+01		
2.2	-3.120	-1.598	.602	-.920	.759-03	.602	.759-03	.252-01	.400+01	.120+00	.252-01	.154+01		
2.4	-3.520	-1.798	.602	-1.120	.302-03	.602	.302-03	.159-01	.400+01	.759-01	.159-01	.155+01		
2.6	-3.919	-1.998	.602	-1.319	.120-03	.602	.120-03	.100-01	.400+01	.479-01	.100-01	.156+01		
2.8	-4.319	-2.198	.602	-1.519	.479-04	.602	.479-04	.634-02	.400+01	.302-01	.634-02	.156+01		
3.0	-4.719	-2.398	.602	-1.719	.191-04	.602	.191-04	.400-02	.400+01	.191-01	.400-02	.157+01		
3.4	-5.519	-2.798	.602	-2.119	.303-05	.602	.303-05	.159-02	.400+01	.760-02	.159-02	.157+01		
3.8	-6.319	-3.198	.602	-2.519	.479-06	.602	.479-06	.634-03	.400+01	.303-02	.634-03	.157+01		
4.2	-7.119	-3.598	.602	-2.919	.760-07	.602	.760-07	.252-03	.400+01	.120-02	.252-03	.157+01		
4.6	-7.919	-3.998	.602	-3.319	.120-07	.602	.120-07	.100-03	.400+01	.479-03	.100-03	.157+01		
5.0	-8.719	-4.398	.602	-3.719	.191-08	.602	.191-08	.400-04	.400+01	.191-03	.400-04	.157+01		

EXACT ZIMM EIGENVALUES									
LI	LN	1/(LN)	SUM 1/(LP)	SUM LI/LP	RECIP ROCAL	SUM (1/LP) ²	SUM (1/LP) ²	N= 4 H*= .10	PHI
.372+00	.302+01	.331+00	.427+01	1.590	.629	.818+01	1.1332	.448	1.034
REDUCED DYNAMIC VISCOSITY AND MODULUS									
LOG OMTI	LOG ETA2R	LOG G1P	LOG G2P	LOG ETA1R	LOG ETA2R	LOG G1R	LOG G2R	LOG ETA1R	LOG ETA2R
-2.8	.201	-2.746	-5.546	-2.599	.159+01	.190-02	.285-05	.252-02	.159+01
-2.0	.201	-1.946	-3.946	-1.799	.159+01	.113-01	.113-03	.159-01	.159+01
-1.8	.201	-1.746	-3.546	-1.599	.159+01	.190-01	.285-03	.252-01	.159+01
-1.4	.201	-1.346	-2.746	-1.199	.159+01	.451-01	.179-02	.632-01	.159+01
-1.0	.199	-.950	-1.950	-.801	.158+01	.112+00	.112-01	.158+00	.158+01
-.8	.194	-.755	-1.555	-.606	.156+01	.176+00	.276-01	.248+00	.157+01
-.6	.184	-.563	-1.159	-.416	.153+01	.270+00	.677-01	.384+00	.155+01
-.4	.161	-.402	-.802	-.239	.145+01	.396+00	.158+00	.576+00	.150+01
-.2	.111	-.273	-.473	-.089	.129+01	.533+00	.336+00	.815+00	.140+01
.0	.025	-.204	-.204	.025	.105+01	.625+00	.625+00	.106+01	.123+01
.2	-.095	-.199	.001	.105	.804+00	.632+00	.100+01	.127+01	.102+01
.4	-.235	-.235	.165	.165	.582+00	.582+00	.146+01	.146+01	.823+00
.6	-.400	-.293	.307	.200	.398+00	.509+00	.203+01	.158+01	.646+00
.8	-.609	-.375	.425	.191	.246+00	.421+00	.266+01	.155+01	.488+00
1.0	-.876	-.491	.509	.124	.133+00	.323+00	.323+01	.133+01	.349+00
1.2	-1.199	-.641	.559	.001	.632-01	.228+00	.362+01	.100+01	.237+00
1.4	-1.562	-.817	.593	-.162	.274-01	.153+00	.393+01	.689+00	.155+00
1.6	-1.945	-1.066	.594	-.345	.113-01	.997-01	.393+01	.451+00	.994-01
1.8	-2.339	-1.201	.599	-.539	.459-02	.629-01	.397+01	.289+00	.631-01
2.0	-2.736	-1.393	.601	-.736	.134-02	.399-01	.399+01	.184+00	.399-01
2.2	-3.135	-1.598	.602	-.935	.733-03	.252-01	.400+01	.116+00	.252-01
2.4	-3.534	-1.798	.602	-1.134	.292-03	.159-01	.400+01	.734-01	.159-01
2.6	-3.934	-1.998	.602	-1.334	.116-03	.100-01	.400+01	.463-01	.100-01
2.8	-4.334	-2.198	.602	-1.534	.464-04	.634-02	.400+01	.292-01	.634-02
3.0	-4.734	-2.398	.602	-1.734	.185-04	.400-02	.400+01	.185-01	.400-02
3.2	-5.134	-2.593	.602	-2.134	.292-05	.159-02	.400+01	.735-02	.159-02
3.4	-5.534	-2.793	.602	-2.534	.464-06	.634-03	.400+01	.292-02	.634-03
3.6	-5.934	-2.993	.602	-2.934	.735-07	.252-03	.400+01	.116-02	.252-03
3.8	-6.334	-3.193	.602	-3.334	.116-07	.100-03	.400+01	.464-03	.100-03
4.0	-6.734	-3.393	.602	-3.734	.185-08	.400-04	.400+01	.185-03	.400-04
4.2	-7.134	-3.593	.602	-4.134	.252-09	.157-04	.400+01	.735-04	.157-04
4.4	-7.534	-3.793	.602	-4.534	.323-10	.123-05	.400+01	.100-04	.123-05
4.6	-7.934	-3.993	.602	-4.934	.393-11	.997-05	.400+01	.451-05	.994-05
4.8	-8.334	-4.193	.602	-5.334	.464-12	.634-06	.400+01	.634-06	.631-06
5.0	-8.734	-4.393	.602	-5.734	.533-13	.735-07	.400+01	.735-07	.735-07
5.2	-9.134	-4.593	.602	-6.134	.602-14	.815-08	.400+01	.815-08	.815-08
5.4	-9.534	-4.793	.602	-6.534	.677-15	.896-09	.400+01	.896-09	.896-09
5.6	-9.934	-4.993	.602	-6.934	.748-16	.977-10	.400+01	.977-10	.977-10
5.8	-10.334	-5.193	.602	-7.334	.819-17	.106-11	.400+01	.106-11	.106-11
6.0	-10.734	-5.393	.602	-7.734	.890-18	.123-12	.400+01	.123-12	.123-12
6.2	-11.134	-5.593	.602	-8.134	.961-19	.140-13	.400+01	.140-13	.140-13
6.4	-11.534	-5.793	.602	-8.534	.103-20	.157-14	.400+01	.157-14	.157-14
6.6	-11.934	-5.993	.602	-8.934	.174-21	.174-15	.400+01	.174-15	.174-15
6.8	-12.334	-6.193	.602	-9.334	.245-22	.191-16	.400+01	.191-16	.191-16
7.0	-12.734	-6.393	.602	-9.734	.316-23	.208-17	.400+01	.208-17	.208-17
7.2	-13.134	-6.593	.602	-10.134	.387-24	.225-18	.400+01	.225-18	.225-18
7.4	-13.534	-6.793	.602	-10.534	.458-25	.242-19	.400+01	.242-19	.242-19
7.6	-13.934	-6.993	.602	-10.934	.529-26	.259-20	.400+01	.259-20	.259-20
7.8	-14.334	-7.193	.602	-11.334	.600-27	.276-21	.400+01	.276-21	.276-21
8.0	-14.734	-7.393	.602	-11.734	.671-28	.293-22	.400+01	.293-22	.293-22
8.2	-15.134	-7.593	.602	-12.134	.742-29	.310-23	.400+01	.310-23	.310-23
8.4	-15.534	-7.793	.602	-12.534	.813-30	.327-24	.400+01	.327-24	.327-24
8.6	-15.934	-7.993	.602	-12.934	.884-31	.344-25	.400+01	.344-25	.344-25
8.8	-16.334	-8.193	.602	-13.334	.955-32	.361-26	.400+01	.361-26	.361-26
9.0	-16.734	-8.393	.602	-13.734	.102-33	.378-27	.400+01	.102-33	.378-27
9.2	-17.134	-8.593	.602	-14.134	.173-34	.395-28	.400+01	.173-34	.395-28
9.4	-17.534	-8.793	.602	-14.534	.244-35	.412-29	.400+01	.244-35	.412-29
9.6	-17.934	-8.993	.602	-14.934	.315-36	.429-30	.400+01	.315-36	.429-30
9.8	-18.334	-9.193	.602	-15.334	.386-37	.446-31	.400+01	.386-37	.446-31
10.0	-18.734	-9.393	.602	-15.734	.457-38	.463-32	.400+01	.457-38	.463-32
10.2	-19.134	-9.593	.602	-16.134	.528-39	.480-33	.400+01	.528-39	.480-33
10.4	-19.534	-9.793	.602	-16.534	.599-40	.497-34	.400+01	.599-40	.497-34
10.6	-19.934	-9.993	.602	-16.934	.670-41	.514-35	.400+01	.670-41	.514-35
10.8	-20.334	-10.193	.602	-17.334	.741-42	.531-36	.400+01	.741-42	.531-36
11.0	-20.734	-10.393	.602	-17.734	.812-43	.548-37	.400+01	.812-43	.548-37
11.2	-21.134	-10.593	.602	-18.134	.883-44	.565-38	.400+01	.883-44	.565-38
11.4	-21.534	-10.793	.602	-18.534	.954-45	.582-39	.400+01	.954-45	.582-39
11.6	-21.934	-10.993	.602	-18.934	.102-46	.599-40	.400+01	.102-46	.599-40
11.8	-22.334	-11.193	.602	-19.334	.173-47	.616-41	.400+01	.173-47	.616-41
12.0	-22.734	-11.393	.602	-19.734	.244-48	.633-42	.400+01	.244-48	.633-42
12.2	-23.134	-11.593	.602	-20.134	.315-49	.650-43	.400+01	.315-49	.650-43
12.4	-23.534	-11.793	.602	-20.534	.386-50	.667-44	.400+01	.386-50	.667-44
12.6	-23.934	-11.993	.602	-20.934	.457-51	.684-45	.400+01	.457-51	.684-45
12.8	-24.334	-12.193	.602	-21.334	.528-52	.701-46	.400+01	.528-52	.701-46
13.0	-24.734	-12.393	.602	-21.734	.599-53	.718-47	.400+01	.599-53	.718-47
13.2	-25.134	-12.593	.602	-22.134	.670-54	.735-48	.400+01	.670-54	.735-48
13.4	-25.534	-12.793	.602	-22.534	.741-55	.752-49	.400+01	.741-55	.752-49
13.6	-25.934	-12.993	.602	-22.934	.812-56	.769-50	.400+01	.812-56	.769-50
13.8	-26.334	-13.193	.602	-23.334	.883-57	.786-51	.400+01	.883-57	.786-51
14.0	-26.734	-13.393	.602	-23.734	.954-58	.803-52	.400+01	.954-58	.803-52
14.2	-27.134	-13.593	.602	-24.134	.102-59	.820-53	.400+01	.102-59	.820-53
14.4	-27.534	-13.793	.602	-24.534	.173-60	.837-54	.400+01	.173-60	.837-54
14.6	-27.934	-13.993	.602	-24.934	.244-61	.854-55	.400+01	.244-61	.854-55
14.8	-28.334	-14.193	.602	-25.334	.315-62	.871-56	.400+01	.315-62	.871-56
15.0	-28.734	-14.393	.602	-25.734	.386-63	.888-57	.400+01	.386-63	.888-57
15.2	-29.134	-14.593	.602	-26.134	.457-64	.905-58	.400+01	.457-64	.905-58
15.4	-29.534	-14.793	.602	-26.534	.528-65	.922-59	.400+01	.528-65	.922-59
15.6	-29.934	-14.993	.602	-26.934	.599-66	.939-60	.400+01	.599-66	.939-60
15.8	-30.334	-15.193	.602	-27.334	.670-67	.956-61	.400+01	.670-67	.956-61
16.0	-30.734	-15.393	.602	-27.734	.741-68	.973-62	.400+01	.741-68	.973-62
16.2	-31.134	-15.593	.602	-28.134	.812-69	.990-63	.400+01	.812-69	.990-63
16.4	-31.534	-15.793	.602	-28.534	.883-70	.100-64	.400+01	.883-70	.100-64
16.6	-31.934	-15.993	.602	-28.934	.954-71	.117-65	.400+01	.954-71	.117-65
16.8	-32.334	-16.193	.602	-29.334	.102-72	.134-66	.400+01	.102-72	.134-66
17.0	-32.734	-16.393	.602	-29.734	.173-73	.151-67	.400+01	.173-73	.151-67
17.2	-33.134	-16.593	.602	-30.134	.244-74	.168-68	.400+01	.244-74	.168-68
17.4	-33.534	-16.793	.602	-30.534	.315-75	.185-69	.400+01	.315-75	.185-69
17.6	-33.934	-16.993	.602	-30.934	.386-76	.202-70	.400+01	.386-76	.202-70
17.8	-34.334	-17.193	.602	-31.334	.457-77	.219-71	.400+01	.457-77	.219-71
18.0	-34.734	-17.393	.602	-31.734	.528-78	.236-72	.400+01	.528-78	.236-72
18.2	-35.134	-17.593	.602	-32.134	.599-79	.253-73	.400+01	.599-79	.253-73
18.4	-35.534	-17.793	.602	-32.534	.670-80	.270-74	.400+01	.670-80	.270-74
18.6	-35.934	-17.993	.602	-32.934	.741-81	.287-75	.400+01	.741-81	.287-75
18.8	-36.334	-18.193	.602	-33.334	.812-82	.304-76	.400+01	.812-82	.304-76
19.0	-36.734	-18.393	.602	-33.734	.883-83	.321-77	.400+01	.883-83	.321-77
19.2	-37.134	-18.593	.602	-34.134	.954-84	.338-78	.400+01	.954-84	.338-78
19.4	-37.534	-18.793	.602	-34.534	.102-85	.355-79	.400+01	.102-85	.355-79
19.6	-37.934	-18.993	.602	-34.934	.173-86	.372-80	.400+01	.173-86	.372-80
19.8	-38.334	-19.193	.602	-35.					

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 PHI
 .369+00 .284+01 .352+00 .437+01 1.613 .620 .838+01 1.1426 .439 1.374

N= 4 H*= .130

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON		ARCTAN
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R/1
OMTI	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	ETA2R/1	
-2.8	.208	-2.742	-5.542	-2.592	.161+01	.181-02	.287-05	.256-02	.161+01	.161+01	.112-02	
-2.0	.208	-1.942	-3.942	-1.792	.161+01	.114-01	.114-03	.161-01	.161+01	.161+01	.708-02	
-1.8	.208	-1.742	-3.542	-1.592	.161+01	.181-01	.287-03	.256-01	.161+01	.161+01	.112-01	
-1.4	.207	-1.343	-2.743	-1.193	.161+01	.454-01	.181-02	.641-01	.161+01	.161+01	.282-01	
-1.0	.205	-.946	-1.946	-.795	.160+01	.113+00	.113-01	.160+00	.161+01	.161+01	.706-01	
-.8	.201	-.752	-1.552	-.599	.159+01	.177+00	.281-01	.252+00	.160+01	.160+01	.111+00	
-.6	.191	-.566	-1.156	-.409	.155+01	.272+00	.683-01	.390+00	.157+01	.157+01	.174+00	
-.4	.167	-.398	-.798	-.233	.147+01	.400+00	.159+00	.585+00	.152+01	.152+01	.265+00	
-.2	.119	-.269	-.469	-.091	.131+01	.529+00	.340+00	.820+00	.142+01	.142+01	.389+00	
.0	.033	-.199	-.199	.033	.108+01	.673+00	.633+00	.108+01	.125+01	.125+01	.531+00	
.2	-.086	-.191	.079	.114	.820+00	.644+00	.102+01	.130+01	.104+01	.104+01	.665+00	
.4	-.227	-.225	.175	.173	.593+00	.595+00	.150+01	.149+01	.840+00	.840+00	.787+00	
.6	-.395	-.282	.318	.205	.402+00	.522+00	.208+01	.160+01	.659+00	.659+00	.914+00	
.8	-.610	-.366	.434	.190	.245+00	.430+00	.272+01	.155+01	.495+00	.495+00	.105+01	
1.0	-.884	-.485	.515	.116	.131+00	.327+00	.327+01	.131+01	.353+00	.353+00	.119+01	
1.2	-1.212	-.638	.552	-.012	.614-01	.230+00	.365+01	.973+00	.238+00	.238+00	.131+01	
1.4	-1.578	-.815	.585	-.178	.264-01	.153+00	.385+01	.664+00	.155+00	.155+00	.140+01	
1.6	-1.963	-1.005	.595	-.363	.109-01	.989-01	.394+01	.434+00	.995-01	.995-01	.146+01	
1.8	-2.357	-1.201	.599	-.557	.440-02	.630-01	.397+01	.278+00	.631-01	.631-01	.150+01	
2.0	-2.754	-1.399	.601	-.754	.176-02	.399-01	.399+01	.176+00	.399-01	.399-01	.153+01	
2.2	-3.153	-1.598	.602	-.953	.703-03	.252-01	.400+01	.111+00	.252-01	.252-01	.154+01	
2.4	-3.553	-1.798	.602	-1.153	.280-03	.159-01	.400+01	.704-01	.159-01	.159-01	.155+01	
2.6	-3.953	-1.998	.602	-1.353	.112-03	.100-01	.400+01	.444-01	.100-01	.100-01	.156+01	
2.8	-4.352	-2.198	.602	-1.552	.444-04	.634-02	.400+01	.280-01	.634-02	.634-02	.156+01	
3.0	-4.752	-2.398	.602	-1.752	.177-04	.400-02	.400+01	.177-01	.400-02	.400-02	.157+01	
3.4	-5.552	-2.798	.602	-2.152	.280-05	.159-02	.400+01	.704-02	.159-02	.159-02	.157+01	
3.8	-6.352	-3.198	.602	-2.552	.444-06	.634-03	.400+01	.280-02	.634-03	.634-03	.157+01	
4.2	-7.152	-3.598	.602	-2.952	.704-07	.252-03	.400+01	.112-02	.252-03	.252-03	.157+01	
4.6	-7.952	-3.998	.602	-3.352	.112-07	.100-03	.400+01	.444-03	.100-03	.100-03	.157+01	
5.0	-8.752	-4.398	.602	-3.752	.177-08	.400-04	.400+01	.177-03	.400-04	.400-04	.157+01	

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM SUM(L1) JER PHI
 -23
 .367+00 .272+01 .367+00 .444+01 1.629 .614 .853+01 1.1495 .433 1.611

N= 4 H= .150

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2/1	ETA2R	ETA2/1
OMTI	ETA2R	ETA2R	GIR	G2R	ETA2R	ETA2R	ETA2R	GIR	G2R	ETA2R	ETA2/1	ETA2R	ETA2/1
-2.8	.212	-2.739	-5.539	-2.588	.163+01	.182-02	.182-02	.289-05	.258-02	.163+01	.112-02	.163+01	.112-02
-2.0	.212	-1.940	-3.340	-1.788	.163+01	.115-01	.115-01	.115-03	.163-01	.163+01	.706-02	.163+01	.706-02
-1.8	.212	-1.740	-3.540	-1.588	.163+01	.182-01	.182-01	.289-03	.258-01	.163+01	.112-01	.163+01	.112-01
-1.4	.212	-1.340	-2.740	-1.188	.163+01	.457-01	.457-01	.182-02	.648-01	.163+01	.291-01	.163+01	.291-01
-1.0	.209	-.543	-1.943	-.791	.162+01	.114+00	.114+00	.114-01	.162+00	.162+01	.703-01	.162+01	.703-01
-.8	.205	-.749	-1.549	-.595	.160+01	.178+00	.178+00	.283-01	.254+00	.161+01	.111+00	.161+01	.111+00
-.6	.195	-.563	-1.163	-.405	.157+01	.24+00	.24+00	.687-01	.394+00	.159+01	.173+00	.159+01	.173+00
-.4	.172	-.395	-.795	-.228	.149+01	.402+00	.402+00	.160+00	.592+00	.154+01	.264+00	.154+01	.264+00
-.2	.124	-.265	-.465	-.076	.133+01	.543+00	.543+00	.343+00	.839+00	.144+01	.338+00	.144+01	.338+00
.0	.039	-.154	-.194	.039	.109+01	.639+00	.639+00	.639+00	.109+01	.127+01	.529+00	.127+01	.529+00
.2	-.080	-.186	.014	.120	.832+00	.652+00	.652+00	.103+01	.132+01	.106+01	.665+00	.106+01	.665+00
.4	-.221	-.218	.182	.179	.601+00	.605+00	.605+00	.152+01	.151+01	.853+00	.789+00	.853+00	.789+00
.6	-.392	-.275	.325	.208	.405+00	.531+00	.531+00	.211+01	.161+01	.668+00	.919+00	.668+00	.919+00
.8	-.611	-.360	.440	.189	.245+00	.437+00	.437+00	.275+01	.155+01	.501+00	.106+01	.501+00	.106+01
1.0	-.889	-.481	.519	.111	.129+00	.331+00	.331+00	.331+01	.129+01	.355+00	.120+01	.355+00	.120+01
1.2	-1.221	-.636	.554	-.021	.601-01	.731+00	.731+00	.367+01	.952+00	.23+00	.132+01	.23+00	.132+01
1.4	-1.589	-.814	.586	-.189	.258-01	.153+00	.153+00	.386+01	.647+00	.156+00	.140+01	.156+00	.140+01
1.6	-1.975	-1.004	.596	-.375	.106-01	.940-01	.940-01	.394+01	.422+00	.995-01	.146+01	.995-01	.146+01
1.8	-2.369	-1.201	.593	-.569	.427-02	.630-01	.630-01	.398+01	.270+00	.632-01	.150+01	.632-01	.150+01
2.0	-2.757	-1.399	.601	-.767	.171-02	.399-01	.399-01	.399+01	.171+00	.399-01	.153+01	.399-01	.153+01
2.2	-3.166	-1.598	.602	-.966	.682-03	.252-01	.252-01	.400+01	.108+00	.252-01	.154+01	.252-01	.154+01
2.4	-3.566	-1.798	.602	-1.166	.272-03	.159-01	.159-01	.400+01	.683-01	.159-01	.155+01	.683-01	.155+01
2.6	-3.965	-1.998	.602	-1.365	.108-03	.100-01	.100-01	.400+01	.431-01	.100-01	.156+01	.431-01	.156+01
2.8	-4.365	-2.198	.602	-1.565	.431-04	.634-02	.634-02	.400+01	.272-01	.634-02	.156+01	.272-01	.156+01
3.0	-4.765	-2.398	.602	-1.765	.172-04	.400-02	.400-02	.400+01	.172-01	.400-02	.157+01	.400-02	.157+01
3.4	-5.565	-2.798	.602	-2.165	.272-05	.159-02	.159-02	.400+01	.693-02	.159-02	.157+01	.693-02	.157+01
3.6	-6.365	-3.193	.602	-2.565	.431-06	.634-03	.634-03	.400+01	.272-02	.634-03	.157+01	.272-02	.157+01
4.2	-7.165	-3.598	.602	-2.965	.683-07	.252-03	.252-03	.400+01	.108-02	.252-03	.157+01	.108-02	.157+01
4.6	-7.965	-3.998	.602	-3.365	.108-07	.100-03	.100-03	.400+01	.431-03	.100-03	.157+01	.431-03	.157+01
5.0	-8.765	-4.398	.602	-3.765	.172-08	.400-04	.400-04	.400+01	.172-03	.400-04	.157+01	.172-03	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM SUM(L1 JER PHI
 .362+00 .242+01 .413+00 .463+01 1.675 .597 .832+01 1.169S .417 2.240
 -23

N= 4 H*= .20

REDUCED DYNAMIC VISCOSITY AND MODULUS									
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA1R
ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1
-2.8	.224	-2.732	-5.532	-2.576	.168+01	.185-02	.294-05	.266-02	.168+01
-2.0	.224	-1.932	-3.932	-1.776	.158+01	.117-01	.117-03	.168-01	.168+01
-1.8	.224	-1.732	-3.532	-1.576	.163+01	.185-01	.294-03	.265-01	.168+01
-1.4	.224	-1.332	-2.732	-1.176	.157+01	.465-01	.185-02	.666-01	.167+01
-1.0	.221	-.936	-1.936	-.773	.156+01	.116+00	.116-01	.166+00	.167+01
-.8	.217	-.741	-1.541	-.583	.155+01	.191+00	.288-01	.261+00	.156+01
-.6	.208	-.555	-1.155	-.392	.161+01	.279+00	.700-01	.405+00	.164+01
-.4	.185	-.387	-.787	-.215	.153+01	.410+00	.163+00	.610+00	.159+01
-.2	.138	-.256	-.456	-.062	.137+01	.555+00	.350+00	.856+00	.148+01
.0	.054	-.182	-.182	.054	.113+01	.657+00	.657+00	.117+01	.131+01
.2	-.064	-.170	.030	.136	.864+00	.676+00	.107+01	.137+01	.110+01
.4	-.207	-.199	.201	.193	.621+00	.632+00	.159+01	.156+01	.895+00
.6	-.395	-.255	.345	.215	.412+00	.556+00	.221+01	.154+01	.692+00
.8	-.615	-.343	.457	.185	.243+00	.454+00	.296+01	.153+01	.514+00
1.0	-.905	-.470	.530	.095	.124+00	.339+00	.339+01	.124+01	.361+00
1.2	-1.247	-.630	.570	-.047	.567-01	.234+00	.371+01	.898+00	.241+00
1.4	-1.620	-.811	.599	-.220	.240-01	.154+00	.338+01	.603+00	.156+00
1.6	-2.006	-1.003	.597	-.408	.992-02	.992-01	.395+01	.391+00	.997-01
1.8	-2.403	-1.200	.600	-.603	.395-02	.631-01	.398+01	.249+00	.632-01
2.0	-2.801	-1.399	.601	-.801	.158-02	.399-01	.399+01	.158+00	.400-01
2.2	-3.201	-1.598	.602	-1.001	.630-03	.252-01	.400+01	.999-01	.252-01
2.4	-3.600	-1.798	.602	-1.200	.251-03	.159-01	.400+01	.630-01	.159-01
2.6	-4.000	-1.993	.602	-1.400	.100-03	.100-01	.400+01	.398-01	.100-01
2.8	-4.400	-2.198	.602	-1.600	.398-04	.634-02	.400+01	.251-01	.634-02
3.0	-4.800	-2.396	.602	-1.800	.158-04	.400-02	.400+01	.158-01	.400-02
3.4	-5.600	-2.798	.602	-2.200	.251-05	.159-02	.400+01	.631-02	.159-02
3.8	-6.400	-3.196	.602	-2.600	.398-06	.634-03	.400+01	.251-02	.634-03
4.2	-7.200	-3.598	.602	-3.000	.631-07	.252-03	.400+01	.100-02	.252-03
4.6	-8.000	-3.998	.602	-3.400	.100-07	.100-03	.400+01	.398-03	.100-03
5.0	-8.800	-4.398	.602	-3.800	.158-08	.400-04	.400+01	.158-03	.400-04

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM LI/LP RECIP SUM (1/LP)² SUM(LI) JER PHI
 .357+00 .213+01 .471+00 .485+01 1.731 .578 .939+01 1.1959 .399 2.935

N= 4 H= .250

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON				ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	G2R	G2R	ETA2R	ETA2R/1
OMTI	ETA2R	ETA2R	G1P	G2P	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	G2R	G2R	ETA2R	ETA2R/1
-2.8	.238	-2.722	-5.522	-2.562	.173+01	.190-02	.190-02	.190-02	.190-02	.190-02	.190-02	.274-02	.274-02	.173+01	.109-02
-2.0	.238	-1.922	-3.922	-1.762	.173+01	.120-01	.120-01	.120-01	.120-01	.120-01	.120-01	.173-01	.173-01	.173+01	.691-02
-1.8	.238	-1.722	-3.522	-1.562	.173+01	.190-01	.190-01	.190-01	.190-01	.190-01	.190-01	.274-01	.274-01	.173+01	.109-01
-1.4	.238	-1.323	-2.723	-1.162	.173+01	.475-01	.475-01	.475-01	.475-01	.475-01	.475-01	.689-01	.689-01	.173+01	.275-01
-1.0	.236	-.926	-1.926	-.764	.172+01	.119+00	.119+00	.119+00	.119+00	.119+00	.119+00	.172+00	.172+00	.172+01	.686-01
-.8	.232	-.731	-1.531	-.568	.171+01	.196+00	.196+00	.196+00	.196+00	.196+00	.196+00	.270+00	.270+00	.172+01	.106+00
-.6	.222	-.545	-1.145	-.378	.167+01	.285+00	.285+00	.285+00	.285+00	.285+00	.285+00	.419+00	.419+00	.169+01	.169+00
-.4	.200	-.376	-.776	-.200	.159+01	.421+00	.421+00	.421+00	.421+00	.421+00	.421+00	.631+00	.631+00	.164+01	.259+00
-.2	.154	-.244	-.444	-.045	.142+01	.571+00	.571+00	.571+00	.571+00	.571+00	.571+00	.899+00	.899+00	.153+01	.391+00
.0	.072	-.163	-.168	.072	.118+01	.680+00	.680+00	.680+00	.680+00	.680+00	.680+00	.118+01	.118+01	.136+01	.523+00
.2	-.045	-.151	.049	.155	.901+00	.706+00	.706+00	.706+00	.706+00	.706+00	.706+00	.143+01	.143+01	.114+01	.665+00
.4	-.192	-.176	.224	.208	.643+00	.656+00	.656+00	.656+00	.656+00	.656+00	.656+00	.167+01	.167+01	.926+00	.803+00
.6	-.378	-.233	.367	.222	.418+00	.595+00	.595+00	.595+00	.595+00	.595+00	.595+00	.233+01	.233+01	.719+00	.950+00
.8	-.621	-.326	.474	.179	.239+00	.472+00	.472+00	.472+00	.472+00	.472+00	.472+00	.298+01	.298+01	.529+00	.110+01
1.0	-.926	-.459	.541	.074	.119+00	.347+00	.347+00	.347+00	.347+00	.347+00	.347+00	.347+01	.347+01	.367+00	.124+01
1.2	-1.277	-.625	.575	-.077	.579-01	.237+00	.237+00	.237+00	.237+00	.237+00	.237+00	.838+00	.838+00	.243+00	.135+01
1.4	-1.655	-.809	.591	-.255	.222-01	.155+00	.155+00	.155+00	.155+00	.155+00	.155+00	.390+01	.390+01	.157+00	.143+01
1.6	-2.045	-1.002	.598	-.445	.901-02	.994-01	.994-01	.994-01	.994-01	.994-01	.994-01	.396+01	.396+01	.998-01	.148+01
1.8	-2.441	-1.200	.600	-.641	.362-02	.631-01	.631-01	.631-01	.631-01	.631-01	.631-01	.398+01	.398+01	.632-01	.151+01
2.0	-2.840	-1.393	.601	-.840	.145-02	.399-01	.399-01	.399-01	.399-01	.399-01	.399-01	.400+01	.400+01	.400-01	.153+01
2.2	-3.239	-1.598	.602	-1.039	.576-03	.252-01	.252-01	.252-01	.252-01	.252-01	.252-01	.913-01	.913-01	.252-01	.155+01
2.4	-3.639	-1.798	.602	-1.239	.230-03	.159-01	.159-01	.159-01	.159-01	.159-01	.159-01	.577-01	.577-01	.159-01	.156+01
2.6	-4.039	-1.998	.602	-1.439	.914-04	.100-01	.100-01	.100-01	.100-01	.100-01	.100-01	.364-01	.364-01	.100-01	.158+01
2.8	-4.439	-2.198	.602	-1.639	.364-04	.634-02	.634-02	.634-02	.634-02	.634-02	.634-02	.230-01	.230-01	.634-02	.157+01
3.0	-4.839	-2.398	.602	-1.839	.145-04	.400-02	.400-02	.400-02	.400-02	.400-02	.400-02	.145-01	.145-01	.400-02	.157+01
3.4	-5.639	-2.798	.602	-2.239	.230-05	.159-02	.159-02	.159-02	.159-02	.159-02	.159-02	.577-02	.577-02	.159-02	.157+01
3.8	-6.439	-3.198	.602	-2.639	.364-06	.634-03	.634-03	.634-03	.634-03	.634-03	.634-03	.230-02	.230-02	.634-03	.157+01
4.2	-7.239	-3.598	.602	-3.039	.577-07	.252-03	.252-03	.252-03	.252-03	.252-03	.252-03	.914-03	.914-03	.252-03	.157+01
4.6	-8.039	-3.998	.602	-3.439	.914-08	.100-03	.100-03	.100-03	.100-03	.100-03	.100-03	.364-03	.364-03	.100-03	.157+01
5.0	-8.839	-4.398	.602	-3.839	.145-08	.400-04	.400-04	.400-04	.400-04	.400-04	.400-04	.145-03	.145-03	.400-04	.157+01

EXACT ZIMM EIGENVALUES	N = 9 H* = .075				PHI	
LI	LN	1/(LN)	SUM	RECIP		
			1/(LP)	ROCAL		
-129+00	.339+01	.295+00	.131+02	1.690	1.1129	.390
				.592	.667+02	.840
					(1/LP)2	
					SUM(LI	JFR
						-23
						.840

1

EXACT ZIMM EIGENVALUES

LI	LN	1/(LN)	SUM 1/(LP)	SUM LI/LP	RECIP QOCAL	SUM (1/LP) ²	SUM(LI /LP) ²	JER	H= .10	PHI
.132+00	.322+01	.310+00	.130+02	1.720	.581	.644+02	1.1205	.379	1.116	

REDUCED DYNAMIC VISCOSITY AND MODULUS

LOG OMTI	LOG ETA1R	LOG ETA2R	LOG GIR	LOG G2P	LOG ETA1R	LOG ETA2R	LOG GIR	LOG G2R	LOG ETAR	LOG MCD	LOG ARCTAN ETA2/1
-2.8	.236	-2.751	-5.551	-2.564	.172+01	.178-02	.281-05	.273-02	.172+01	.172+01	.103-02
-2.0	.236	-1.951	-3.951	-1.764	.172+01	.172-01	.112-03	.172-01	.172+01	.172+01	.651-02
-1.8	.236	-1.751	-3.551	-1.564	.172+01	.178-01	.281-03	.273-01	.172+01	.172+01	.103-01
-1.4	.235	-1.351	-2.751	-1.165	.172+01	.445-01	.177-02	.684-01	.172+01	.172+01	.259-01
-1.0	.233	-.954	-1.954	-.767	.171+01	.111+00	.111-01	.171+00	.171+01	.171+01	.648-01
-.8	.229	-.760	-1.550	-.571	.170+01	.174+00	.275-01	.269+00	.170+01	.170+01	.102+00
-.6	.220	-.574	-1.174	-.380	.156+01	.266+00	.669-01	.417+00	.168+01	.168+01	.159+00
-.4	.198	-.408	-.808	-.202	.158+01	.391+00	.156+00	.629+00	.163+01	.163+01	.243+00
-.2	.154	-.279	-.479	-.046	.143+01	.526+00	.332+00	.899+00	.152+01	.152+01	.353+00
.0	.077	-.212	-.212	.077	.119+01	.614+00	.614+00	.119+01	.134+01	.134+01	.475+00
.2	-.024	-.209	-.009	.176	.947+00	.618+00	.980+00	.150+01	.113+01	.113+01	.579+00
.4	-.133	-.244	.156	.267	.736+00	.570+00	.143+01	.145+01	.931+00	.931+00	.658+00
.6	-.248	-.294	.306	.352	.565+00	.508+00	.202+01	.225+01	.760+00	.760+00	.732+00
.8	-.376	-.352	.448	.424	.421+00	.445+00	.291+01	.256+01	.612+00	.612+00	.613+00
1.0	-.528	-.418	.532	.472	.297+00	.382+00	.392+01	.297+01	.497+00	.497+00	.910+00
1.2	-.718	-.501	.599	.482	.191+00	.316+00	.500+01	.303+01	.350+00	.350+00	.107+01
1.4	-.964	-.610	.790	.436	.109+00	.246+00	.617+01	.273+01	.259+00	.259+00	.115+01
1.6	-1.269	-.751	.849	.331	.539-01	.177+00	.706+01	.214+01	.185+00	.185+00	.128+01
1.8	-1.620	-.921	.879	.180	.240-01	.120+00	.757+01	.151+01	.122+00	.122+00	.137+01
2.0	-1.998	-1.107	.893	.002	.100-01	.792-01	.782+01	.100+01	.782-01	.782-01	.144+01
2.2	-2.389	-1.301	.899	-.189	.409-02	.500-01	.793+01	.647+00	.502-01	.502-01	.145+01
2.4	-2.785	-1.499	.901	-.385	.164-02	.317-01	.797+01	.412+00	.318-01	.318-01	.152+01
2.6	-3.183	-1.698	.902	-.583	.655-03	.201-01	.799+01	.261+00	.201-01	.201-01	.154+01
2.8	-3.593	-1.897	.903	-.783	.261-03	.127-01	.800+01	.165+00	.127-01	.127-01	.155+01
3.0	-3.983	-2.097	.903	-.983	.104-03	.800-02	.800+01	.104+00	.800-02	.800-02	.156+01
3.4	-4.783	-2.497	.903	-1.383	.155-04	.318-02	.800+01	.414-01	.318-02	.318-02	.157+01
3.8	-5.582	-2.897	.903	-1.782	.252-05	.127-02	.800+01	.165-01	.127-02	.127-02	.157+01
4.2	-6.382	-3.297	.903	-2.182	.414-06	.505-03	.800+01	.657-02	.505-03	.505-03	.157+01
4.6	-7.182	-3.697	.903	-2.582	.657-07	.201-03	.800+01	.262-02	.201-03	.201-03	.157+01
5.0	-7.982	-4.097	.903	-2.982	.104-07	.800-04	.800+01	.104-02	.800-04	.800-04	.157+01

EXACT ZIMM EIGENVALUES						N = 8 H ₂ O = .130							
L1	LN	I/(LN)	SUM I/(LP)	SUM LI/LP	RECIP ROCAL	SUM (I/LP) ²	SUM(LI /LP) ²	JER	PFI	-23	1.446		
.135+00	.303+01	.330+00	.130+02	1.759	.569	-.618+02	1.1304	.365	1.446				

-41-

EXACT ZIMP EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² SUM(L1 JER PHI
 .137+00 .290+01 .345+00 .130+02 1.786 .560 .602+02 1.1375 .357 1.668

N= 8 H=.150

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA	G2R	ETA	ETA2/1
OMT	ETA	ETA2R	GIR	ETA	ETA2R	G2R	GIR	ETA	ETA2R	ETA	G2R	ETA	ETA2/1
-2.6	.252	-2.744	-5.544	-2.548	.179+01	.180-02	.286-05	.283-02	.179+01	.179+01	.283-02	.179+01	.101-02
-2.0	.252	-1.944	-3.944	-1.748	.179+01	.114-01	.114-03	.179-01	.179+01	.179+01	.179-01	.179+01	.637-02
-1.8	.252	-1.744	-3.544	-1.548	.179+01	.190-01	.286-03	.283-01	.179+01	.179+01	.283-01	.179+01	.101-01
-1.4	.252	-1.345	-2.745	-1.148	.178+01	.452-01	.180-02	.710-01	.179+01	.179+01	.710-01	.179+01	.253-01
-1.0	.249	-.948	-1.948	-.751	.178+01	.113+00	.113-01	.178+00	.178+01	.178+01	.178+00	.178+01	.634-01
-.8	.246	-.754	-1.554	-.554	.176+01	.176+00	.280-01	.279+00	.177+01	.177+01	.279+00	.177+01	.998-01
-.6	.237	-.568	-1.158	-.363	.172+01	.271+00	.680-01	.433+00	.175+01	.175+01	.433+00	.175+01	.156+00
-.4	.216	-.400	-.800	-.184	.164+01	.398+00	.158+00	.655+00	.169+01	.169+01	.655+00	.169+01	.237+00
-.2	.173	-.271	-.471	-.027	.149+01	.536+00	.338+00	.939+00	.158+01	.158+01	.939+00	.158+01	.346+00
.0	.099	-.201	-.201	.099	.126+01	.629+00	.629+00	.126+01	.140+01	.140+01	.126+01	.140+01	.465+00
.2	.001	-.194	.006	.201	.100+01	.640+00	.101+01	.159+01	.119+01	.119+01	.159+01	.119+01	.568+00
.4	-.106	-.224	.176	.294	.783+00	.597+00	.150+01	.197+01	.985+00	.985+00	.197+01	.985+00	.652+00
.6	-.221	-.268	.332	.379	.601+00	.539+00	.215+01	.239+01	.807+00	.807+00	.239+01	.807+00	.731+00
.8	-.353	-.322	.478	.447	.444+00	.477+00	.301+01	.280+01	.651+00	.651+00	.280+01	.651+00	.821+00
1.0	-.513	-.387	.613	.487	.307+00	.410+00	.410+01	.307+01	.512+00	.512+00	.307+01	.512+00	.929+00
1.2	-.719	-.473	.727	.481	.191+00	.337+00	.533+01	.303+01	.387+00	.387+00	.303+01	.387+00	.105+01
1.4	-.983	-.590	.810	.417	.104+00	.257+00	.646+01	.261+01	.277+00	.277+00	.261+01	.277+00	.119+01
1.6	-1.305	-.740	.860	.295	.496-01	.182+00	.724+01	.197+01	.189+00	.189+00	.197+01	.189+00	.130+01
1.8	-1.666	-.916	.884	.134	.216-01	.121+00	.766+01	.136+01	.123+00	.123+00	.136+01	.123+00	.140+01
2.0	-2.049	-1.105	.895	-.049	.893-02	.786-01	.796+01	.893+00	.791-01	.791-01	.893+00	.791-01	.146+01
2.2	-2.442	-1.300	.900	-.242	.361-02	.501-01	.794+01	.572+00	.502-01	.502-01	.572+00	.502-01	.150+01
2.4	-2.840	-1.498	.902	-.440	.145-02	.318-01	.798+01	.363+00	.318-01	.318-01	.363+00	.318-01	.153+01
2.6	-3.238	-1.697	.903	-.638	.578-03	.201-01	.799+01	.230+00	.201-01	.201-01	.230+00	.201-01	.154+01
2.8	-3.638	-1.897	.903	-.838	.230-03	.127-01	.800+01	.145+00	.127-01	.127-01	.145+00	.127-01	.155+01
3.0	-4.038	-2.097	.903	-1.038	.917-04	.800-02	.800+01	.917-01	.800-02	.800-02	.917-01	.800-02	.156+01
3.4	-4.838	-2.497	.903	-1.438	.145-04	.316-02	.800+01	.365+01	.318-02	.318-02	.365+01	.318-02	.157+01
3.6	-5.638	-2.897	.903	-1.838	.230-05	.127-02	.800+01	.145-01	.127-02	.127-02	.145-01	.127-02	.157+01
4.2	-6.438	-3.297	.903	-2.238	.365-05	.505-03	.800+01	.579+02	.505-03	.505-03	.579+02	.505-03	.157+01
4.6	-7.238	-3.697	.903	-2.638	.579-07	.201-03	.800+01	.230+02	.201-03	.201-03	.230+02	.201-03	.157+01
5.0	-8.038	-4.097	.903	-3.038	.917-08	.800-04	.800+01	.917+03	.800-04	.800-04	.917+03	.800-04	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² /LP² SUM(L1) JER PHI
 -23
 .143+00 .257+01 .390+00 .130+02 1.860 .538 .567+02 1.1572 .334 2.228

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2I	ETA2R/1	ETA2I/1
OMTI	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	G2R	ETA2R	ETA2R/1	ETA2I/1
-2.8	.270	-2.737	-5.537	.186+01	.183-02	.291-05	.186+01	.183-02	.291-05	.295-07	.186+01	.986-03	.986-03
-2.0	.270	-1.937	-3.937	.196+01	.116-01	.116-03	.196+01	.116-01	.116-03	.186-01	.186+01	.622-02	.622-02
-1.8	.270	-1.737	-3.537	.186+01	.183-01	.291-03	.186+01	.183-01	.291-03	.295-01	.186+01	.986-02	.986-02
-1.4	.259	-1.337	-2.737	.186+01	.460-01	.183-02	.186+01	.460-01	.183-02	.740-01	.186+01	.247-01	.247-01
-1.0	.267	-.940	-1.940	.185+01	.115+00	.115-01	.185+01	.115+00	.115-01	.185+00	.185+01	.619-01	.619-01
-.8	.264	-.746	-1.546	.183+01	.179+00	.284-01	.183+01	.179+00	.284-01	.291+00	.184+01	.975-01	.975-01
-.6	.255	-.560	-1.150	.190+01	.276+00	.692-01	.190+01	.276+00	.692-01	.452+00	.182+01	.152+00	.152+00
-.4	.235	-.392	-.792	.172+01	.406+00	.161+00	.172+01	.406+00	.161+00	.694+00	.176+01	.232+00	.232+00
-.2	.193	-.261	-.461	.156+01	.548+00	.348+00	.156+01	.548+00	.348+00	.935+00	.165+01	.338+00	.338+00
.0	.122	-.189	-.199	.133+01	.647+00	.647+00	.133+01	.647+00	.647+00	.137+01	.147+01	.454+00	.454+00
.2	.028	-.177	.023	.107+01	.656+00	.106+01	.107+01	.656+00	.106+01	.169+01	.126+01	.558+00	.558+00
.4	-.078	-.201	.199	.836+00	.630+00	.158+01	.836+00	.630+00	.158+01	.210+01	.105+01	.646+00	.646+00
.6	-.194	-.240	.350	.640+00	.576+00	.229+01	.640+00	.576+00	.229+01	.255+01	.861+00	.733+00	.733+00
.8	-.330	-.289	.511	.467+00	.514+00	.324+01	.467+00	.514+00	.324+01	.295+01	.694+00	.833+00	.833+00
1.0	-.502	-.354	.646	.315+00	.442+00	.442+01	.315+00	.442+00	.442+01	.315+01	.543+00	.952+00	.952+00
1.2	-.724	-.446	.754	.189+00	.358+00	.568+01	.189+00	.358+00	.568+01	.299+01	.405+00	.109+01	.109+01
1.4	-1.009	-.572	.828	.980-01	.268+00	.674+01	.980-01	.268+00	.674+01	.246+01	.285+00	.122+01	.122+01
1.6	-1.346	-.731	.859	.451-01	.186+00	.740+01	.451-01	.186+00	.740+01	.180+01	.191+00	.133+01	.133+01
1.8	-1.717	-.911	.899	.192-01	.123+00	.774+01	.192-01	.123+00	.774+01	.121+01	.124+00	.142+01	.142+01
2.0	-2.104	-1.103	.897	.797-02	.799-01	.799+01	.797-02	.799-01	.799+01	.787+00	.797-01	.147+01	.147+01
2.2	-2.499	-1.299	.901	.317-02	.502-01	.796+01	.317-02	.502-01	.796+01	.503+00	.503-01	.151+01	.151+01
2.4	-2.897	-1.498	.902	.127-01	.318-01	.798+01	.127-01	.318-01	.798+01	.319+00	.318-01	.153+01	.153+01
2.6	-3.296	-1.697	.903	.506-03	.201-01	.799+01	.506-03	.201-01	.799+01	.201+00	.201-01	.155+01	.155+01
2.8	-3.696	-1.897	.903	.202-03	.127-01	.800+01	.202-03	.127-01	.800+01	.127+00	.127-01	.155+01	.155+01
3.0	-4.095	-2.097	.903	.803-04	.800-02	.800+01	.803-04	.800-02	.800+01	.803-01	.800-02	.156+01	.156+01
3.4	-4.695	-2.497	.903	.127-04	.318-02	.800+01	.127-04	.318-02	.800+01	.320-01	.318-02	.157+01	.157+01
3.8	-5.695	-2.897	.903	.202-05	.127-02	.800+01	.202-05	.127-02	.800+01	.127-01	.127-02	.157+01	.157+01
4.2	-6.495	-3.297	.903	.320-06	.505-03	.800+01	.320-06	.505-03	.800+01	.507-02	.505-03	.157+01	.157+01
4.6	-7.295	-3.697	.903	.507-07	.201-03	.800+01	.507-07	.201-03	.800+01	.202-02	.201-03	.157+01	.157+01
5.0	-8.095	-4.097	.903	.803-08	.800-04	.800+01	.803-08	.800-04	.800+01	.803-03	.800-04	.157+01	.157+01

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² /LP² PHI
 -1.48+00 .224+01 .447+00 .131+02 1.946 .514 .538+02 1.1807 .312 2.810

N= R H= .250

REDUCED DYNAMIC VISCOSITY AND MODULUS										MCP			ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	FTAIR	ETA2R	G1D	G2R	ETAIR	ETA2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	ETA2R	ETA2R
-2.8	.289	-2.728	-5.528	-2.511	.195+01	.187-02	.195+01	.187-02	.297-05	.309-02	.195+01	.195+01	.195+01	.962-03
-2.0	.289	-1.928	-3.928	-1.711	.195+01	.118-01	.195+01	.118-01	.113-03	.195-01	.195+01	.195+01	.195+01	.607-02
-1.8	.289	-1.728	-3.528	-1.511	.195+01	.187-01	.195+01	.187-01	.297-03	.309-01	.195+01	.195+01	.195+01	.961-02
-1.4	.289	-1.328	-2.728	-1.111	.194+01	.469-01	.194+01	.469-01	.187-02	.774-01	.195+01	.195+01	.195+01	.241-01
-1.0	.287	-.932	-1.932	-.713	.194+01	.117+00	.194+01	.117+00	.117-01	.194+00	.194+01	.194+01	.194+01	.604-01
-.8	.283	-.737	-1.537	-.517	.192+01	.183+00	.192+01	.183+00	.290-01	.304+00	.193+01	.193+01	.193+01	.951-01
-.6	.275	-.551	-1.151	-.325	.188+01	.291+00	.188+01	.291+00	.707-01	.473+00	.190+01	.190+01	.190+01	.148+00
-.4	.256	-.382	-.782	-.144	.180+01	.415+00	.180+01	.415+00	.165+00	.718+00	.185+01	.185+01	.185+01	.226+00
-.2	.216	-.250	-.450	.016	.164+01	.562+00	.164+01	.562+00	.355+00	.104+01	.174+01	.174+01	.174+01	.329+00
.0	.148	-.175	-.175	.148	.140+01	.669+00	.140+01	.669+00	.669+00	.140+01	.156+01	.156+01	.156+01	.444+00
.2	.056	-.157	.043	.256	.114+01	.696+00	.114+01	.696+00	.110+01	.180+01	.133+01	.133+01	.133+01	.549+00
.4	-.048	-.175	.225	.352	.896+00	.658+00	.896+00	.658+00	.168+01	.225+01	.112+01	.112+01	.112+01	.641+00
.6	-.165	-.208	.392	.435	.683+00	.620+00	.683+00	.620+00	.247+01	.272+01	.923+00	.923+00	.923+00	.737+00
.8	-.309	-.254	.546	.491	.491+00	.558+00	.491+00	.558+00	.352+01	.310+01	.743+00	.743+00	.743+00	.849+00
1.0	-.494	-.320	.680	.506	.321+00	.479+00	.321+00	.479+00	.479+01	.321+01	.576+00	.576+00	.576+00	.980+00
1.2	-.737	-.419	.781	.463	.183+00	.381+00	.183+00	.381+00	.604+01	.290+01	.423+00	.423+00	.423+00	.112+01
1.4	-1.042	-.555	.845	.358	.908-01	.278+00	.908-01	.278+00	.699+01	.228+01	.293+00	.293+00	.293+00	.126+01
1.6	-1.393	-.722	.878	.207	.404-01	.124+00	.404-01	.124+00	.754+01	.161+01	.194+00	.194+00	.194+00	.136+01
1.8	-1.772	-.907	.893	.028	.169-01	.124+00	.169-01	.124+00	.781+01	.107+01	.125+00	.125+00	.125+00	.143+01
2.0	-2.162	-1.101	.899	-.142	.688-02	.792-01	.688-02	.792-01	.792+01	.698+00	.795-01	.795-01	.795-01	.148+01
2.2	-2.559	-1.299	.901	-.359	.276-02	.503-01	.276-02	.503-01	.797+01	.438+00	.504-01	.504-01	.504-01	.152+01
2.4	-2.957	-1.498	.902	-.557	.110-02	.318-01	.110-02	.318-01	.799+01	.277+00	.318-01	.318-01	.318-01	.154+01
2.6	-3.357	-1.697	.903	-.757	.440-03	.201-01	.440-03	.201-01	.799+01	.175+00	.201-01	.201-01	.201-01	.155+01
2.8	-3.756	-1.897	.903	-.956	.175-03	.127-01	.175-03	.127-01	.800+01	.111+00	.127-01	.127-01	.127-01	.156+01
3.0	-4.156	-2.097	.903	-1.156	.698-04	.800-02	.698-04	.800-02	.800+01	.698-01	.800-02	.800-02	.800-02	.156+01
3.4	-4.956	-2.497	.903	-1.556	.111-04	.318-02	.111-04	.318-02	.800+01	.278-01	.318-02	.318-02	.318-02	.157+01
3.8	-5.756	-2.897	.903	-1.956	.175-05	.127-02	.175-05	.127-02	.800+01	.111-01	.127-02	.127-02	.127-02	.157+01
4.2	-6.556	-3.297	.903	-2.356	.278-06	.505-03	.278-06	.505-03	.800+01	.440-02	.505-03	.505-03	.505-03	.157+01
4.6	-7.356	-3.697	.903	-2.756	.440-07	.201-03	.440-07	.201-03	.800+01	.175-02	.201-03	.201-03	.201-03	.157+01
5.0	-8.156	-4.097	.903	-3.156	.698-08	.800-04	.698-08	.800-04	.800+01	.698-03	.800-04	.800-04	.800-04	.157+01

(N7)/I N7 17

SUM	SUM(L1	JFR	PHT
(1/LP)2	/LP)2		-23
.532+02	1.1871	.306	2.054

	SUM	SUM	RECIP
LI/LP	111(10)	LI/LP	POCAL
	132+02	1.969	.508

$$N = 9 \quad H^* = .262$$

PHI
-23
054

REDUCED DYNAMIC VISCOSITY AND MODULUS

[illegible]

REDUCED DYNAMIC VISCOSITY AND MODULUS									
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	FAIR	ETA2R	GIP	G2R	ETA1P	ETA2P	G1R	G2R	MOD
ETA2/1	ARCTAN	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1	ETA2/1
-2.8	.241	-2.758	-5.558	-2.559	.174+01	.175-02	.277-05	.276-02	.174+01
-2.0	.241	-1.958	-3.958	-1.759	.174+01	.110-01	.110-03	.174-01	.174+01
-1.8	.241	-1.758	-3.558	-1.559	.174+01	.175-01	.277-03	.276-01	.174+01
-1.4	.241	-1.359	-2.759	-1.159	.174+01	.438-01	.174-02	.693-01	.174+01
-1.0	.238	-.962	-1.962	-.762	.173+01	.109+00	.109-01	.173+00	.174+01
-.8	.235	-.768	-1.568	-.565	.172+01	.171+00	.270-01	.272+00	.173+01
-.6	.226	-.582	-1.182	-.374	.168+01	.252+00	.657-01	.427+00	.170+01
-.4	.205	-.416	-.816	-.195	.160+01	.394+00	.153+00	.638+00	.165+01
-.2	.161	-.289	-.489	-.039	.145+01	.514+00	.324+00	.914+00	.154+01
.0	.087	-.225	-.275	.087	.122+01	.596+00	.596+00	.122+01	.136+01
.2	-.010	-.227	-.027	.190	.978+00	.593+00	.939+00	.155+01	.114+01
.4	-.109	-.271	.129	.291	.777+00	.535+00	.134+01	.195+01	.944+00
.6	-.207	-.331	.269	.393	.620+00	.467+00	.186+01	.247+01	.776+00
.8	-.307	-.398	.402	.493	.493+00	.400+00	.253+01	.311+01	.635+00
1.0	-.409	-.470	.530	.591	.390+00	.339+00	.339+01	.390+01	.517+00
1.2	-.514	-.545	.655	.686	.306+00	.295+00	.452+01	.435+01	.418+00
1.4	-.625	-.622	.778	.775	.237+00	.239+00	.600+01	.596+01	.337+00
1.6	-.744	-.699	.901	.856	.180+00	.200+00	.797+01	.717+01	.269+00
1.8	-.890	-.777	1.023	.920	.132+00	.167+00	.105+02	.832+01	.213+00
2.0	-1.044	-.861	1.139	.956	.904-01	.138+00	.138+02	.904+01	.165+00
2.2	-1.253	-.959	1.241	.947	.559-01	.110+00	.174+02	.895+01	.123+00
2.4	-1.521	-1.085	1.315	.879	.301-01	.872-01	.207+02	.757+01	.876-01
2.6	-1.846	-1.241	1.359	.754	.143-01	.575-01	.229+02	.568+01	.592-01
2.8	-2.209	-1.419	1.391	.591	.618-02	.381-01	.241+02	.390+01	.386-01
3.0	-2.593	-1.609	1.391	.407	.255-02	.246-01	.246+02	.255+01	.247-01
3.4	-3.384	-2.003	1.397	.016	.413-03	.993-02	.249+02	.104+01	.994-02
3.8	-4.182	-2.402	1.398	-.382	.657-04	.396-02	.250+02	.415+00	.396-02
4.2	-4.982	-2.802	1.398	-.782	.104-04	.158-02	.250+02	.165+00	.158-02
4.6	-5.782	-3.202	1.398	-1.182	.165-05	.628-03	.250+02	.657-01	.628-03
5.0	-6.582	-3.602	1.398	-1.582	.262-06	.250-03	.250+02	.262-01	.250-03

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM SUM(L1 JER PHI
 .193-01 .347+01 .288+00 .927+02 1.791 .558 .297+04 1.1097 .346 1.077

REDUCED DYNAMIC VISCOSITY AND MODULUS										N= 25 H= .075			
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	SUM	SUM(L1	JER	PHI
OMTI	ETAIR	ETA2R	G1R	G2R	ETAIR	ETA2R	G1R	G2P	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.253	-2.755	-5.555	-2.547	.179+01	.176-02	.279-05	.284-02	.179+01	.179+01	.179+01	.179+01	.982-03
-2.0	.253	-1.955	-3.955	-1.747	.179+01	.111-01	.111-03	.179-01	.179+01	.179+01	.179+01	.179+01	.620-02
-1.8	.253	-1.755	-3.555	-1.547	.179+01	.176-01	.279-03	.284-01	.179+01	.179+01	.179+01	.179+01	.982-02
-1.4	.253	-1.355	-2.755	-1.147	.179+01	.441-01	.176-02	.712-01	.179+01	.179+01	.179+01	.179+01	.246-01
-1.0	.251	-.959	-1.959	-.749	.178+01	.110+00	.110-01	.178+00	.178+01	.178+01	.178+01	.178+01	.617-01
-.8	.247	-.765	-1.565	-.553	.177+01	.172+00	.273-01	.280+00	.177+01	.177+01	.177+01	.177+01	.971-01
-.6	.238	-.579	-1.179	-.362	.173+01	.264+00	.662-01	.435+00	.175+01	.175+01	.175+01	.175+01	.151+00
-.4	.218	-.412	-.812	-.182	.165+01	.387+00	.154+00	.657+00	.170+01	.170+01	.170+01	.170+01	.230+00
-.2	.175	-.285	-.485	-.025	.150+01	.519+00	.327+00	.944+00	.158+01	.158+01	.158+01	.158+01	.334+00
.0	.103	-.219	-.219	.103	.127+01	.604+00	.604+00	.127+01	.140+01	.140+01	.140+01	.140+01	.444+00
.2	.010	-.219	-.019	.210	.102+01	.603+00	.956+00	.162+01	.119+01	.119+01	.119+01	.119+01	.533+00
.4	-.088	-.260	.140	.312	.817+00	.549+00	.138+01	.205+01	.985+00	.985+00	.985+00	.985+00	.591+00
.6	-.184	-.317	.283	.416	.655+00	.482+00	.192+01	.261+01	.813+00	.813+00	.813+00	.813+00	.635+00
.8	-.282	-.361	.419	.518	.523+00	.416+00	.263+01	.330+01	.668+00	.668+00	.668+00	.668+00	.673+00
1.0	-.383	-.450	.550	.617	.414+00	.355+00	.355+01	.414+01	.548+00	.548+00	.548+00	.548+00	.708+00
1.2	-.488	-.522	.678	.712	.325+00	.301+00	.476+01	.516+01	.443+00	.443+00	.443+00	.443+00	.746+00
1.4	-.599	-.596	.804	.801	.252+00	.254+00	.637+01	.632+01	.357+00	.357+00	.357+00	.357+00	.789+00
1.6	-.722	-.670	.930	.878	.190+00	.214+00	.850+01	.755+01	.286+00	.286+00	.286+00	.286+00	.844+00
1.8	-.863	-.747	1.053	.937	.137+00	.179+00	.113+02	.864+01	.225+00	.225+00	.225+00	.225+00	.918+00
2.0	1.038	-.832	1.158	.962	.916-01	.147+00	.147+02	.916+01	.173+00	.173+00	.173+00	.173+00	.101+01
2.2	1.263	-.936	1.264	.937	.546-01	.116+00	.183+02	.866+01	.128+00	.128+00	.128+00	.128+00	.113+01
2.4	1.548	-1.070	1.330	.857	.293-01	.851-01	.214+02	.711+01	.897-01	.897-01	.897-01	.897-01	.125+01
2.6	1.686	-1.233	1.367	.714	.130-01	.595-01	.233+02	.518+01	.599-01	.599-01	.599-01	.599-01	.135+01
2.8	2.257	-1.415	1.385	.543	.554-02	.385-01	.243+02	.349+01	.389-01	.389-01	.389-01	.389-01	.143+01
3.0	2.644	-1.607	1.393	.356	.227-02	.247-01	.247+02	.227+01	.248-01	.248-01	.248-01	.248-01	.148+01
3.4	3.437	-2.003	1.397	-.037	.365-03	.993-02	.250+02	.918+00	.994-02	.994-02	.994-02	.994-02	.153+01
3.8	4.236	-2.402	1.398	-.436	.581-04	.396-02	.250+02	.366+00	.396-02	.396-02	.396-02	.396-02	.156+01
4.2	5.036	-2.802	1.398	-.836	.921-05	.158-02	.250+02	.146+00	.158-02	.158-02	.158-02	.158-02	.156+01
4.6	5.836	-3.202	1.398	-1.236	.146-05	.628-03	.250+02	.581-01	.628-03	.628-03	.628-03	.628-03	.157+01
5.0	6.636	-3.602	1.398	-1.636	.231-06	.250-03	.250+02	.231-01	.250-03	.250-03	.250-03	.250-03	.157+01

EXACT Z7MM EIGENVALUES
 LN 1/(LN) SUM 1/(LP) SUM L1/LP SUM RECIP ROCAL PHI
 -209-01 .330+01 .303+00 .881+02 1.840 .543
 SUM (1/LP)2 /LP)2 SUM (1/LP)2 /LP)2 SUM (1/LP)2 /LP)2
 .256+04 1.1177 .330 1.364

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON				ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	FTAIR	ETA2R	GIR	G2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	G1R	G2R	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.265	-2.752	-5.552	-2.535	.184+01	.177-02	.184+01	.177-02	.184+01	.281-05	.292-02	.184+01	.184+01	.963-03	.963-03
-2.0	.265	-1.952	-3.952	-1.735	.184+01	.112-01	.184+01	.112-01	.184+01	.112-03	.184-01	.184+01	.184+01	.607-02	.607-02
-1.8	.265	-1.752	-3.552	-1.535	.184+01	.177-01	.184+01	.177-01	.184+01	.281-03	.292-01	.184+01	.184+01	.963-02	.963-02
-1.4	.264	-1.352	-2.752	-1.136	.184+01	.444-01	.184+01	.444-01	.184+01	.177-02	.732-01	.184+01	.184+01	.242-01	.242-01
-1.0	.262	-.956	-1.956	-.738	.183+01	.111+00	.183+01	.111+00	.183+01	.111-01	.183+00	.183+01	.183+01	.605-01	.605-01
-.8	.259	-.761	-1.561	-.541	.181+01	.173+00	.181+01	.173+00	.181+01	.275-01	.288+00	.182+01	.182+01	.952-01	.952-01
-.6	.250	-.576	-1.176	-.350	.178+01	.266+00	.178+01	.266+00	.178+01	.667-01	.447+00	.180+01	.180+01	.148+00	.148+00
-.4	.230	-.409	-.809	-.170	.170+01	.390+00	.170+01	.390+00	.170+01	.155+00	.676+00	.174+01	.174+01	.226+00	.226+00
-.2	.189	-.281	-.481	-.011	.154+01	.524+00	.154+01	.524+00	.154+01	.330+00	.975+00	.163+01	.163+01	.327+00	.327+00
.0	.119	-.214	-.214	.119	.131+01	.611+00	.131+01	.611+00	.131+01	.611+00	.131+01	.145+01	.145+01	.435+00	.435+00
.2	.028	-.212	-.012	.228	.107+01	.614+00	.107+01	.614+00	.107+01	.973+00	.169+01	.123+01	.123+01	.522+00	.522+00
.4	-.067	-.250	.150	.333	.858+00	.552+00	.858+00	.552+00	.858+00	.141+01	.215+01	.103+01	.103+01	.580+00	.580+00
.6	-.161	-.303	.297	.439	.690+00	.497+00	.690+00	.497+00	.690+00	.198+01	.275+01	.851+00	.851+00	.524+00	.524+00
.8	-.258	-.364	.436	.542	.552+00	.432+00	.552+00	.432+00	.552+00	.273+01	.349+01	.701+00	.701+00	.664+00	.664+00
1.0	-.358	-.431	.569	.642	.439+00	.371+00	.439+00	.371+00	.439+00	.371+01	.439+01	.575+00	.575+00	.702+00	.702+00
1.2	-.463	-.500	.700	.737	.345+00	.316+00	.345+00	.316+00	.345+00	.501+01	.546+01	.458+00	.458+00	.743+00	.743+00
1.4	-.575	-.571	.829	.825	.266+00	.269+00	.266+00	.269+00	.266+00	.675+01	.658+01	.378+00	.378+00	.791+00	.791+00
1.6	-.701	-.643	.957	.899	.199+00	.228+00	.199+00	.228+00	.199+00	.906+01	.792+01	.302+00	.302+00	.852+00	.852+00
1.8	-.849	-.719	1.031	.951	.141+00	.191+00	.141+00	.191+00	.141+00	.121+02	.893+01	.238+00	.238+00	.934+00	.934+00
2.0	-1.035	-.806	1.194	.965	.922-01	.156+00	.922-01	.156+00	.922-01	.156+02	.922+01	.182+00	.182+00	.104+01	.104+01
2.2	-1.276	-.916	1.284	.924	.529-01	.121+00	.529-01	.121+00	.529-01	.192+02	.839+01	.132+00	.132+00	.116+01	.116+01
2.4	-1.578	-1.058	1.342	.822	.264-01	.875-01	.264-01	.875-01	.264-01	.220+02	.664+01	.915-01	.915-01	.128+01	.128+01
2.6	-1.927	-1.227	1.373	.673	.118-01	.593-01	.118-01	.593-01	.118-01	.236+02	.471+01	.605-01	.605-01	.137+01	.137+01
2.8	-2.304	-1.412	1.398	.496	.497-02	.387-01	.497-02	.387-01	.497-02	.244+02	.314+01	.390-01	.390-01	.144+01	.144+01
3.0	-2.694	-1.606	1.394	.306	.202-02	.248-01	.202-02	.248-01	.202-02	.248+02	.202+01	.248-01	.248-01	.149+01	.149+01
3.2	-3.488	-2.003	1.397	-.088	.325-03	.994-02	.325-03	.994-02	.325-03	.250+02	.816+00	.994-02	.994-02	.154+01	.154+01
3.4	-4.287	-2.402	1.398	-.487	.516-04	.396-02	.516-04	.396-02	.516-04	.250+02	.326+00	.396-02	.396-02	.156+01	.156+01
3.6	-5.087	-2.802	1.398	-.887	.818-05	.158-02	.818-05	.158-02	.818-05	.250+02	.130+00	.158-02	.158-02	.157+01	.157+01
3.8	-5.687	-3.202	1.398	-1.287	.130-05	.628-03	.130-05	.628-03	.130-05	.250+02	.516-01	.628-03	.628-03	.157+01	.157+01
4.0	-6.687	-3.602	1.398	-1.687	.206-06	.250-03	.206-06	.250-03	.206-06	.250+02	.206-01	.250-03	.250-03	.157+01	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 JFR SUM(L1) H* = .130 PHI
 -228-01 .310+01 .323+00 .835+02 1.899 .527 .218+04 1.1270 .313 1.681

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2I	ETA2R	ETA2I
OMTI	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	ETA2I	ETA2R	ETA2I
-2.8	.278	-2.748	-5.548	-2.522	.190+01	.179-02	.283-05	.301-02	.190+01	.190+01	.941-03	.190+01	.941-03
-2.0	.278	-1.948	-3.948	-1.722	.190+01	.113-01	.113-03	.190-01	.190+01	.190+01	.594-02	.190+01	.594-02
-1.8	.278	-1.748	-3.548	-1.522	.190+01	.179-01	.283-03	.301-01	.190+01	.190+01	.941-02	.190+01	.941-02
-1.4	.278	-1.349	-2.749	-1.122	.190+01	.448-01	.178-02	.755-01	.190+01	.190+01	.236-01	.190+01	.236-01
-1.0	.276	-.952	-1.952	-.724	.189+01	.112+00	.112-01	.189+00	.189+01	.189+01	.591-01	.189+01	.591-01
-.8	.273	-.758	-1.558	-.527	.187+01	.175+00	.277-01	.297+00	.188+01	.188+01	.930-01	.188+01	.930-01
-.6	.264	-.572	-1.172	-.336	.184+01	.268+00	.673-01	.462+00	.186+01	.186+01	.145+00	.186+01	.145+00
-.4	.245	-.405	-.805	-.155	.176+01	.394+00	.157+00	.700+00	.180+01	.180+01	.220+00	.180+01	.220+00
-.2	.205	-.276	-.476	.005	.160+01	.529+00	.334+00	.101+01	.169+01	.169+01	.319+00	.169+01	.319+00
.0	.137	-.208	-.208	.137	.137+01	.620+00	.620+00	.137+01	.150+01	.150+01	.424+00	.150+01	.424+00
.2	.049	-.204	-.004	.249	.112+01	.626+00	.992+00	.178+01	.128+01	.128+01	.510+00	.128+01	.510+00
.4	-.043	-.238	.162	.357	.906+00	.578+00	.145+01	.228+01	.107+01	.107+01	.567+00	.107+01	.567+00
.6	-.135	-.288	.312	.465	.733+00	.515+00	.205+01	.292+01	.896+00	.896+00	.612+00	.896+00	.612+00
.8	-.230	-.346	.454	.570	.589+00	.451+00	.285+01	.372+01	.742+00	.742+00	.653+00	.742+00	.653+00
1.0	-.329	-.408	.592	.671	.469+00	.391+00	.391+01	.469+01	.610+00	.610+00	.694+00	.610+00	.694+00
1.2	-.434	-.474	.726	.766	.368+00	.336+00	.532+01	.584+01	.498+00	.498+00	.739+00	.498+00	.739+00
1.4	-.548	-.541	.859	.852	.283+00	.288+00	.723+01	.711+01	.404+00	.404+00	.794+00	.404+00	.794+00
1.6	-.678	-.610	.990	.922	.210+00	.245+00	.977+01	.835+01	.323+00	.323+00	.864+00	.323+00	.864+00
1.8	-.836	-.686	1.114	.964	.146+00	.206+00	.130+02	.921+01	.253+00	.253+00	.955+00	.253+00	.955+00
2.0	-1.037	-.777	1.223	.963	.918-01	.167+00	.167+02	.918+01	.191+00	.191+00	.107+01	.191+00	.107+01
2.2	-1.298	-.895	1.305	.902	.504-01	.127+00	.202+02	.799+01	.137+00	.137+00	.119+01	.137+00	.119+01
2.4	-1.616	-1.046	1.354	.784	.242-01	.900-01	.226+02	.608+01	.932-01	.932-01	.131+01	.932-01	.131+01
2.6	-1.976	-1.221	1.379	.624	.106-01	.601-01	.239+02	.421+01	.610-01	.610-01	.140+01	.610-01	.140+01
2.8	-2.359	-1.410	1.390	.441	.438-02	.389-01	.246+02	.276+01	.392-01	.392-01	.146+01	.392-01	.146+01
3.0	-2.751	-1.605	1.395	.249	.177-02	.248-01	.248+02	.177+01	.249-01	.249-01	.150+01	.249-01	.150+01
3.4	-3.547	-2.003	1.397	-.147	.284-03	.994-02	.250+02	.713+00	.995-02	.995-02	.154+01	.995-02	.154+01
3.8	-4.346	-2.402	1.398	-.546	.450-04	.396-02	.250+02	.284+00	.396-02	.396-02	.156+01	.396-02	.156+01
4.2	-5.146	-2.802	1.398	-.946	.714-05	.158-02	.250+02	.113+00	.158-02	.158-02	.157+01	.158-02	.157+01
4.6	-5.946	-3.202	1.398	-1.346	.113-05	.628-03	.250+02	.451-01	.628-03	.628-03	.157+01	.628-03	.157+01
5.0	-6.746	-3.602	1.398	-1.746	.179-06	.250-03	.250+02	.179-01	.250-03	.250-03	.157+01	.250-03	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² /LP² SUM(L1) JER PHI
 .240-01 .296+01 .337+00 .808+02 1.938 .516 .197+04 1.1331 .302 1.877

N=25 H*=.150

REDUCED DYNAMIC VISCOSITY AND MODULUS										MCD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2/I	ETA2R	ETA2/I
0MTI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA2R	ETA2/I	ETA2/I	ETA2R	ETA2/I
-2.8	.287	-2.746	-5.546	-2.513	.194+01	.180-02	.285-05	.307-02	.194+01	.927-03	.927-03	.194+01	.927-03
-2.0	.287	-1.946	-3.946	-1.712	.194+01	.113-01	.113-03	.194-01	.194+01	.585-02	.585-02	.194+01	.585-02
-1.8	.287	-1.746	-3.546	-1.513	.194+01	.180-01	.285-03	.307-01	.194+01	.927-02	.927-02	.194+01	.927-02
-1.4	.287	-1.346	-2.746	-1.113	.194+01	.450-01	.179-02	.771-01	.194+01	.233-01	.233-01	.194+01	.233-01
-1.0	.285	-.950	-1.950	-.715	.193+01	.112+00	.112-01	.193+00	.197+01	.582-01	.582-01	.197+01	.582-01
-.8	.282	-.755	-1.555	-.513	.191+01	.176+00	.278-01	.303+00	.192+01	.916-01	.916-01	.192+01	.916-01
-.6	.273	-.569	-1.159	-.327	.188+01	.270+00	.677-01	.471+00	.190+01	.143+00	.143+00	.190+01	.143+00
-.4	.254	-.402	-.802	-.146	.180+01	.396+00	.158+00	.715+00	.184+01	.217+00	.217+00	.184+01	.217+00
-.2	.215	-.273	-.473	.015	.164+01	.533+00	.336+00	.104+01	.173+01	.314+00	.314+00	.173+01	.314+00
.0	.149	-.204	-.204	.149	.141+01	.675+00	.625+00	.141+01	.154+01	.418+00	.418+00	.154+01	.418+00
.2	.063	-.198	.062	.263	.116+01	.634+00	.100+01	.183+01	.132+01	.501+00	.501+00	.132+01	.501+00
.4	-.027	-.231	.169	.373	.940+00	.598+00	.148+01	.236+01	.111+01	.559+00	.559+00	.111+01	.559+00
.6	-.118	-.278	.322	.482	.762+00	.527+00	.210+01	.303+01	.927+00	.605+00	.605+00	.927+00	.605+00
.8	-.212	-.334	.466	.588	.614+00	.454+00	.293+01	.388+01	.770+00	.647+00	.647+00	.770+00	.647+00
1.0	-.310	-.394	.606	.690	.490+00	.404+00	.404+01	.490+01	.635+00	.690+00	.690+00	.635+00	.690+00
1.2	-.415	-.456	.744	.785	.394+00	.350+00	.554+01	.609+01	.520+00	.738+00	.738+00	.520+00	.738+00
1.4	-.531	-.521	.879	.869	.295+00	.301+00	.757+01	.740+01	.421+00	.797+00	.797+00	.421+00	.797+00
1.6	-.665	-.589	1.011	.935	.216+00	.258+00	.103+02	.862+01	.337+00	.872+00	.872+00	.337+00	.872+00
1.8	-.829	-.664	1.136	.971	.148+00	.217+00	.137+02	.935+01	.262+00	.971+00	.971+00	.262+00	.971+00
2.0	-1.041	-.753	1.241	.959	.909-01	.174+00	.174+02	.909+01	.197+00	.109+01	.109+01	.197+00	.109+01
2.2	-1.314	-.883	1.317	.886	.485-01	.131+00	.207+02	.769+01	.140+00	.122+01	.122+01	.140+00	.122+01
2.4	-1.643	-1.039	1.351	.757	.227-01	.913-01	.229+02	.571+01	.941-01	.133+01	.133+01	.941-01	.133+01
2.6	-2.009	-1.218	1.382	.591	.979-02	.605-01	.241+02	.390+01	.613-01	.141+01	.141+01	.613-01	.141+01
2.8	-2.335	-1.409	1.391	.475	.403-02	.390-01	.246+02	.254+01	.392-01	.147+01	.147+01	.392-01	.147+01
3.0	-2.789	-1.605	1.395	.211	.163-02	.248-01	.248+02	.163+01	.249-01	.151+01	.151+01	.249-01	.151+01
3.2	-3.585	-2.002	1.398	-.185	.260-03	.994-02	.250+02	.653+00	.995-02	.154+01	.154+01	.995-02	.154+01
3.4	-4.385	-2.402	1.398	-.585	.112-04	.396-02	.250+02	.260+00	.396-02	.156+01	.156+01	.396-02	.156+01
4.0	-5.185	-2.802	1.398	-.985	.654-05	.158-02	.250+02	.104+00	.158-02	.157+01	.157+01	.158-02	.157+01
4.6	-5.985	-3.202	1.398	-1.385	.104-05	.628-03	.250+02	.413-01	.628-03	.157+01	.157+01	.628-03	.157+01
5.0	-6.785	-3.602	1.398	-1.785	.164-06	.250-03	.250+02	.164-01	.250-03	.157+01	.157+01	.250-03	.157+01

EXACT ZIMM EIGENVALUES
 LI LN SUM 1/(LN) SUM 1/(LP) SUM 1/LP RECIP ROCAL SUM (1/LP)² SUM (1/LP)² /LP² PHI
 -270-01 .262+01 .381+00 .754+02 2.039 .491 .157+04 1.1478 .276 2.335

N= 25 H*= .200

REDUCED DYNAMIC VISCOSITY AND MODULUS

LOG OMTI	LOG FTAIR	LOG ETA2R	LOG GIP	LOG G2R	ETA1P	ETA2R	G1R	G2R	MOD ETAP	ARCTAN CTA2/1
-2.8	.309	-2.740	-5.540	-2.491	.204+01	.192-02	.288-05	.323-02	.204+01	.892-03
-2.0	.309	-1.940	-3.940	-1.601	.204+01	.115-01	.115-03	.204-01	.204+01	.563-02
-1.8	.309	-1.740	-3.540	-1.491	.204+01	.192-01	.288-03	.323-01	.204+01	.892-02
-1.4	.309	-1.341	-2.741	-1.091	.204+01	.456-01	.192-02	.811-01	.204+01	.224-01
-1.0	.307	-.944	-1.944	-.693	.203+01	.114+00	.114-01	.203+00	.203+01	.560-01
-.8	.304	-.750	-1.550	-.496	.201+01	.178+00	.282-01	.319+00	.202+01	.882-01
-.6	.296	-.563	-1.163	-.304	.198+01	.273+00	.686-01	.497+00	.200+01	.137+00
-.4	.278	-.396	-.796	-.122	.190+01	.402+00	.150+00	.755+00	.194+01	.209+00
-.2	.241	-.266	-.466	.041	.174+01	.542+00	.342+00	.110+01	.182+01	.302+00
.0	.178	-.195	-.195	.178	.151+01	.639+00	.639+00	.151+01	.164+01	.401+00
.2	.097	-.185	.015	.297	.125+01	.653+00	.104+01	.198+01	.141+01	.482+00
.4	.011	-.213	.197	.411	.103+01	.613+00	.154+01	.258+01	.119+01	.539+00
.6	-.076	-.255	.345	.524	.839+00	.556+00	.222+01	.334+01	.101+01	.586+00
.8	-.167	-.304	.496	.633	.680+00	.407+00	.314+01	.429+01	.843+00	.631+00
1.0	-.264	-.357	.643	.736	.545+00	.440+00	.440+01	.545+01	.700+00	.679+00
1.2	-.370	-.413	.787	.830	.427+00	.387+00	.613+01	.677+01	.576+00	.736+00
1.4	-.490	-.471	.929	.910	.324+00	.338+00	.849+01	.813+01	.468+00	.807+00
1.6	-.635	-.535	1.065	.965	.212+00	.292+00	.116+02	.924+01	.373+00	.899+00
1.8	-.820	-.614	1.186	.980	.152+00	.243+00	.154+02	.956+01	.287+00	.101+01
2.0	-1.052	-.719	1.281	.938	.868-01	.191+00	.191+02	.868+01	.210+00	.114+01
2.2	-1.355	-.859	1.341	.835	.432-01	.118+00	.219+02	.684+01	.145+00	.127+01
2.4	-1.715	-1.027	1.373	.685	.193-01	.940-01	.236+02	.484+01	.960-01	.137+01
2.6	-2.093	-1.212	1.388	.507	.807-02	.613-01	.244+02	.321+01	.619-01	.144+01
2.8	-2.484	-1.406	1.354	.316	.328-02	.392-01	.248+02	.207+01	.394-01	.149+01
3.0	-2.680	-1.604	1.396	.120	.132-02	.249-01	.249+02	.132+01	.249-01	.152+01
3.4	-3.678	-2.002	1.398	-.278	.210-03	.995-02	.250+02	.527+00	.995-02	.155+01
3.8	-4.478	-2.402	1.398	-.678	.333-04	.396-02	.250+02	.210+00	.396-02	.156+01
4.2	-5.277	-2.802	1.398	-1.077	.528-05	.158-02	.250+02	.837-01	.158-02	.157+01
4.6	-6.077	-3.202	1.398	-1.477	.837-06	.628-03	.250+02	.333-01	.628-03	.157+01
5.0	-6.877	-3.602	1.398	-1.877	.133-06	.250-03	.250+02	.133-01	.250-03	.157+01

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#1250

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 SUM(LI JFR PHI
 .308-01 .220+01 .454+00 .706+02 2.173 .460 .123+04 1.1659 .247 2.864

N= 25 H*= .262

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON			ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	FAIR	ETA2R	GIR	ETAIR	ETA2R	G2R	G2R	G2R	G2R	G2R	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.337	-2.733	-5.533	-2.463	.217+01	.195-02	.293-05	.344-02	.217+01	.217+01	.217+01	.217+01	.851-03	
-2.0	.337	-1.933	-3.933	-1.663	.217+01	.117-01	.117-01	.217-01	.217+01	.217+01	.217+01	.217+01	.537-02	
-1.8	.337	-1.733	-3.533	-1.463	.217+01	.195-01	.293-03	.344-01	.217+01	.217+01	.217+01	.217+01	.850-02	
-1.4	.337	-1.334	-2.734	-1.063	.217+01	.464-01	.185-02	.864-01	.217+01	.217+01	.217+01	.217+01	.213-01	
-1.0	.335	-.937	-1.937	-.665	.216+01	.116+00	.116-01	.216+00	.217+01	.217+01	.217+01	.217+01	.534-01	
-.8	.332	-.743	-1.543	-.468	.215+01	.191+00	.297-01	.340+00	.215+01	.215+01	.215+01	.215+01	.840-01	
-.6	.324	-.556	-1.156	-.276	.211+01	.278+03	.698-01	.530+00	.213+01	.213+01	.213+01	.213+01	.131+00	
-.4	.307	-.388	-.788	-.093	.203+01	.409+00	.163+00	.808+00	.207+01	.207+01	.207+01	.207+01	.199+00	
-.2	.272	-.257	-.457	.072	.187+01	.553+00	.349+00	.118+01	.195+01	.195+01	.195+01	.195+01	.287+00	
.0	.214	-.184	-.184	.214	.164+01	.655+00	.655+00	.164+01	.176+01	.176+01	.176+01	.176+01	.381+00	
.2	.138	-.169	.031	.338	.137+01	.677+00	.107+01	.218+01	.153+01	.153+01	.153+01	.153+01	.458+00	
.4	.058	-.191	.209	.458	.114+01	.645+00	.162+01	.287+01	.131+01	.131+01	.131+01	.131+01	.514+00	
.6	-.025	-.225	.375	.575	.945+00	.595+00	.237+01	.376+01	.112+01	.112+01	.112+01	.112+01	.562+00	
.8	-.112	-.266	.534	.688	.773+00	.542+00	.342+01	.487+01	.944+00	.944+00	.944+00	.944+00	.612+00	
1.0	-.207	-.309	.591	.793	.621+00	.490+00	.490+01	.621+01	.791+00	.791+00	.791+00	.791+00	.669+00	
1.2	-.315	-.356	.844	.885	.485+00	.441+00	.699+01	.768+01	.655+00	.655+00	.655+00	.655+00	.738+00	
1.4	-.443	-.406	.994	.957	.360+00	.392+00	.985+01	.905+01	.533+00	.533+00	.533+00	.533+00	.828+00	
1.6	-.608	-.469	1.131	.992	.247+00	.340+00	.135+02	.982+01	.420+00	.420+00	.420+00	.420+00	.942+00	
1.8	-.825	-.557	1.243	.975	.150+00	.276+00	.175+02	.943+01	.315+00	.315+00	.315+00	.315+00	.108+01	
2.0	-1.106	-.680	1.320	.944	.783-01	.209+00	.209+02	.783+01	.223+00	.223+00	.223+00	.223+00	.121+01	
2.2	-1.442	-.837	1.363	.758	.361-01	.146+00	.231+02	.573+01	.150+00	.150+00	.150+00	.150+00	.133+01	
2.4	-1.812	-1.017	1.383	.588	.154-01	.962-01	.242+02	.387+01	.974-01	.974-01	.974-01	.974-01	.141+01	
2.6	-2.199	-1.208	1.392	.401	.632-02	.619-01	.247+02	.252+01	.623-01	.623-01	.623-01	.623-01	.147+01	
2.8	-2.594	-1.454	1.396	.206	.255-02	.394-01	.249+02	.161+01	.395-01	.395-01	.395-01	.395-01	.151+01	
3.0	-2.992	-1.603	1.397	.008	.102-02	.249-01	.249+02	.102+01	.250-01	.250-01	.250-01	.250-01	.153+01	
3.4	-3.791	-2.002	1.398	-.391	.162-03	.995-02	.250+02	.407+03	.995-02	.995-02	.995-02	.995-02	.155+01	
3.8	-4.590	-2.402	1.398	-.790	.257-04	.396-02	.250+02	.162+00	.396-02	.396-02	.396-02	.396-02	.156+01	
4.2	-5.390	-2.802	1.398	-1.190	.407-05	.158-02	.250+02	.645-01	.158-02	.158-02	.158-02	.158-02	.157+01	
4.6	-6.190	-3.202	1.398	-1.590	.645-06	.626-03	.250+02	.257-01	.628-03	.628-03	.628-03	.628-03	.157+01	
5.0	-6.990	-3.602	1.398	-1.990	.102-06	.250-03	.250+02	.102-01	.250-03	.250-03	.250-03	.250-03	.157+01	

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) L1/LP RECIP SUM (1/LP)2 /LP)2 JER SUM(L1 JER PHI
 .330-01 .194+01 .515+00 .685+02 2.263 .442 .108+04 1.1773 .230 3.183

N= 25 H= .300

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.355	-2.729	-5.529	-2.445	.226+01	.197-02	.296-05	.359-02	.226+01	.226+01	.226+01	.226+01	.226+01
-2.0	.355	-1.929	-3.929	-1.645	.226+01	.118-01	.118-03	.226-01	.226+01	.226+01	.226+01	.226+01	.226+01
-1.8	.355	-1.729	-3.529	-1.445	.226+01	.197-01	.296-03	.359-01	.226+01	.226+01	.226+01	.226+01	.226+01
-1.4	.354	-1.330	-2.730	-1.045	.226+01	.468-01	.186-07	.900-01	.226+01	.226+01	.226+01	.226+01	.226+01
-1.0	.353	-.933	-1.933	-.647	.226+01	.117+00	.117-01	.225+00	.226+01	.226+01	.226+01	.226+01	.226+01
-.8	.350	-.738	-1.538	-.450	.224+01	.193+00	.289-01	.355+00	.224+01	.224+01	.224+01	.224+01	.224+01
-.6	.343	-.552	-1.152	-.257	.220+01	.291+00	.705-01	.553+00	.222+01	.222+01	.222+01	.222+01	.222+01
-.4	.326	-.384	-.784	-.074	.212+01	.413+00	.165+00	.844+00	.216+01	.216+01	.216+01	.216+01	.216+01
-.2	.293	-.252	-.452	.093	.196+01	.560+00	.353+00	.124+01	.204+01	.204+01	.204+01	.204+01	.204+01
.0	.236	-.177	-.177	.235	.172+01	.666+00	.666+00	.172+01	.185+01	.185+01	.185+01	.185+01	.185+01
.2	.164	-.160	.040	.364	.146+01	.692+00	.110+01	.231+01	.162+01	.162+01	.162+01	.162+01	.162+01
.4	.087	-.177	.223	.487	.122+01	.655+00	.167+01	.307+01	.139+01	.139+01	.139+01	.139+01	.139+01
.6	.008	-.207	.393	.608	.102+01	.622+00	.247+01	.405+01	.119+01	.119+01	.119+01	.119+01	.119+01
.8	-.077	-.241	.559	.723	.837+00	.574+00	.362+01	.528+01	.102+01	.102+01	.102+01	.102+01	.102+01
1.0	-.171	-.278	.722	.820	.674+00	.527+00	.527+01	.674+01	.856+00	.856+00	.856+00	.856+00	.856+00
1.2	-.281	-.318	.882	.919	.523+00	.481+00	.763+01	.829+01	.711+00	.711+00	.711+00	.711+00	.711+00
1.4	-.418	-.364	1.036	.982	.392+00	.432+00	.109+02	.959+01	.577+00	.577+00	.577+00	.577+00	.577+00
1.6	-.599	-.429	1.171	1.001	.252+00	.373+00	.148+02	.100+02	.450+00	.450+00	.450+00	.450+00	.450+00
1.8	-.840	-.525	1.275	.960	.145+00	.298+00	.188+02	.912+01	.331+00	.331+00	.331+00	.331+00	.331+00
2.0	-1.145	-.661	1.339	.855	.717-01	.218+00	.218+02	.717+01	.230+00	.230+00	.230+00	.230+00	.230+00
2.2	-1.496	-.823	1.372	.704	.319-01	.149+00	.236+02	.505+01	.152+00	.152+00	.152+00	.152+00	.152+00
2.4	-1.875	-1.013	1.387	.525	.133-01	.971-01	.244+02	.335+01	.980-01	.980-01	.980-01	.980-01	.980-01
2.6	-2.266	-1.206	1.394	.334	.542-02	.622-01	.248+02	.216+01	.624-01	.624-01	.624-01	.624-01	.624-01
2.8	-2.662	-1.404	1.396	.138	.218-02	.395-01	.249+02	.137+01	.395-01	.395-01	.395-01	.395-01	.395-01
3.0	-3.061	-1.603	1.397	-.061	.869-03	.250-01	.250+02	.869+00	.250-01	.250-01	.250-01	.250-01	.250-01
3.2	-3.460	-2.002	1.398	-.460	.138-03	.995-02	.250+02	.347+00	.995-02	.995-02	.995-02	.995-02	.995-02
3.4	-3.860	-2.402	1.398	-.860	.219-04	.396-02	.250+02	.138+00	.396-02	.396-02	.396-02	.396-02	.396-02
3.6	-4.260	-2.802	1.398	-1.260	.347-05	.158-02	.250+02	.550-01	.158-02	.158-02	.158-02	.158-02	.158-02
3.8	-4.660	-3.202	1.398	-1.660	.550-06	.628-03	.250+02	.219-01	.628-03	.628-03	.628-03	.628-03	.628-03
4.0	-5.060	-3.602	1.398	-2.060	.871-07	.250-03	.250+02	.871-02	.250-03	.250-03	.250-03	.250-03	.250-03

$$N = 50 \quad H^* = .050$$

EXACT ZIMM EIGENVALUES

SUM	SUM	RECIP
LI/LP)	LI/LP	ROCAL
339+03	1.780	.562

SUM	SUM(L1
(1/LP)2	/LP)2
-400+05	1.1048

PHI
-23
928

REDUCED DYNAMIC VISCOSITY AND MODULUS

[illegible]

EXACT ZIMM EIGENVALUES			SUM	RECIP	SUM	N= 50	H*= .075
LI	LN	1/(LN)	L1/LP	ROCAL	(1/LP)2	SUM(LI	JER
						/LP)2	PHI
.598-02	.348+01	.287+00	.308+03	.543	.312+05	1.1139	.329
							1.265
							-23

#1250

EXACT ZIMM EIGENVALUES						N= 50 H*= .10
L1	LN	SUM 1/(LN)	SUM 1/(LP)	RECIP ROCAL	SUM (1/LP)2 /LP)2	PFI -23
.669-.02	.331+.01	.302+00	.283+.03	.527	.250+.05 1.1221	.312 1.552

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EXACT ZIMM EIGENVALUES						N= 50 H*= .130			
L1	LN	1/(LN)	SUM	RECIP	SUM	SUM(L1	JFR	PHI	
			1/(LP)	ROCAL	(1/LP)2	/LP)2		-23	
.755-02	.311+01	.322+00	.260+03	.509	.198+05	1.1309	.293	1.851	

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EXACT ZIMM EIGENVALUES
LI LN 1/(LN)

REDUCED DYNAMIC VISCOSITY AND MODULUS

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REDUCED DYNAMIC VISCOSITY AND MODULUS										
LOG	LOG	LOG	LOG	LOG	ETAIR	ETA2R	G1R	G2R	MON	ARCTAN
OMTI	FTAIR	ETA2R	G1R	G2P					ETAR	ETA2/1
-2.8	.324	-2.740	-5.540	-2.476	.211+01	.192-02	.298-05	.334-02	.211+01	.863-03
-2.0	.324	-1.940	-3.940	-1.676	.211+01	.115-01	.115-03	.211-01	.211+01	.544-02
-1.8	.324	-1.740	-3.540	-1.476	.211+01	.192-01	.288-03	.334-01	.211+01	.862-02
-1.4	.324	-1.341	-2.741	-1.076	.211+01	.456-01	.182-07	.839-01	.211+01	.216-01
-1.0	.322	-.944	-1.944	-.678	.210+01	.114+00	.114-01	.210+00	.210+01	.542-01
-.8	.319	-.749	-1.549	-.481	.208+01	.178+00	.282-01	.330+00	.209+01	.852-01
-.6	.311	-.563	-1.163	-.289	.205+01	.273+00	.687-01	.514+00	.207+01	.133+00
-.4	.294	-.396	-.796	-.106	.197+01	.402+00	.160+00	.783+00	.201+01	.202+00
-.2	.258	-.266	-.466	.058	.191+01	.542+00	.342+00	.114+01	.199+01	.291+00
.0	.198	-.195	-.195	.198	.158+01	.629+00	.639+00	.158+01	.170+01	.385+00
.2	.120	-.185	.015	.320	.132+01	.653+00	.104+01	.209+01	.147+01	.460+00
.4	.040	-.213	.187	.440	.110+01	.613+00	.154+01	.275+01	.126+01	.510+00
.6	-.042	-.256	.344	.558	.909+00	.555+00	.221+01	.352+01	.106+01	.548+00
.8	-.125	-.306	.454	.675	.750+00	.494+00	.312+01	.473+01	.899+00	.582+00
1.0	-.211	-.362	.638	.789	.616+00	.435+00	.435+01	.616+01	.754+00	.615+00
1.2	-.300	-.420	.780	.900	.501+00	.380+00	.602+01	.794+01	.629+00	.649+00
1.4	-.395	-.481	.919	1.005	.403+00	.331+00	.830+01	.101+02	.521+00	.627+00
1.6	-.497	-.542	1.058	1.105	.318+00	.287+00	.114+02	.127+02	.429+00	.735+00
1.8	-.613	-.603	1.197	1.187	.244+00	.249+00	.157+02	.154+02	.349+00	.796+00
2.0	-.749	-.668	1.332	1.251	.173+00	.215+00	.215+02	.178+02	.279+00	.878+00
2.2	-.920	-.742	1.458	1.280	.120+00	.191+00	.287+02	.190+02	.217+00	.985+00
2.4	-1.145	-.840	1.560	1.255	.716-01	.145+00	.363+02	.180+02	.161+00	.111+01
2.6	-1.432	-.971	1.629	1.168	.370-01	.107+00	.426+02	.147+02	.113+00	.124+01
2.8	-1.772	-1.132	1.668	1.028	.169-01	.736-01	.465+02	.107+02	.757-01	.135+01
3.0	-2.144	-1.314	1.686	.856	.718-02	.495-01	.485+02	.718+01	.490-01	.142+01
3.2	-.927	-1.703	1.697	.473	.118-02	.198-01	.498+02	.297+01	.198-01	.151+01
3.4	-3.724	-2.101	1.699	.076	.189-03	.792-02	.500+02	.119+01	.792-02	.155+01
4.2	-4.524	-2.501	1.699	-.324	.299-04	.315-02	.500+02	.475+00	.315-02	.156+01
4.6	-5.324	-2.901	1.699	-.724	.475-05	.126-02	.500+02	.189+00	.126-02	.157+01
5.0	-6.124	-3.301	1.699	-1.124	.752-06	.500-03	.500+02	.752-01	.500-03	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (L1/LP)2 JER PHI
 .109-01 .229+01 .437+00 .203+03 2.215 .452 .969+04 1.1587 .236 2.773

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	ETAIR	ETA2R	GIR	ETAIP	ETA2R	GIR	ETAIP	ETA2R	GIR	G2R	ETAIR	ETA2R	ETA2R
-2.8	.345	-2.736	-5.536	.221+01	.184-02	-2.455	.221+01	.184-02	.291-05	.351-02	.221+01	.829-03	.829-03
-2.0	.345	-1.936	-3.936	.271+01	.116-01	-1.655	.271+01	.116-01	.116-03	.221-01	.221+01	.523-02	.523-02
-1.8	.345	-1.736	-3.536	.221+01	.184-01	-1.455	.221+01	.184-01	.291-03	.351-01	.221+01	.829-02	.829-02
-1.4	.345	-1.337	-2.737	.221+01	.461-01	-1.055	.221+01	.461-01	.183-02	.891-01	.221+01	.208-01	.208-01
-1.0	.343	-1.940	-1.940	.220+01	.115+00	-.657	.220+01	.115+00	.115-01	.220+00	.221+01	.521-01	.521-01
-.8	.340	-.745	-1.545	.219+01	.180+00	-.460	.219+01	.180+00	.285-01	.347+00	.220+01	.819-01	.819-01
-.6	.333	-.559	-1.159	.215+01	.276+00	-.267	.215+01	.276+00	.693-01	.541+00	.217+01	.127+00	.127+00
-.4	.316	-.391	-.791	.207+01	.406+00	-.084	.207+01	.406+00	.162+00	.825+00	.211+01	.194+00	.194+00
-.2	.235	-.261	-.461	.192+01	.549+00	.082	.192+01	.549+00	.346+00	.121+01	.199+01	.279+00	.279+00
.0	.225	-.186	-.188	.168+01	.649+00	.225	.168+01	.649+00	.649+00	.168+01	.180+01	.369+00	.369+00
.2	.152	-.176	.024	.142+01	.667+00	.352	.142+01	.667+00	.106+01	.225+01	.157+01	.439+00	.439+00
.4	.076	-.200	.200	.119+01	.631+00	.476	.119+01	.631+00	.158+01	.299+01	.135+01	.487+00	.487+00
.6	-.001	-.238	.362	.997+00	.578+00	.599	.997+00	.578+00	.230+01	.397+01	.115+01	.525+00	.525+00
.8	-.080	-.284	.516	.832+00	.520+00	.720	.832+00	.520+00	.328+01	.525+01	.981+00	.559+00	.559+00
1.0	-.162	-.333	.667	.688+00	.464+00	.838	.688+00	.464+00	.464+01	.688+01	.830+00	.593+00	.593+00
1.2	-.249	-.385	.815	.564+00	.412+00	.951	.564+00	.412+00	.653+01	.894+01	.698+00	.531+00	.531+00
1.4	-.342	-.437	.963	.455+00	.365+00	1.058	.455+00	.365+00	.918+01	.114+02	.583+00	.677+00	.677+00
1.6	-.446	-.490	1.110	.358+00	.324+00	1.154	.358+00	.324+00	.129+02	.143+02	.483+00	.735+00	.735+00
1.8	-.567	-.544	1.256	.271+00	.286+00	1.233	.271+00	.286+00	.180+02	.171+02	.394+00	.812+00	.812+00
2.0	-.718	-.606	1.394	.191+00	.248+00	1.282	.191+00	.248+00	.248+02	.191+02	.313+00	.914+00	.914+00
2.2	-.917	-.686	1.514	.121+00	.206+00	1.283	.121+00	.206+00	.326+02	.192+02	.239+00	.104+01	.104+01
2.4	-1.177	-.799	1.601	.666-01	.159+00	1.223	.666-01	.159+00	.399+02	.167+02	.172+00	.117+01	.117+01
2.6	-1.496	-.946	1.654	.319-01	.113+00	1.104	.319-01	.113+00	.450+02	.127+02	.118+00	.130+01	.130+01
2.8	-1.857	-1.121	1.679	.139-01	.758-01	.943	.139-01	.758-01	.478+02	.876+01	.770-01	.139+01	.139+01
3.0	-2.240	-1.309	1.691	.575-02	.491-01	.760	.575-02	.491-01	.491+02	.575+01	.494-01	.145+01	.145+01
3.4	-3.030	-1.702	1.698	.933-03	.198-01	.370	.933-03	.198-01	.499+02	.234+01	.199-01	.152+01	.152+01
3.8	-3.829	-2.101	1.699	.148-03	.792-02	-.029	.148-03	.792-02	.500+02	.936+00	.792-02	.155+01	.155+01
4.2	-4.628	-2.501	1.699	.235-04	.315-02	-.428	.235-04	.315-02	.500+02	.373+00	.315-02	.156+01	.156+01
4.6	-5.428	-2.901	1.699	.373-05	.126-02	-.828	.373-05	.126-02	.500+02	.148+00	.126-02	.157+01	.157+01
5.0	-6.228	-3.301	1.699	.591-06	.500-03	-1.228	.591-06	.500-03	.500+02	.591-01	.500-03	.157+01	.157+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² SUM(LI) JFR PHI
 .113-01 .221+01 .453+00 .199+03 2.241 .446 .914+04 1.1611 .231 2.853

N= 50 H*= .262

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	G1R	G2R	ETAR	ETA2/I
OMTI	ETAIR	ETA2R	ETAIR	G1R	G2R	ETAIR	ETA2R	G1R	G2R	G1R	G2R	ETAR	ETA2/I
-2.8	.350	-2.735	-5.535	-2.450	.224+01	.184-02	.224+01	.292-05	.355-02	.292-05	.355-02	.224+01	.821-03
-2.0	.350	-1.935	-3.935	-1.650	.224+01	.116-01	.224+01	.116-01	.224-01	.116-01	.224-01	.224+01	.518-02
-1.8	.350	-1.735	-3.535	-1.450	.224+01	.184-01	.224+01	.292-03	.355-01	.292-03	.355-01	.224+01	.821-02
-1.4	.350	-1.336	-2.736	-1.050	.224+01	.462-01	.224+01	.184-02	.891-01	.184-02	.891-01	.224+01	.206-01
-1.0	.348	-.939	-1.939	-.652	.223+01	.115+00	.223+01	.115-01	.223+00	.115-01	.223+00	.223+01	.516-01
-.8	.345	-.744	-1.544	-.455	.222+01	.180+00	.222+01	.285-01	.351+00	.285-01	.351+00	.222+01	.811-01
-.6	.338	-.558	-1.158	-.262	.218+01	.277+00	.218+01	.695-01	.547+00	.695-01	.547+00	.220+01	.126+00
-.4	.322	-.390	-.790	-.078	.210+01	.407+00	.210+01	.162+00	.835+00	.162+00	.835+00	.214+01	.192+00
-.2	.228	-.259	-.459	.088	.194+01	.550+00	.194+01	.347+00	.122+01	.347+00	.122+01	.202+01	.276+00
.0	.232	-.187	-.187	.232	.170+01	.651+00	.170+01	.651+00	.170+01	.651+00	.170+01	.182+01	.365+00
.2	.160	-.174	.076	.360	.144+01	.670+00	.144+01	.106+01	.229+01	.106+01	.229+01	.159+01	.435+00
.4	.084	-.197	.203	.484	.121+01	.635+00	.121+01	.160+01	.305+01	.160+01	.305+01	.137+01	.482+00
.6	.008	-.234	.366	.608	.102+01	.583+00	.102+01	.232+01	.406+01	.232+01	.406+01	.117+01	.519+00
.8	-.070	-.273	.521	.730	.852+00	.527+00	.852+00	.332+01	.538+01	.332+01	.538+01	.100+01	.553+00
1.0	-.151	-.327	.673	.849	.707+00	.471+00	.707+00	.471+01	.707+01	.471+01	.707+01	.850+00	.588+00
1.2	-.237	-.376	.824	.963	.590+00	.420+00	.590+00	.666+01	.919+01	.666+01	.919+01	.716+00	.627+00
1.4	-.330	-.427	.973	1.070	.468+00	.374+00	.468+00	.940+01	.118+02	.940+01	.118+02	.600+00	.674+00
1.6	-.434	-.477	1.123	1.166	.368+00	.333+00	.368+00	.133+02	.147+02	.133+02	.147+02	.497+00	.736+00
1.8	-.557	-.530	1.270	1.243	.277+00	.295+00	.277+00	.186+02	.175+02	.186+02	.175+02	.405+00	.817+00
2.0	-.713	-.591	1.409	1.287	.194+00	.256+00	.194+00	.256+02	.194+02	.256+02	.194+02	.321+00	.924+00
2.2	-.918	-.674	1.526	1.282	.121+00	.212+00	.121+00	.336+02	.191+02	.336+02	.191+02	.244+00	.105+01
2.4	-1.187	-.790	1.610	1.213	.650-01	.162+00	.650-01	.407+02	.163+02	.407+02	.163+02	.175+00	.119+01
2.6	-1.514	-.942	1.658	1.086	.306-01	.114+00	.306-01	.455+02	.122+02	.455+02	.122+02	.118+00	.131+01
2.8	-1.879	-1.118	1.682	.921	.132-01	.761-01	.132-01	.480+02	.834+01	.480+02	.834+01	.773-01	.140+01
3.0	-2.263	-1.308	1.692	.737	.545-02	.492-01	.545-02	.492+02	.545+01	.492+02	.545+01	.495-01	.146+01
3.4	-3.055	-1.702	1.698	.345	.882-03	.199-01	.882-03	.499+02	.222+01	.499+02	.222+01	.199-01	.153+01
3.8	-3.853	-2.101	1.699	-.053	.140-03	.792-02	.140-03	.500+02	.885+00	.500+02	.885+00	.792-02	.155+01
4.2	-4.653	-2.501	1.699	-.453	.222-04	.315-02	.222-04	.500+02	.352+00	.500+02	.352+00	.315-02	.156+01
4.6	-5.453	-2.901	1.699	-.853	.352-05	.126-02	.352-05	.500+02	.140+00	.500+02	.140+00	.126-02	.157+01
5.0	-6.253	-3.301	1.699	-1.253	.559-06	.500-03	.559-06	.500+02	.559-01	.500+02	.559-01	.500-03	.157+01

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)² JER PHI
 N= 50 H*= .30
 .123-01 .195+01 .514+00 .189+03 2.326 .430 .769+04 1.1684 .216 3.101

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2I	ETA2R	ETA2I
OMTI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA2R	ETA2I	ETA2R	ETA2I	ETA2I
-2.8	.367	-2.732	-5.532	-2.433	.233+01	.135-02	.293-05	.369-02	.233+01	.233+01	.796-03		
-2.0	.367	-1.932	-3.932	-1.633	.233+01	.117-01	.117-03	.233-01	.233+01	.233+01	.502-02		
-1.8	.367	-1.733	-3.533	-1.433	.233+01	.125-01	.293-03	.369-01	.233+01	.233+01	.796-02		
-1.4	.366	-1.333	-2.733	-1.034	.232+01	.465-01	.185-02	.925-01	.232+01	.232+01	.200-01		
-1.0	.365	-.936	-1.936	-.635	.232+01	.116+00	.116-01	.232+00	.232+01	.232+01	.500-01		
-.8	.362	-.742	-1.542	-.438	.230+01	.131+00	.287-01	.365+00	.231+01	.231+01	.726-01		
-.6	.355	-.555	-1.155	-.245	.226+01	.278+00	.699-01	.569+00	.228+01	.228+01	.122+00		
-.4	.339	-.387	-.787	-.061	.218+01	.410+00	.163-00	.869+00	.222+01	.222+01	.186+00		
-.2	.306	-.256	-.456	.106	.203+01	.555+00	.350+00	.129+01	.210+01	.210+01	.267+00		
.0	.252	-.182	-.182	.252	.179+01	.658+00	.658+00	.179+01	.191+01	.191+01	.352+00		
.2	.183	-.167	.033	.343	.153+01	.680+00	.108+01	.242+01	.167+01	.167+01	.419+00		
.4	.111	-.188	.212	.511	.129+01	.648+00	.163+01	.325+01	.145+01	.145+01	.465+00		
.6	.039	-.222	.378	.639	.109+01	.599+00	.239+01	.436+01	.125+01	.125+01	.501+00		
.8	-.036	-.262	.538	.764	.921+00	.547+00	.345+01	.581+01	.107+01	.107+01	.536+00		
1.0	-.114	-.305	.695	.886	.769+00	.495+00	.495+01	.769+01	.915+00	.915+00	.572+00		
1.2	-.197	-.349	.851	1.003	.635+00	.448+00	.710+01	.101+02	.777+00	.777+00	.615+00		
1.4	-.290	-.392	1.006	1.110	.513+00	.406+00	.102+02	.129+02	.654+00	.654+00	.669+00		
1.6	-.396	-.435	1.165	1.204	.402+00	.367+00	.146+02	.160+02	.544+00	.544+00	.740+00		
1.8	-.527	-.483	1.317	1.273	.297+00	.329+00	.208+02	.187+02	.443+00	.443+00	.837+00		
2.0	-.699	-.545	1.455	1.301	.200+00	.245+00	.285+02	.200+02	.348+00	.348+00	.960+00		
2.2	-.931	-.637	1.563	1.269	.117+00	.231+00	.366+02	.186+02	.259+00	.259+00	.110+01		
2.4	-1.226	-.767	1.633	1.174	.594-01	.171+00	.430+02	.149+02	.181+00	.181+00	.124+01		
2.6	-1.572	-.930	1.670	1.028	.268-01	.117+00	.468+02	.107+02	.120+00	.120+00	.135+01		
2.8	-1.948	-1.113	1.687	.852	.113-01	.771-01	.486+02	.712+01	.779-01	.779-01	.143+01		
3.0	-2.337	-1.306	1.694	.663	.460-02	.494-01	.494+02	.460+01	.497-01	.497-01	.148+01		
3.4	-3.132	-1.702	1.698	.268	.739-03	.199-01	.499+02	.186+01	.199-01	.199-01	.153+01		
3.8	-3.931	-2.101	1.699	-.131	.117-03	.792-02	.500+02	.740+00	.792-02	.792-02	.156+01		
4.2	-4.731	-2.501	1.699	-.531	.186-04	.315-02	.500+02	.295+00	.315-02	.315-02	.156+01		
4.6	-5.530	-2.901	1.699	-.930	.295-05	.126-02	.500+02	.117+00	.126-02	.126-02	.157+01		
5.0	-6.330	-3.301	1.699	-1.330	.467-06	.500-03	.500+02	.467-01	.500-03	.500-03	.157+01		

EXACT ZIMM EIGENVALUES										N=100 H=.05				FHI	
LI	LN	LOG	1/(LN)	SUM	RECIP	SUM	ROCAL	(1/LP)2	SUM	SUM(L1	JER	335	1.123	-23	
				1/(LP)		1.821	.549	.450+06	1.1099						
				.116+04											
				.273+00											
				.366+01											
				.157-02											
REDUCED DYNAMIC VISCOSITY AND MODULUS															
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETA2R	ETA2R	GIR	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.250	-2.735	-5.555	-2.540	.182+01	.176-02	.279-05	.289-02	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01
-2.0	.260	-1.955	-3.955	-1.740	.192+01	.111-01	.111-03	.182-01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01
-1.8	.260	-1.755	-3.555	-1.540	.182+01	.176-01	.279-03	.289-01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01
-1.4	.260	-1.355	-2.755	-1.140	.192+01	.441-01	.176-02	.724-01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01	.182+01
-1.0	.258	-.959	-1.959	-.742	.191+01	.110+00	.110-01	.181+00	.181+01	.181+01	.181+01	.181+01	.181+01	.181+01	.181+01
-.8	.254	-.764	-1.564	-.546	.180+01	.172+00	.273-01	.285+00	.180+01	.180+01	.180+01	.180+01	.180+01	.180+01	.180+01
-.6	.245	-.579	-1.179	-.355	.176+01	.264+00	.663-01	.442+00	.178+01	.178+01	.178+01	.178+01	.178+01	.178+01	.178+01
-.4	.225	-.412	-.812	-.175	.168+01	.397+00	.154+00	.669+00	.172+01	.172+01	.172+01	.172+01	.172+01	.172+01	.172+01
-.2	.184	-.285	-.485	-.016	.153+01	.519+00	.327+00	.963+00	.161+01	.161+01	.161+01	.161+01	.161+01	.161+01	.161+01
.0	.113	-.219	-.219	.113	.170+01	.604+00	.604+00	.130+01	.143+01	.143+01	.143+01	.143+01	.143+01	.143+01	.143+01
.2	.022	-.213	-.019	.222	.105+01	.603+00	.956+00	.167+01	.121+01	.121+01	.121+01	.121+01	.121+01	.121+01	.121+01
.4	-.073	-.261	.139	.327	.846+00	.549+00	.138+01	.213+01	.101+01	.101+01	.101+01	.101+01	.101+01	.101+01	.101+01
.6	-.165	-.318	.282	.435	.683+00	.481+00	.191+01	.272+01	.836+00	.836+00	.836+00	.836+00	.836+00	.836+00	.836+00
.8	-.259	-.384	.416	.541	.551+00	.413+00	.261+01	.349+01	.689+00	.689+00	.689+00	.689+00	.689+00	.689+00	.689+00
1.0	-.353	-.456	.544	.647	.443+00	.350+00	.350+01	.443+01	.565+00	.565+00	.565+00	.565+00	.565+00	.565+00	.565+00
1.2	-.449	-.533	.667	.751	.356+00	.293+00	.464+01	.564+01	.461+00	.461+00	.461+00	.461+00	.461+00	.461+00	.461+00
1.4	-.545	-.614	.786	.855	.295+00	.243+00	.611+01	.716+01	.375+00	.375+00	.375+00	.375+00	.375+00	.375+00	.375+00
1.6	-.643	-.697	.903	.957	.228+00	.201+00	.800+01	.907+01	.304+00	.304+00	.304+00	.304+00	.304+00	.304+00	.304+00
1.8	-.742	-.782	1.018	1.058	.181+00	.155+00	.104+02	.114+02	.245+00	.245+00	.245+00	.245+00	.245+00	.245+00	.245+00
2.0	-.843	-.867	1.133	1.157	.144+00	.136+00	.136+02	.144+02	.198+00	.198+00	.198+00	.198+00	.198+00	.198+00	.198+00
2.2	-.946	-.953	1.247	1.254	.113+00	.111+00	.177+02	.179+02	.159+00	.159+00	.159+00	.159+00	.159+00	.159+00	.159+00
2.4	-1.055	-1.038	1.362	1.345	.882-01	.917-01	.230+02	.221+02	.127+00	.127+00	.127+00	.127+00	.127+00	.127+00	.127+00
2.6	-1.171	-1.121	1.479	1.429	.675-01	.757-01	.301+02	.269+02	.101+00	.101+00	.101+00	.101+00	.101+00	.101+00	.101+00
2.8	-1.300	-1.203	1.597	1.500	.501-01	.627-01	.395+02	.316+02	.802-01	.802-01	.802-01	.802-01	.802-01	.802-01	.802-01
3.0	-1.454	-1.287	1.713	1.546	.352-01	.516-01	.516+02	.352+02	.625-01	.625-01	.625-01	.625-01	.625-01	.625-01	.625-01
3.4	-1.897	-1.500	1.900	1.503	.127-01	.316-01	.794+02	.318+02	.340-01	.340-01	.340-01	.340-01	.340-01	.340-01	.340-01
3.8	-2.561	-1.821	1.979	1.239	.275-02	.151-01	.953+02	.173+02	.153-01	.153-01	.153-01	.153-01	.153-01	.153-01	.153-01
4.2	-3.333	-2.204	1.996	.867	.465-03	.626-02	.992+02	.737+01	.628-02	.628-02	.628-02	.628-02	.628-02	.628-02	.628-02
4.6	-4.128	-2.601	1.999	.472	.745-04	.251-02	.999+02	.297+01	.251-02	.251-02	.251-02	.251-02	.251-02	.251-02	.251-02
5.0	-4.927	-3.000	2.000	.073	.118-04	.100-02	.100+03	.118+01	.100-02	.100-02	.100-02	.100-02	.100-02	.100-02	.100-02

EXACT ZIMM EIGENVALUES
LI LN 1/(LN)

[illegible]

REDUCED CYNATIC VISCOSITY AND MODULUS

[illegible]

EXACT ZIMP EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) RECIP SUM SUM(L1) JER PHI
 -276-02 .297+01 .336+00 .749+03 2.064 .484 .150+06 1.1401 .268 2.175

REDUCED DYNAMIC VISCOSITY AND MODULUS										N=100 H=.15			
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	SUM	SUM(L1)	JER	PHI
OMTI	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	ARCTAN		
-2.8	.315	-2.743	-5.543	-2.485	.206+01	.181-02	.286-05	.327-02	.206+01	.875-03			
-2.0	.315	-1.943	-3.943	-1.685	.206+01	.114-01	.114-03	.206-01	.206+01	.552-02			
-1.8	.315	-1.743	-3.543	-1.485	.206+01	.121-01	.286-03	.327-01	.206+01	.875-02			
-1.4	.314	-1.344	-2.744	-1.085	.206+01	.453-01	.180-02	.821-01	.206+01	.220-01			
-1.0	.313	-.947	-1.947	-.687	.205+01	.113+00	.113-01	.205+00	.206+01	.551-01			
-.8	.309	-.753	-1.553	-.491	.204+01	.177+00	.280-01	.323+00	.205+01	.865-01			
-.6	.302	-.567	-1.167	-.298	.200+01	.271+00	.682-01	.503+00	.202+01	.135+00			
-.4	.284	-.393	-.799	-.116	.192+01	.399+00	.159+00	.765+00	.196+01	.205+00			
-.2	.247	-.270	-.470	.047	.177+01	.537+00	.339+00	.111+01	.185+01	.295+00			
.0	.186	-.200	-.200	.186	.153+01	.631+00	.631+00	.153+01	.166+01	.391+00			
.2	.107	-.192	.008	.307	.128+01	.642+00	.102+01	.203+01	.143+01	.466+00			
.4	.024	-.223	.177	.424	.106+01	.598+00	.150+01	.266+01	.122+01	.515+00			
.6	-.058	-.269	.331	.547	.876+00	.538+00	.214+01	.349+01	.103+01	.551+00			
.8	-.141	-.324	.476	.659	.723+00	.474+00	.299+01	.456+01	.865+00	.580+00			
1.0	-.225	-.385	.615	.775	.595+00	.412+00	.412+01	.595+01	.724+00	.606+00			
1.2	-.401	-.450	.750	.888	.497+00	.355+00	.562+01	.773+01	.603+00	.629+00			
1.4	-.492	-.518	.882	.999	.397+00	.303+00	.762+01	.998+01	.500+00	.652+00			
1.6	-.587	-.583	1.012	1.108	.322+00	.258+00	.103+02	.128+02	.413+00	.676+00			
1.8	-.687	-.660	1.140	1.213	.259+00	.219+00	.138+02	.163+02	.339+00	.702+00			
2.0	-.794	-.731	1.269	1.313	.206+00	.186+00	.186+02	.206+02	.277+00	.735+00			
2.2	-.873	-.802	1.398	1.406	.161+00	.158+00	.250+02	.255+02	.225+00	.776+00			
2.4	-.914	-.873	1.527	1.486	.122+00	.114+00	.337+02	.306+02	.181+00	.832+00			
2.6	-1.054	-.946	1.654	1.546	.893-01	.113+00	.451+02	.352+02	.144+00	.909+00			
2.8	-1.229	-1.028	1.772	1.571	.590-01	.978-01	.592+02	.372+02	.111+00	.101+01			
3.0	-1.458	-1.131	1.869	1.547	.349-01	.740-01	.740+02	.349+02	.818-01	.113+01			
3.4	-2.029	-1.429	1.971	1.311	.814-02	.372-01	.935+02	.205+02	.381-01	.136+01			
3.8	-2.851	-1.805	1.995	.949	.141-02	.157-01	.989+02	.890+01	.157-01	.148+01			
4.2	-3.644	-2.201	1.999	.556	.227-03	.630-02	.998+02	.360+01	.630-02	.153+01			
4.6	-4.443	-2.600	2.000	.157	.361-04	.251-02	.100+03	.144+01	.251-02	.156+01			
5.0	-5.243	-3.000	2.000	-.243	.572-05	.100-02	.100+03	.572+00	.100-02	.157+01			

#1250

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 PHI
 .406-02 .221+01 .453+00 .562+03 2.285 .438 .702+05 1.1589 .222 2.852

N=100 H*=.262

REDUCED DYNAMIC VISCOSITY AND MODULUS										MCD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2/1	ETA2/1
OMTI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA2R	ETA2R	ETA2R	ETA2/1	ETA2/1
-2.8	.359	-2.736	-5.536	-2.441	.229+01	.184-02	.291-05	.362-02	.229+01	.229+01	.229+01	.804-03	.804-03
-2.0	.359	-1.936	-3.936	-1.641	.229+01	.116-01	.116-03	.229-01	.229+01	.229+01	.229+01	.507-02	.507-02
-1.8	.359	-1.736	-3.536	-1.441	.228+01	.184-01	.291-03	.362-01	.228+01	.228+01	.228+01	.804-02	.804-02
-1.4	.359	-1.337	-2.737	-1.041	.228+01	.461-01	.183-02	.909-01	.228+01	.228+01	.228+01	.202-01	.202-01
-1.0	.357	-.940	-1.940	-.643	.227+01	.115+00	.115-01	.227+00	.228+01	.228+01	.228+01	.505-01	.505-01
-.8	.354	-.745	-1.545	-.446	.226+01	.190+00	.285-01	.358+00	.227+01	.227+01	.227+01	.194-01	.194-01
-.6	.347	-.559	-1.159	-.253	.222+01	.276+00	.693-01	.558+00	.224+01	.224+01	.224+01	.124+00	.124+00
-.4	.331	-.391	-.791	-.069	.214+01	.406+00	.162+00	.853+00	.218+01	.218+01	.218+01	.187+00	.187+00
-.2	.298	-.261	-.461	.098	.199+01	.549+00	.346+00	.125+01	.206+01	.206+01	.206+01	.270+00	.270+00
.0	.243	-.188	-.188	.243	.175+01	.649+00	.649+00	.175+01	.187+01	.187+01	.187+01	.355+00	.355+00
.2	.173	-.176	.024	.373	.149+01	.667+00	.106+01	.236+01	.163+01	.163+01	.163+01	.421+00	.421+00
.4	.100	-.200	.200	.500	.126+01	.631+00	.158+01	.317+01	.141+01	.141+01	.141+01	.464+00	.464+00
.6	.028	-.239	.361	.628	.107+01	.577+00	.230+01	.425+01	.121+01	.121+01	.121+01	.496+00	.496+00
.8	-.045	-.285	.515	.755	.901+00	.519+00	.327+01	.569+01	.104+01	.104+01	.104+01	.523+00	.523+00
1.0	-.120	-.336	.664	.880	.758+00	.462+00	.462+01	.758+01	.888+00	.888+00	.888+00	.547+00	.547+00
1.2	-.198	-.389	.811	1.002	.635+00	.408+00	.647+01	.101+02	.755+00	.755+00	.755+00	.572+00	.572+00
1.4	-.278	-.444	.956	1.122	.527+00	.360+00	.904+01	.132+02	.639+00	.639+00	.639+00	.599+00	.599+00
1.6	-.362	-.498	1.102	1.238	.434+00	.317+00	.126+02	.173+02	.538+00	.538+00	.538+00	.631+00	.631+00
1.8	-.453	-.552	1.248	1.347	.352+00	.290+00	.177+02	.222+02	.450+00	.450+00	.450+00	.672+00	.672+00
2.0	-.554	-.605	1.395	1.446	.279+00	.248+00	.248+02	.279+02	.373+00	.373+00	.373+00	.727+00	.727+00
2.2	-.672	-.659	1.541	1.528	.213+00	.220+00	.348+02	.337+02	.306+00	.306+00	.306+00	.801+00	.801+00
2.4	-.819	-.718	1.682	1.581	.152+00	.191+00	.481+02	.381+02	.244+00	.244+00	.244+00	.901+00	.901+00
2.6	-1.012	-.795	1.805	1.598	.972-01	.160+00	.638+02	.387+02	.187+00	.187+00	.187+00	.103+01	.103+01
2.8	-1.267	-.904	1.896	1.533	.541-01	.125+00	.787+02	.341+02	.136+00	.136+00	.136+00	.116+01	.116+01
3.0	-1.582	-1.049	1.951	1.418	.262-01	.894-01	.894+02	.262+02	.931-01	.931-01	.931-01	.129+01	.129+01
3.4	-2.322	-1.409	1.991	1.078	.477-02	.390-01	.980+02	.120+02	.393-01	.393-01	.393-01	.145+01	.145+01
3.8	-3.111	-1.801	1.999	.689	.774-03	.158-01	.997+02	.489+01	.158-01	.158-01	.158-01	.152+01	.152+01
4.2	-3.909	-2.200	2.000	.291	.123-03	.631-02	.999+02	.195+01	.631-02	.631-02	.631-02	.155+01	.155+01
4.6	-4.709	-2.600	2.000	-.109	.195-04	.251-02	.100+03	.778+00	.251-02	.251-02	.251-02	.156+01	.156+01
5.0	-5.509	-3.000	2.000	-.509	.310-05	.100-02	.100+03	.310+00	.100-02	.100-02	.100-02	.157+01	.157+01

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM (L1) JER PHI
 .450-02 .195+01 .514+00 .524+03 2.360 .424 .574+05 1.1636 .209 3.044

N=100 M=30

REDUCED DYNAMIC VISCOSITY AND MODULUS									
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	FTAIR	ETA2R	G1R	ETAIR	ETA2R	G1R	G2R	ETAR	ARCTAN
-2.8	.373	-2.734	-5.534	-2.427	.236+01	.184-02	.292-05	.374-02	.236+01
-2.0	.373	-1.934	-3.934	-1.627	.236+01	.116-01	.116-03	.236-01	.236+01
-1.8	.373	-1.734	-3.534	-1.427	.236+01	.184-01	.292-03	.374-01	.236+01
-1.4	.373	-1.335	-2.735	-1.027	.236+01	.463-01	.184-02	.939-01	.236+01
-1.0	.371	-.938	-1.938	-.629	.235+01	.115+00	.115-01	.235+00	.235+01
-.8	.368	-.744	-1.544	-.432	.233+01	.180+00	.286-01	.370+00	.234+01
-.6	.361	-.557	-1.157	-.239	.230+01	.277+00	.696-01	.577+00	.231+01
-.4	.346	-.389	-.789	-.054	.222+01	.408+00	.162+00	.883+00	.225+01
-.2	.314	-.258	-.458	.114	.206+01	.552+00	.348+00	.130+01	.213+01
.0	.261	-.185	-.185	.261	.182+01	.653+00	.653+00	.182+01	.194+01
.2	.194	-.172	.078	.394	.156+01	.674+00	.107+01	.248+01	.170+01
.4	.124	-.194	.206	.524	.133+01	.639+00	.161+01	.334+01	.148+01
.6	.055	-.231	.369	.655	.113+01	.598+00	.234+01	.452+01	.128+01
.8	-.015	-.274	.526	.785	.956+00	.532+00	.336+01	.609+01	.110+01
1.0	-.087	-.322	.678	.913	.819+00	.477+00	.477+01	.819+01	.947+01
1.2	-.161	-.371	.829	1.039	.691+00	.426+00	.675+01	.109+02	.811+01
1.4	-.238	-.420	.940	1.162	.578+00	.380+00	.954+01	.145+02	.692+00
1.6	-.320	-.469	1.131	1.280	.478+00	.340+00	.135+02	.190+02	.587+00
1.8	-.410	-.516	1.284	1.390	.389+00	.305+00	.193+02	.245+02	.494+00
2.0	-.513	-.561	1.439	1.497	.307+00	.275+00	.275+02	.307+02	.412+00
2.2	-.638	-.608	1.592	1.562	.230+00	.246+00	.390+02	.365+02	.337+00
2.4	-.801	-.668	1.732	1.599	.158+00	.215+00	.540+02	.397+02	.267+00
2.6	-1.020	-.753	1.847	1.580	.956-01	.177+00	.703+02	.381+02	.201+00
2.8	-1.303	-.876	1.924	1.497	.497-01	.133+00	.839+02	.314+02	.142+00
3.0	-1.641	-1.034	1.966	1.359	.228-01	.925-01	.925+02	.228+02	.952-01
3.4	-2.401	-1.406	1.994	.999	.397-02	.193-01	.987+02	.998+01	.395-01
3.6	3.194	-1.801	1.999	.606	.640-03	.158-01	.998+02	.404+01	.158-01
4.2	3.993	-2.200	2.000	.207	.102-03	.631-02	.100+03	.161+01	.631-02
4.6	4.792	-2.600	2.000	-.192	.161-04	.251-02	.100+03	.642+00	.251-02
5.0	5.592	-3.000	2.000	-.592	.256-05	.100-02	.100+03	.256+00	.100-02

EXACT ZIMM EIGENVALUES										N=200 H*= .05				PHI	
LI	LN	1/(LN)	SUM 1/(LP)	SUM L1/LP	RECIP ROCAL	SUM GIR	SUM G2R	MOD ETAR	ARCTAN ETA2/1						
LOG OMTI	LOG ETAIR	LOG ETA2R	LOG GIR	LOG G2R	MOD ETA2R	MOD GIR	MOD G2R	MOD ETAR	MOD ARCTAN						
-2.8	.271	-2.752	-5.552	-2.529	.187+01	.177-02	.280-05	.296-02	.187+01	.948-03					
-2.0	.271	-1.952	-3.952	-1.729	.187+01	.112-01	.112-03	.137-01	.187+01	.598-02					
-1.8	.271	-1.753	-3.553	-1.529	.187+01	.177-01	.280-03	.296-01	.187+01	.948-02					
-1.4	.270	-1.353	-2.753	-1.130	.186+01	.444-01	.177-02	.742-01	.186+01	.238-01					
-1.0	.268	-.956	-1.956	-.732	.186+01	.111+00	.111-01	.186+00	.186+01	.595-01					
-.8	.265	-.762	-1.562	-.535	.184+01	.173+00	.274-01	.292+00	.185+01	.937-01					
-.6	.256	-.576	-1.176	-.344	.180+01	.265+00	.666-01	.453+00	.182+01	.146+00					
-.4	.237	-.410	-.810	-.163	.172+01	.389+00	.155+00	.687+00	.177+01	.222+00					
-.2	.196	-.282	-.482	-.004	.157+01	.523+00	.330+00	.991+00	.165+01	.321+00					
.0	.127	-.215	-.215	.127	.134+01	.609+00	.609+00	.134+01	.147+01	.427+00					
.2	.039	-.214	-.014	.239	.109+01	.611+00	.968+00	.173+01	.125+01	.510+00					
.4	-.053	-.253	.147	.347	.885+00	.558+00	.140+01	.222+01	.105+01	.563+00					
.6	-.144	-.309	.291	.456	.718+00	.491+00	.196+01	.286+01	.870+00	.600+00					
.8	-.235	-.372	.428	.565	.582+00	.424+00	.258+01	.367+01	.720+00	.630+00					
1.0	-.327	-.443	.557	.673	.471+00	.361+00	.361+01	.471+01	.593+00	.654+00					
1.2	-.421	-.519	.681	.779	.380+00	.303+00	.480+01	.602+01	.486+00	.674+00					
1.4	-.515	-.598	.802	.885	.306+00	.252+00	.634+01	.768+01	.396+00	.690+00					
1.6	-.610	-.680	.920	.990	.246+00	.209+00	.831+01	.978+01	.322+00	.705+00					
1.8	-.705	-.765	1.035	1.095	.197+00	.172+00	.108+02	.124+02	.261+00	.717+00					
2.0	-.802	-.851	1.149	1.198	.158+00	.141+00	.141+02	.158+02	.211+00	.730+00					
2.2	-.901	-.938	1.262	1.299	.126+00	.115+00	.183+02	.199+02	.171+00	.742+00					
2.4	-1.000	-1.026	1.374	1.400	.999-01	.942-01	.237+02	.251+02	.137+00	.756+00					
2.6	-1.102	-1.114	1.486	1.498	.790-01	.770-01	.306+02	.315+02	.110+00	.772+00					
2.8	-1.208	-1.200	1.600	1.592	.620-01	.630-01	.398+02	.391+02	.884-01	.794+00					
3.0	-1.319	-1.286	1.714	1.681	.480-01	.518-01	.518+02	.480+02	.706-01	.823+00					
3.4	-1.577	-1.452	1.948	1.823	.265-01	.353-01	.887+02	.665+02	.441-01	.927+00					
3.8	-1.960	-1.643	2.157	1.840	.110-01	.227-01	.143+03	.691+02	.252-01	.112+01					
4.2	-2.567	-1.933	2.267	1.633	.271-02	.117-01	.185+03	.430+02	.120-01	.134+01					
4.6	-3.320	-2.305	2.295	1.280	.479-03	.496-02	.197+03	.191+02	.498-02	.147+01					
5.0	-4.111	-2.700	2.300	.889	.774-04	.200-02	.200+03	.774+01	.200-02	.153+01					

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP ROCAL SUM (1/LP)2 /LP)2 SUM(11 JER PHI
 .479-03 .366+01 .273+00 .390+04 1.866 .536 .487+07 1.1157 .321 1.334

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM SUM(L1 JER PHI
 .594-03 .349+01 .287+00 .327+04 1.941 .515 .319+07 1.1251 .299 1.677

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON				ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	G1R	G2R	ETAR	ETA2/1	
OMTI	ETAIR	ETA2R	G1R	ETAIR	ETA2R	G2R	ETAIR	ETA2R	G1R	G2R	ETAR	ETA2/1			
-2.8	.288	-2.749	-5.549	-2.512	.194+01	.178-02	.283-05	.308-02	.194+01	.194+01	.194+01	.194+01	.194+01	.194+01	.919-03
-2.0	.288	-1.949	-3.949	-1.712	.194+01	.113-01	.113-03	.194-01	.113-03	.194-01	.194+01	.194+01	.194+01	.194+01	.580-02
-1.8	.288	-1.749	-3.549	-1.512	.194+01	.178-01	.283-03	.308-01	.194+01	.194+01	.194+01	.194+01	.194+01	.194+01	.919-02
-1.4	.238	-1.349	-2.749	-1.112	.194+01	.447-01	.178-02	.772-01	.194+01	.194+01	.194+01	.194+01	.194+01	.194+01	.231-01
-1.0	.286	-.953	-1.953	-.714	.193+01	.112+00	.112-01	.193+00	.193+01	.193+01	.193+01	.193+01	.193+01	.193+01	.577-01
-.8	.282	-.758	-1.558	-.518	.192+01	.174+00	.276-01	.304+00	.192+01	.192+01	.192+01	.192+01	.192+01	.192+01	.908-01
-.6	.274	-.573	-1.173	-.326	.188+01	.268+00	.672-01	.472+00	.190+01	.190+01	.190+01	.190+01	.190+01	.190+01	.141+00
-.4	.255	-.406	-.806	-.145	.180+01	.393+00	.156+00	.716+00	.184+01	.184+01	.184+01	.184+01	.184+01	.184+01	.215+00
-.2	.216	-.277	-.477	.016	.164+01	.528+00	.333+00	.104+01	.173+01	.173+01	.173+01	.173+01	.173+01	.173+01	.311+00
.0	.150	-.209	-.209	.150	.141+01	.618+00	.618+00	.141+01	.154+01	.154+01	.154+01	.154+01	.154+01	.154+01	.412+00
.2	.066	-.205	-.005	.266	.116+01	.623+00	.988+00	.184+01	.132+01	.132+01	.132+01	.132+01	.132+01	.132+01	.492+00
.4	-.022	-.241	.159	.378	.950+00	.574+00	.144+01	.239+01	.111+01	.111+01	.111+01	.111+01	.111+01	.111+01	.543+00
.6	-.109	-.293	.307	.491	.777+00	.509+00	.203+01	.309+01	.929+00	.929+00	.929+00	.929+00	.929+00	.929+00	.580+00
.8	-.197	-.354	.446	.603	.635+00	.443+00	.280+01	.401+01	.774+00	.774+00	.774+00	.774+00	.774+00	.774+00	.609+00
1.0	-.286	-.421	.579	.714	.517+00	.380+00	.380+01	.517+01	.641+00	.641+00	.641+00	.641+00	.641+00	.641+00	.633+00
1.2	-.377	-.493	.707	.823	.420+00	.322+00	.510+01	.666+01	.529+00	.529+00	.529+00	.529+00	.529+00	.529+00	.653+00
1.4	-.468	-.569	.831	.932	.340+00	.270+00	.678+01	.855+01	.434+00	.434+00	.434+00	.434+00	.434+00	.434+00	.671+00
1.6	-.561	-.647	.953	1.079	.275+00	.225+00	.897+01	.109+02	.355+00	.355+00	.355+00	.355+00	.355+00	.355+00	.686+00
1.8	-.655	-.728	1.072	1.145	.221+00	.187+00	.118+02	.140+02	.290+00	.290+00	.290+00	.290+00	.290+00	.290+00	.701+00
2.0	-.750	-.811	1.189	1.250	.178+00	.155+00	.155+02	.178+02	.236+00	.236+00	.236+00	.236+00	.236+00	.236+00	.715+00
2.2	-.847	-.895	1.305	1.353	.142+00	.127+00	.202+02	.225+02	.191+00	.191+00	.191+00	.191+00	.191+00	.191+00	.730+00
2.4	-.946	-.979	1.421	1.454	.113+00	.105+00	.264+02	.284+02	.154+00	.154+00	.154+00	.154+00	.154+00	.154+00	.747+00
2.6	-1.048	-1.063	1.537	1.552	.895-01	.865-01	.344+02	.356+02	.124+00	.124+00	.124+00	.124+00	.124+00	.124+00	.768+00
2.8	-1.155	-1.146	1.654	1.645	.699-01	.715-01	.451+02	.441+02	.100+00	.100+00	.100+00	.100+00	.100+00	.100+00	.796+00
3.0	-1.270	-1.227	1.773	1.730	.537-01	.592-01	.592+02	.537+02	.799-01	.799-01	.799-01	.799-01	.799-01	.799-01	.834+00
3.2	-1.551	-1.391	2.009	1.849	.281-01	.407-01	.102+03	.707+02	.495-01	.495-01	.495-01	.495-01	.495-01	.495-01	.966+00
3.4	-1.993	-1.601	2.199	1.807	.102-01	.251-01	.158+03	.642+02	.271-01	.271-01	.271-01	.271-01	.271-01	.271-01	.119+01
3.6	-2.656	-1.920	2.280	1.544	.221-02	.120-01	.190+03	.350+02	.122-01	.122-01	.122-01	.122-01	.122-01	.122-01	.139+01
3.8	-3.426	-2.303	2.297	1.174	.375-03	.498-02	.198+03	.149+02	.500-02	.500-02	.500-02	.500-02	.500-02	.500-02	.150+01
4.0	-4.222	-2.700	2.300	.778	.600-04	.200-02	.200+03	.600+01	.200-02	.200-02	.200-02	.200-02	.200-02	.200-02	.154+01

[illegible]

-75-

#1250

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 PHI
 .941-03 .297+01 .336+00 .225+04 2.115 .473 .129+07 1.1435 .256 2.308
 N=200 H*= .15

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2/1	ETA2R	ETA2/1
OMTI	ETA2R	GIR	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	ETA2R	G2R	ETA2R	ETA2R	ETA2/1
-2.8	.325	-2.742	-5.542	-2.475	.212+01	.181-02	.287-05	.335-07	.212+01	.857-03			
-2.0	.325	-1.942	-3.942	-1.675	.212+01	.114-01	.114-03	.212-01	.212+01	.541-02			
-1.8	.325	-1.742	-3.542	-1.475	.211+01	.181-01	.287-03	.335-01	.212+01	.857-02			
-1.4	.325	-1.342	-2.742	-1.075	.211+01	.455-01	.181-02	.841-01	.211+01	.215-01			
-1.0	.323	-.946	-1.946	-.677	.210+01	.113+00	.113-01	.210+00	.211+01	.538-01			
-.8	.320	-.751	-1.551	-.480	.209+01	.177+00	.281-01	.331+00	.210+01	.846-01			
-.6	.313	-.565	-1.165	-.287	.205+01	.272+00	.684-01	.516+00	.207+01	.132+00			
-.4	.295	-.398	-.798	-.105	.197+01	.400+00	.159+00	.785+00	.201+01	.200+00			
-.2	.259	-.268	-.468	.059	.182+01	.539+00	.340+00	.115+01	.190+01	.289+00			
.0	.199	-.198	-.198	.199	.158+01	.635+00	.635+00	.158+01	.171+01	.381+00			
.2	.123	-.189	.011	.323	.133+01	.647+00	.103+01	.210+01	.148+01	.454+00			
.4	.043	-.219	.181	.443	.111+01	.604+00	.152+01	.278+01	.126+01	.500+00			
.6	-.036	-.264	.336	.564	.921+00	.545+00	.217+01	.367+01	.107+01	.534+00			
.8	-.116	-.317	.483	.684	.766+00	.482+00	.304+01	.483+01	.905+00	.561+00			
1.0	-.197	-.377	.623	.803	.635+00	.420+00	.420+01	.635+01	.762+00	.594+00			
1.2	-.280	-.441	.759	.920	.525+00	.362+00	.574+01	.832+01	.638+00	.604+00			
1.4	-.364	-.508	.892	1.036	.432+00	.310+00	.779+01	.103+02	.532+00	.622+00			
1.6	-.450	-.578	1.022	1.150	.355+00	.264+00	.105+02	.141+02	.442+00	.640+00			
1.8	-.538	-.650	1.150	1.262	.290+00	.224+00	.141+02	.183+02	.366+00	.658+00			
2.0	-.629	-.723	1.277	1.371	.235+00	.189+00	.199+02	.235+02	.302+00	.678+00			
2.2	-.722	-.796	1.404	1.478	.190+00	.160+00	.253+02	.300+02	.248+00	.701+00			
2.4	-.820	-.870	1.530	1.580	.151+00	.135+00	.339+02	.380+02	.203+00	.729+00			
2.6	-.924	-.942	1.658	1.676	.119+00	.114+00	.455+02	.474+02	.165+00	.765+00			
2.8	-1.039	-1.014	1.786	1.761	.914-01	.969-01	.611+02	.577+02	.133+00	.814+00			
3.0	-1.171	-1.086	1.914	1.829	.675-01	.820-01	.820+02	.675+02	.106+00	.882+00			
3.4	-1.541	-1.259	2.141	1.859	.288-01	.551-01	.138+03	.723+02	.622-01	.109+01			
3.8	-2.137	-1.538	2.262	1.663	.730-02	.290-01	.183+03	.461+02	.299-01	.132+01			
4.2	-2.886	-1.906	2.294	1.314	.130-02	.124-01	.197+03	.206+02	.125-01	.147+01			
4.6	-3.677	-2.300	2.300	.923	.211-03	.501-02	.199+03	.838+01	.502-02	.153+01			
5.0	-4.475	-2.699	2.301	.525	.335-04	.200-02	.200+03	.335+01	.200-02	.155+01			

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIPI (1/LP)2 SUM (1/LP)2 JER PHI
 .140-02 .229+01 .437+00 .164+04 2.294 .436 .591+06 1.1565 .220 2.806

N=200 H=.25

REDUCED DYNAMIC VISCOSITY		AND		MODULUS		MC		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R
-2.8	.361	-2.737	-5.537	-2.439	.183-02	.291-05	.364-02	.229+01	.799-03
-2.0	.361	-1.937	-3.537	-1.639	.116-01	.116-03	.229-01	.229+01	.504-02
-1.8	.361	-1.737	-3.537	-1.439	.183-01	.290-03	.364-01	.229+01	.799-02
-1.4	.350	-1.337	-2.737	-1.040	.460-01	.183-02	.913-01	.229+01	.201-01
-1.0	.359	-.941	-1.941	-.641	.115+00	.115-01	.228+00	.229+01	.502-01
-.8	.356	-.746	-1.546	-.444	.179+00	.284-01	.360+00	.228+01	.789-01
-.6	.349	-.560	-1.160	-.251	.275+00	.692-01	.561+00	.225+01	.123+00
-.4	.333	-.392	-.792	-.067	.405+00	.161+00	.856+00	.219+01	.186+00
-.2	.300	-.262	-.452	.100	.547+00	.345+00	.126+01	.207+01	.268+00
.0	.245	-.189	-.189	.245	.647+00	.647+00	.176+01	.187+01	.352+00
.2	.176	.178	.022	.376	.150+01	.105+01	.238+01	.164+01	.417+00
.4	.104	-.203	.197	.504	.127+01	.157+01	.319+01	.142+01	.458+00
.6	.033	-.243	.357	.673	.108+01	.572+00	.430+01	.122+01	.487+00
.8	-.039	-.290	.510	.761	.915+00	.512+00	.577+01	.105+01	.511+00
1.0	-.111	-.343	.657	.889	.774+00	.454+01	.774+01	.897+00	.531+00
1.2	-.185	-.393	.801	1.015	.653+00	.399+00	.632+01	.765+00	.549+00
1.4	-.261	-.457	.943	1.139	.548+00	.349+00	.876+01	.650+00	.567+00
1.6	-.339	-.517	1.083	1.261	.459+00	.304+00	.121+02	.550+00	.596+00
1.8	-.419	-.577	1.224	1.381	.381+00	.265+00	.167+02	.464+00	.608+00
2.0	-.503	-.635	1.354	1.497	.314+00	.211+00	.231+02	.390+00	.635+00
2.2	-.593	-.694	1.506	1.607	.255+00	.202+00	.321+02	.326+00	.670+00
2.4	-.691	-.751	1.649	1.709	.204+00	.178+00	.446+02	.270+00	.717+00
2.6	-.802	-.806	1.794	1.798	.158+00	.156+00	.622+02	.222+00	.780+00
2.8	-.937	-.865	1.935	1.863	.116+00	.136+00	.860+02	.179+00	.867+00
3.0	-1.110	-.936	2.064	1.890	.775-01	.116+00	.775+02	.139+00	.981+00
3.4	-1.633	-1.165	2.235	1.767	.233-01	.684-01	.172+03	.723-01	.124+01
3.8	-2.351	-1.511	2.249	1.449	.445-02	.308-01	.585+02	.311-01	.143+01
4.2	-3.136	-1.901	2.299	1.064	.731-03	.126-01	.281+02	.126-01	.151+01
4.6	-3.934	-2.299	2.301	.666	.116-03	.502-02	.199+03	.502-02	.155+01
5.0	-4.733	-2.699	2.301	.267	.185-04	.200-02	.464+01	.200-02	.156+01

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 JFR PHI
 .145-02 .221+01 .453+00 .159+04 2.314 .432 .548+06 1.1578 .216 2.855

N=200 H*=.262

REDUCED DYNAMIC VISCOSITY		AND		MODULUS		MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	G1R	G2R	ETA2/1
OMI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA2/1
-2.8	.364	-2.736	-5.536	-2.436	.231+01	.183-02	.291-05	.367-02	.231+01
-2.0	.364	-1.936	-3.936	-1.636	.231+01	.116-01	.116-03	.231-01	.231+01
-1.8	.364	-1.736	-3.536	-1.436	.231+01	.183-01	.291-03	.367-01	.231+01
-1.4	.364	-1.337	-2.737	-1.036	.231+01	.460-01	.183-02	.921-01	.231+01
-1.0	.362	-.940	-1.940	-.638	.230+01	.115+00	.115-01	.230+00	.231+01
-.8	.360	-.746	-1.546	-.440	.229+01	.180+00	.285-01	.363+00	.230+01
-.6	.353	-.560	-1.160	-.247	.225+01	.276+00	.693-01	.566+00	.227+01
-.4	.337	-.392	-.792	-.063	.217+01	.406+00	.162+00	.864+00	.221+01
-.2	.304	-.261	-.461	.104	.201+01	.548+00	.346+00	.127+01	.209+01
.0	.250	-.189	-.189	.250	.178+01	.648+00	.648+00	.178+01	.189+01
.2	.182	-.177	.023	.382	.152+01	.666+00	.105+01	.241+01	.166+01
.4	.111	-.202	.198	.511	.129+01	.629+00	.158+01	.324+01	.144+01
.6	.040	-.241	.359	.640	.110+01	.574+00	.229+01	.437+01	.124+01
.8	-.030	-.288	.512	.770	.932+00	.515+00	.325+01	.588+01	.107+01
1.0	-.102	-.340	.660	.898	.790+00	.457+00	.457+01	.790+01	.913+00
1.2	-.175	-.395	.805	1.025	.658+00	.403+00	.638+01	.106+02	.780+00
1.4	-.250	-.452	.948	1.150	.563+00	.353+00	.887+01	.141+02	.664+00
1.6	-.326	-.510	1.030	1.274	.472+00	.309+00	.123+02	.188+02	.564+00
1.8	-.406	-.569	1.231	1.394	.393+00	.270+00	.170+02	.248+02	.477+00
2.0	-.489	-.626	1.374	1.511	.324+00	.237+00	.237+02	.324+02	.401+00
2.2	-.578	-.682	1.518	1.622	.264+00	.208+00	.330+02	.419+02	.336+00
2.4	-.676	-.737	1.663	1.724	.211+00	.183+00	.461+02	.529+02	.279+00
2.6	-.789	-.790	1.810	1.811	.162+00	.162+00	.645+02	.646+02	.229+00
2.8	-.928	-.848	1.952	1.872	.118+00	.142+00	.895+02	.745+02	.184+00
3.0	-1.108	-.921	2.079	1.892	.779-01	.120+00	.120+03	.779+02	.143+00
3.4	-1.650	-1.158	2.242	1.750	.224-01	.695-01	.175+03	.563+02	.731-01
3.8	-2.377	-1.510	2.290	1.423	.419-02	.309-01	.195+03	.265+02	.312-01
4.2	-3.164	-1.901	2.299	1.036	.685-03	.126-01	.199+03	.109+02	.126-01
4.6	-3.962	-2.299	2.301	.638	.109-03	.502-02	.200+03	.435+01	.502-02
5.0	-4.762	-2.699	2.301	.238	.173-04	.200-02	.200+03	.173+01	.200-02

1

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM (1/LP)2 /LP)2 PHI
 .163-02 .195+01 .514+00 .146+04 2.377 .421 .439+06 1.1609 .205 3.002

N=200 H*= .30

REDUCED DYNAMIC VISCOSITY		AND		MODULUS		MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETAIR	ETAZR	GIR	GZR	ETAIR	ETAZR	GIR	GZR	ETAIR
-2.8	.376	-2.735	-5.535	-2.424	.238+01	.194-02	.292-05	.377-02	.238+01
-2.0	.376	-1.935	-3.935	-1.624	.238+01	.116-01	.116-03	.238-01	.238+01
-1.8	.376	-1.735	-3.535	-1.424	.238+01	.184-01	.292-03	.377-01	.238+01
-1.4	.376	-1.336	-2.736	-1.024	.238+01	.462-01	.184-02	.946-01	.238+01
-1.0	.374	-.939	-1.939	-.626	.237+01	.115+00	.115-01	.237+00	.237+01
-.8	.371	-.745	-1.545	-.429	.235+01	.190+00	.285-01	.373+00	.236+01
-.6	.365	-.558	-1.158	-.235	.232+01	.277+00	.695-01	.582+00	.233+01
-.4	.349	-.390	-.790	-.051	.223+01	.407+00	.162+00	.890+00	.227+01
-.2	.318	-.260	-.460	.118	.208+01	.550+00	.347+00	.131+01	.215+01
.0	.265	-.187	-.187	.265	.184+01	.651+00	.651+00	.184+01	.195+01
.2	.199	-.174	.026	.399	.158+01	.670+00	.106+01	.250+01	.172+01
.4	.130	-.198	.202	.530	.135+01	.634+00	.159+01	.339+01	.149+01
.6	.063	-.236	.364	.663	.116+01	.591+00	.231+01	.460+01	.129+01
.8	-.005	-.281	.519	.795	.989+00	.524+00	.330+01	.624+01	.112+01
1.0	-.074	-.331	.669	.926	.844+00	.467+00	.467+01	.844+01	.965+00
1.2	-.143	-.383	.817	1.057	.719+00	.414+00	.656+01	.114+02	.829+00
1.4	-.215	-.437	.963	1.185	.610+00	.365+00	.918+01	.153+02	.711+00
1.6	-.288	-.491	1.109	1.312	.515+00	.323+00	.128+02	.205+02	.608+00
1.8	-.364	-.545	1.255	1.436	.432+00	.285+00	.180+02	.273+02	.518+00
2.0	-.445	-.596	1.404	1.555	.359+00	.254+00	.254+02	.359+02	.439+00
2.2	-.533	-.645	1.555	1.667	.293+00	.227+00	.359+02	.465+02	.371+00
2.4	-.632	-.691	1.709	1.768	.233+00	.204+00	.511+02	.586+02	.310+00
2.6	-.751	-.739	1.861	1.849	.177+00	.193+00	.727+02	.706+02	.254+00
2.8	-.904	-.795	2.005	1.896	.125+00	.160+00	.101+03	.786+02	.203+00
3.0	-1.110	-.874	2.126	1.890	.777-01	.134+00	.134+03	.777+02	.155+00
3.4	-1.708	-1.140	2.260	1.692	.196-01	.725-01	.182+03	.492+02	.751-01
3.8	-2.459	-1.506	2.294	1.341	.348-02	.312-01	.197+03	.219+02	.314-01
4.2	-3.251	-1.900	2.300	.949	.562-03	.126-01	.199+03	.890+01	.126-01
4.6	-4.049	-2.299	2.301	.551	.893-04	.502-02	.200+03	.355+01	.502-02
5.0	-4.849	-2.699	2.301	.151	.142-04	.200-02	.200+03	.142+01	.200-02

EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM SUM(L1 JFR PHI
 N=300 H=.05
 .240-03 .366+01 .273+00 .786+04 1.888 .530 .194+08 1.1178 .314 1.465

REDUCED DYNAMIC VISCOSITY AND MODULUS										
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	
OMTI	ETA2R	ETA2R	GIR	G2R	ETA1R	ETA2R	GIR	G2R	MOD	
ETA2R	ETA2R	ETA2R	GIR	G2R	ETA1R	ETA2R	GIR	G2R	ETA2R	
-2.8	.276	-2.752	-5.552	-2.524	.189+01	.177-02	.281-05	.299-02	.189+01	.938-03
-2.0	.276	-1.952	-3.952	-1.724	.189+01	.112-01	.112-03	.189-01	.189+01	.592-02
-1.8	.276	-1.752	-3.552	-1.524	.189+01	.177-01	.281-03	.299-01	.189+01	.938-02
-1.4	.276	-1.352	-2.752	-1.124	.189+01	.444-01	.177-02	.751-01	.189+01	.236-01
-1.0	.274	-.956	-1.956	-.726	.188+01	.111+00	.111-01	.188+00	.189+01	.589-01
-.8	.270	-.761	-1.561	-.530	.186+01	.173+00	.275-01	.295+00	.187+01	.927-01
-.6	.262	-.576	-1.176	-.338	.183+01	.266+00	.668-01	.459+00	.185+01	.144+00
-.4	.242	-.409	-.809	-.158	.175+01	.390+00	.155+00	.696+00	.179+01	.220+00
-.2	.202	-.281	-.451	.002	.159+01	.524+00	.331+00	.101+01	.168+01	.318+00
.0	.134	-.214	-.214	.134	.136+01	.611+00	.611+00	.136+01	.149+01	.422+00
.2	.047	-.212	-.012	.247	.111+01	.614+00	.973+00	.177+01	.127+01	.503+00
.4	-.043	-.250	.150	.357	.905+00	.562+00	.141+01	.227+01	.107+01	.556+00
.6	-.132	-.304	.296	.668	.737+00	.496+00	.197+01	.293+01	.889+00	.592+00
.8	-.222	-.367	.433	.578	.599+00	.429+00	.271+01	.378+01	.737+00	.622+00
1.0	-.313	-.437	.553	.687	.486+00	.366+00	.366+01	.486+01	.609+00	.645+00
1.2	-.405	-.511	.689	.795	.393+00	.308+00	.489+01	.624+01	.500+00	.665+00
1.4	-.498	-.589	.811	.902	.318+00	.258+00	.647+01	.799+01	.409+00	.681+00
1.6	-.592	-.670	.930	1.008	.256+00	.214+00	.850+01	.102+02	.333+00	.695+00
1.8	-.686	-.754	1.046	1.114	.206+00	.176+00	.111+02	.130+02	.271+00	.708+00
2.0	-.782	-.840	1.150	1.218	.165+00	.145+00	.145+02	.165+02	.220+00	.719+00
2.2	-.878	-.927	1.273	1.322	.132+00	.118+00	.188+02	.210+02	.178+00	.730+00
2.4	-.976	-1.015	1.325	1.424	.106+00	.967-01	.243+02	.266+02	.143+00	.741+00
2.6	-1.074	-1.103	1.497	1.526	.842-01	.789-01	.314+02	.335+02	.115+00	.753+00
2.8	-1.175	-1.192	1.608	1.625	.658-01	.643-01	.406+02	.421+02	.927-01	.767+00
3.0	-1.279	-1.260	1.720	1.721	.526-01	.525-01	.525+02	.526+02	.744-01	.784+00
3.4	-1.502	-1.451	1.949	1.898	.315-01	.354-01	.890+02	.791+02	.474-01	.844+00
3.8	-1.780	-1.619	2.191	2.020	.166-01	.241-01	.152+03	.105+03	.292-01	.968+00
4.2	-2.215	-1.829	2.371	1.985	.610-02	.148-01	.235+03	.967+02	.160-01	.118+01
4.6	-2.871	-2.145	2.455	1.729	.134-02	.716-02	.285+03	.535+02	.728-02	.139+01
5.0	-3.640	-2.527	2.473	1.360	.229-03	.297-02	.297+03	.229+02	.298-02	.149+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM LI/LP RECIP SUM SUM(LI JER PHI
 -306-03 .349+01 .287+00 .644+04 1.967 .508 (1/LP)2 /LP)2 .291 1.798
 N=300 H*=.075

REDUCED DYNAMIC VISCOSITY AND MODULUS										MON		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2/I	ETA2R	ETA2/I
OMTI	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	ETA2R	ETA2/I	ETA2R	ETA2/I
-2.8	.294	-2.748	-5.548	-2.506	.197+01	.179-02	.283-05	.312-02	.197+01	.197+01	.908-03	.197+01	.573-02
-2.0	.294	-1.948	-3.948	-1.706	.197+01	.113-01	.113-03	.197-01	.197+01	.197+01	.573-02	.197+01	.573-02
-1.8	.294	-1.748	-3.548	-1.506	.197+01	.179-01	.283-03	.312-01	.197+01	.197+01	.908-02	.197+01	.908-02
-1.4	.293	-1.349	-2.749	-1.107	.197+01	.448-01	.178-02	.782-01	.197+01	.197+01	.228-01	.197+01	.228-01
-1.0	.292	-.952	-1.952	-.708	.196+01	.112+00	.112-01	.196+00	.196+01	.196+01	.570-01	.196+01	.570-01
-.8	.288	-.758	-1.558	-.512	.194+01	.175+00	.277-01	.308+00	.195+01	.195+01	.898-01	.195+01	.898-01
-.6	.280	-.572	-1.172	-.320	.191+01	.268+00	.674-01	.479+00	.192+01	.192+01	.140+00	.192+01	.140+00
-.4	.261	-.405	-.805	-.139	.183+01	.394+00	.157+00	.727+00	.187+01	.187+01	.213+00	.187+01	.213+00
-.2	.223	-.276	-.476	.023	.167+01	.530+00	.334+00	.105+01	.175+01	.175+01	.307+00	.175+01	.307+00
.0	.158	-.208	-.208	.158	.144+01	.620+00	.620+00	.144+01	.157+01	.157+01	.407+00	.157+01	.407+00
.2	.075	-.203	-.003	.275	.119+01	.626+00	.992+00	.138+01	.134+01	.134+01	.485+00	.134+01	.485+00
.4	-.012	-.238	.162	.388	.974+00	.578+00	.145+01	.245+01	.113+01	.113+01	.535+00	.113+01	.535+00
.6	-.097	-.289	.311	.503	.800+00	.514+00	.205+01	.318+01	.951+00	.951+00	.571+00	.951+00	.571+00
.8	-.183	-.348	.452	.617	.655+00	.448+00	.283+01	.414+01	.794+00	.794+00	.600+00	.794+00	.600+00
1.0	-.271	-.414	.586	.729	.536+00	.345+00	.385+01	.536+01	.660+00	.660+00	.623+00	.660+00	.623+00
1.2	-.360	-.485	.715	.847	.437+00	.327+00	.519+01	.692+01	.546+00	.546+00	.643+00	.546+00	.643+00
1.4	-.450	-.560	.840	.950	.355+00	.276+00	.692+01	.892+01	.450+00	.450+00	.660+00	.450+00	.660+00
1.6	-.541	-.637	.953	1.059	.248+00	.231+00	.918+01	.115+02	.369+00	.369+00	.675+00	.369+00	.675+00
1.8	-.633	-.717	1.083	1.167	.233+00	.192+00	.121+02	.147+02	.302+00	.302+00	.689+00	.302+00	.689+00
2.0	-.726	-.799	1.201	1.274	.188+00	.159+00	.159+02	.188+02	.246+00	.246+00	.701+00	.246+00	.701+00
2.2	-.821	-.883	1.317	1.379	.151+00	.131+00	.208+02	.240+02	.200+00	.200+00	.714+00	.200+00	.714+00
2.4	-.917	-.967	1.433	1.493	.121+00	.108+00	.271+02	.304+02	.162+00	.162+00	.728+00	.162+00	.728+00
2.6	-1.015	-1.052	1.548	1.585	.966-01	.847-01	.353+02	.385+02	.131+00	.131+00	.743+00	.131+00	.743+00
2.8	-1.116	-1.137	1.663	1.684	.766-01	.730-01	.460+02	.483+02	.106+00	.106+00	.761+00	.106+00	.761+00
3.0	-1.220	-1.221	1.779	1.780	.602-01	.601-01	.601+02	.602+02	.851-01	.851-01	.785+00	.851-01	.785+00
3.4	-1.452	-1.384	2.016	1.948	.353-01	.413-01	.104+03	.846+02	.543-01	.543-01	.863+00	.543-01	.863+00
3.8	-1.765	-1.553	2.247	2.035	.172-01	.280-01	.177+03	.108+03	.328-01	.328-01	.102+01	.328-01	.102+01
4.2	-2.270	-1.792	2.408	1.930	.536-02	.162-01	.256+03	.850+02	.170-01	.170-01	.125+01	.170-01	.125+01
4.6	-2.977	-2.136	2.464	1.623	.105-02	.731-02	.291+03	.420+02	.739-02	.739-02	.143+01	.739-02	.143+01
5.0	-3.759	-2.525	2.475	1.241	.174-03	.299-02	.299+03	.174+02	.299-02	.299-02	.151+01	.299-02	.151+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM SUM(L1) JER PHI
 .372-03 .332+01 .302+00 .547+04 2.034 .492 .821+07 1.1349 .274 2.038

REDUCED DYNAMIC VISCOSITY AND MODULUS										N=300 H= .10			
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	SUM	SUM	SUM	PHI
OMTI	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR
-2.8	.308	-2.745	-5.545	-2.492	.203+01	.180-02	.285-05	.322-02	.203+01	.203+01	.203+01	.203+01	.884-03
-2.0	.308	-1.945	-3.945	-1.692	.203+01	.113-01	.113-03	.203-01	.203+01	.203+01	.203+01	.203+01	.558-02
-1.8	.308	-1.745	-3.545	-1.492	.203+01	.180-01	.285-03	.322-01	.203+01	.203+01	.203+01	.203+01	.884-02
-1.4	.308	-1.346	-2.746	-1.092	.203+01	.451-01	.180-02	.809-01	.203+01	.203+01	.203+01	.203+01	.222-01
-1.0	.306	-.943	-1.943	-.694	.202+01	.112+00	.112-01	.202+00	.203+01	.203+01	.203+01	.203+01	.555-01
-.8	.303	-.755	-1.555	-.497	.201+01	.176+00	.279-01	.318+00	.202+01	.202+01	.202+01	.202+01	.874-01
-.6	.295	-.569	-1.169	-.305	.197+01	.270+00	.678-01	.495+00	.199+01	.199+01	.199+01	.199+01	.136+00
-.4	.277	-.401	-.801	-.123	.189+01	.397+00	.158+00	.753+00	.193+01	.193+01	.193+01	.193+01	.207+00
-.2	.240	-.272	-.472	.040	.174+01	.534+00	.337+00	.110+01	.182+01	.182+01	.182+01	.182+01	.298+00
.0	.177	-.203	-.203	.177	.150+01	.627+00	.627+00	.150+01	.163+01	.163+01	.163+01	.163+01	.395+00
.2	.097	-.197	.003	.297	.125+01	.636+00	.101+01	.198+01	.140+01	.140+01	.140+01	.140+01	.470+00
.4	.014	-.229	.171	.414	.103+01	.590+00	.148+01	.259+01	.119+01	.119+01	.119+01	.119+01	.519+00
.6	-.069	-.277	.323	.531	.854+00	.528+00	.210+01	.340+01	.100+01	.100+01	.100+01	.100+01	.554+00
.8	-.152	-.334	.456	.648	.705+00	.464+00	.292+01	.445+01	.844+00	.844+00	.844+00	.844+00	.582+00
1.0	-.237	-.397	.603	.763	.580+00	.401+00	.401+01	.580+01	.705+00	.705+00	.705+00	.705+00	.605+00
1.2	-.322	-.465	.735	.878	.476+00	.343+00	.544+01	.754+01	.587+00	.587+00	.587+00	.587+00	.624+00
1.4	-.410	-.536	.864	.990	.389+00	.291+00	.731+01	.978+01	.486+00	.486+00	.486+00	.486+00	.642+00
1.6	-.498	-.611	.989	1.102	.318+00	.245+00	.975+01	.126+02	.401+00	.401+00	.401+00	.401+00	.657+00
1.8	-.588	-.688	1.112	1.212	.258+00	.205+00	.129+02	.163+02	.330+00	.330+00	.330+00	.330+00	.671+00
2.0	-.679	-.766	1.234	1.321	.209+00	.171+00	.171+02	.209+02	.270+00	.270+00	.270+00	.270+00	.686+00
2.2	-.772	-.847	1.353	1.428	.169+00	.142+00	.226+02	.268+02	.221+00	.221+00	.221+00	.221+00	.700+00
2.4	-.867	-.928	1.472	1.533	.136+00	.118+00	.297+02	.341+02	.180+00	.180+00	.180+00	.180+00	.716+00
2.6	-.964	-1.009	1.591	1.636	.109+00	.979-01	.390+02	.432+02	.146+00	.146+00	.146+00	.146+00	.734+00
2.8	-1.065	-1.090	1.710	1.735	.861-01	.813-01	.513+02	.543+02	.118+00	.118+00	.118+00	.118+00	.757+00
3.0	-1.171	-1.170	1.830	1.829	.674-01	.676-01	.676+02	.674+02	.954-01	.954-01	.954-01	.954-01	.787+00
3.4	-1.415	-1.327	2.073	1.985	.385-01	.471-01	.118+03	.967+02	.608-01	.608-01	.608-01	.608-01	.886+00
3.8	-1.766	-1.502	2.298	2.034	.172-01	.315-01	.199+03	.108+03	.359-01	.359-01	.359-01	.359-01	.107+01
4.2	-2.334	-1.763	2.431	1.866	.464-02	.170-01	.270+03	.735+02	.176-01	.176-01	.176-01	.176-01	.130+01
4.6	-3.072	-2.131	2.469	1.528	.848-03	.739-02	.294+03	.338+02	.744-02	.744-02	.744-02	.744-02	.146+01
5.0	-3.861	-2.524	2.476	1.139	.138-03	.299-02	.299+03	.138+02	.299-02	.299-02	.299-02	.299-02	.152+01

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SUM      SUM(L1  JER      PHI
(1/LP)2  /LP)2      -23
-.561+07 1.1417    .258 2.258

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	1960	1961	1962	1963	1964	1965	1966	1967	1968	1969	1970	1971	1972	1973	1974	1975	1976	1977	1978	1979	1980	1981	1982	1983	1984	1985	1986	1987	1988	1989	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054	2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066	2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078	2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090	2091	2092	2093	2094	2095	2096	2097	2098	2099	2100	2101	2102	2103	2104	2105	2106	2107	2108	2109	2110	2111	2112	2113	2114	2115	2116	2117	2118	2119	2120	2121	2122	2123	2124	2125	2126	2127	2128	2129	2130	2131	2132	2133	2134	2135	2136	2137	2138	2139	2140	2141	2142	2143	2144	2145	2146	2147	2148	2149	2150	2151	2152	2153	2154	2155	2156	2157	2158	2159	2160	2161	2162	2163	2164	2165	2166	2167	2168	2169	2170	2171	2172	2173	2174	2175	2176	2177	2178	2179	2180	2181	2182	2183	2184	2185	2186	2187	2188	2189	2190	2191	2192	2193	2194	2195	2196	2197	2198	2199	2200	2201	2202	2203	2204	2205	2206	2207	2208	2209	2210	2211	2212	2213	2214	2215	2216	2217	2218	2219	2220	2221	2222	2223	2224	2225	2226	2227	2228	2229	2230	2231	2232	2233	2234	2235	2236	2237	2238	2239	2240	2241	2242	2243	2244	2245	2246	2247	2248	2249	2250	2251	2252	2253	2254	2255	2256	2257	2258	2259	2260	2261	2262	2263	2264	2265	2266	2267	2268	2269	2270	2271	2272	2273	2274	2275	2276	2277	2278	2279	2280	2281	2282	2283	2284	2285	2286	2287	2288	2289	2290	2291	2292	2293	2294	2295	2296	2297	2298	2299	2300	2301	2302	2303	2304	2305	2306	2307	2308	2309	2310	2311	2312	2313	2314	2315	2316	2317	2318	2319	2320	2321	2322	2323	2324	2325	2326	2327	2328	2329	2330	2331	2332	2333	2334	2335	2336	2337	2338	2339	2340	2341	2342	2343	2344	2345	2346	2347	2348	2349	2350	2351	2352	2353	2354	2355	2356	2357	2358	2359	2360	2361	2362	2363	2364	2365	2366	2367	2368	2369	2370	2371	2372	2373	2374	2375	2376	2377	2378	2379	2380	2381	2382	2383	2384	2385	2386	2387	2388	2389	2390	2391	2392	2393	2394	2395	2396	2397	2398	2399	2400	2401	2402	2403	2404	2405	2406	2407	2408	2409	2410	2411	2412	2
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EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RECIP SUM SUM(LI) JER PHI
 .504-03 .297+01 .336+00 .425+04 2.143 .467 .451+07 1.1454 .249 2.377

REDUCED DYNAMIC VISCOSITY AND MODULUS										N=300 H*=.15			
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	SUM	SUM(LI)	JER	PHI
OMI	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	G1R	G2R	ETA1R	ETA2R	ETA2R/1		
-2.8	.331	-2.741	-5.541	-2.469	.214+01	.192-02	.288-05	.340-02	.214+01	.847-03			
-2.0	.331	-1.941	-3.941	-1.669	.214+01	.115-01	.115-03	.214-01	.214+01	.535-02			
-1.8	.331	-1.741	-3.541	-1.469	.214+01	.181-01	.288-03	.340-01	.214+01	.847-02			
-1.4	.331	-1.342	-2.742	-1.069	.214+01	.455-01	.181-02	.852-01	.214+01	.213-01			
-1.0	.329	-.945	-1.945	-.671	.213+01	.114+00	.114-01	.213+00	.214+01	.532-01			
-.8	.326	-.751	-1.551	-.474	.212+01	.178+00	.281-01	.336+00	.212+01	.837-01			
-.6	.318	-.564	-1.164	-.282	.208+01	.273+00	.135-01	.523+00	.210+01	.130+00			
-.4	.301	-.397	-.797	-.099	.200+01	.401+00	.160+00	.796+00	.204+01	.198+00			
-.2	.266	-.267	-.467	.066	.184+01	.541+00	.341+00	.116+01	.192+01	.285+00			
.0	.207	-.196	-.196	.207	.161+01	.636+00	.636+00	.161+01	.173+01	.376+00			
.2	.131	-.188	.012	.331	.135+01	.649+00	.103+01	.215+01	.150+01	.447+00			
.4	.053	-.217	.183	.453	.113+01	.607+00	.153+01	.284+01	.128+01	.493+00			
.6	-.024	-.261	.339	.576	.945+00	.548+00	.218+01	.376+01	.109+01	.526+00			
.8	-.103	-.314	.486	.697	.789+00	.486+00	.306+01	.498+01	.927+00	.552+00			
1.0	-.183	-.372	.628	.817	.657+00	.424+00	.424+01	.657+01	.782+00	.573+00			
1.2	-.263	-.456	.754	.937	.545+00	.367+00	.581+01	.864+01	.657+00	.592+00			
1.4	-.346	-.502	.898	1.054	.451+00	.315+00	.790+01	.113+02	.550+00	.609+00			
1.6	-.429	-.571	1.029	1.171	.372+00	.268+00	.107+02	.148+02	.459+00	.625+00			
1.8	-.515	-.643	1.157	1.285	.306+00	.228+00	.144+02	.193+02	.381+00	.641+00			
2.0	-.602	-.715	1.285	1.398	.250+00	.193+00	.193+02	.250+02	.316+00	.657+00			
2.2	-.692	-.789	1.411	1.508	.203+00	.163+00	.258+02	.322+02	.260+00	.674+00			
2.4	-.784	-.863	1.537	1.616	.164+00	.137+00	.344+02	.413+02	.214+00	.695+00			
2.6	-.880	-.937	1.663	1.720	.132+00	.116+00	.460+02	.524+02	.175+00	.720+00			
2.8	-.982	-1.011	1.789	1.818	.104+00	.976-01	.616+02	.658+02	.143+00	.752+00			
3.0	-1.092	-1.063	1.917	1.908	.809-01	.826-01	.826+02	.809+02	.116+00	.796+00			
3.4	-1.366	-1.230	2.170	2.034	.431-01	.589-01	.148+03	.108+03	.729-01	.939+00			
3.8	-1.803	-1.430	2.370	1.997	.158-01	.372-01	.234+03	.994+02	.404-01	.117+01			
4.2	-2.463	-1.745	2.455	1.737	.344-02	.180-01	.285+03	.545+02	.183-01	.138+01			
4.6	-3.234	-2.127	2.473	1.366	.584-03	.747-02	.297+03	.232+02	.749-02	.149+01			
5.0	-4.029	-2.523	2.477	.971	.936-04	.300-02	.300+03	.936+01	.300-02	.154+01			

EXACT ZIMM EIGENVALUES		N=300 H*= .20				PHI	
LI	LN	SUM	SUM	SUM(LI	JFR	PHI	
	1/(LN)	1/(LP)	11/LP	(1/LP)2		-23	
.633-03	.263+01	.352+04	2.229	.287+07	1.1516	.232	2.622

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EXACT ZIMM EIGENVALUES
 L1 LN 1/(LN) SUM 1/(LP) SUM L1/LP ROCAL RECIP SUM SUM(L1 JFR PHI
 N=300 H= .25
 .764-03 .229+01 .437+00 .302+04 2.308 .433 .19R+07 1.1564 .217 2.814

REDUCED DYNAMIC VISCOSITY AND MODULUS										MOD		ARCTAN	
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	ETA2R	ETA2R	ETA2R	ETA2R
OMTI	FTAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	GIR	G2R	ETAIR	ETA2R	ETA2R	ETA2R	ETA2R
-2.8	.363	-2.737	-5.537	-2.437	.231+01	.183-02	.290-05	.366-02	.231+01	.231+01	.231+01	.794-03	.794-03
-2.0	.363	-1.937	-3.937	-1.637	.231+01	.116-01	.116-03	.231-01	.231+01	.231+01	.231+01	.501-02	.501-02
-1.8	.363	-1.737	-3.537	-1.437	.231+01	.183-01	.290-03	.366-01	.231+01	.231+01	.231+01	.794-02	.794-02
-1.4	.363	-1.337	-2.737	-1.037	.231+01	.460-01	.183-02	.918-01	.231+01	.231+01	.231+01	.199-01	.199-01
-1.0	.361	-.941	-1.941	-.639	.230+01	.115+00	.115-01	.230+00	.230+01	.230+01	.230+01	.499-01	.499-01
-.8	.358	-.746	-1.546	-.442	.228+01	.179+00	.284-01	.362+00	.229+01	.229+01	.229+01	.784-01	.784-01
-.6	.351	-.560	-1.160	-.249	.225+01	.275+00	.692-01	.564+00	.226+01	.226+01	.226+01	.122+00	.122+00
-.4	.335	-.392	-.792	-.065	.217+01	.405+00	.161+00	.862+00	.220+01	.220+01	.220+01	.185+00	.185+00
-.2	.303	-.262	-.462	.103	.201+01	.547+00	.345+00	.127+01	.208+01	.208+01	.208+01	.266+00	.266+00
.0	.249	-.190	-.190	.249	.177+01	.646+00	.646+00	.177+01	.189+01	.189+01	.189+01	.350+00	.350+00
.2	.180	-.178	-.022	.380	.151+01	.664+00	.105+01	.240+01	.165+01	.165+01	.165+01	.413+00	.413+00
.4	.109	-.203	.197	.509	.129+01	.626+00	.157+01	.323+01	.143+01	.143+01	.143+01	.453+00	.453+00
.6	.039	-.243	.357	.639	.109+01	.571+00	.227+01	.435+01	.123+01	.123+01	.123+01	.481+00	.481+00
.8	-.032	-.291	.509	.768	.929+00	.512+00	.323+01	.586+01	.106+01	.106+01	.106+01	.503+00	.503+00
1.0	-.103	-.344	.656	.897	.788+00	.453+00	.453+01	.768+01	.909+00	.909+00	.909+00	.522+00	.522+00
1.2	-.176	-.400	.800	1.024	.667+00	.398+00	.631+01	.106+02	.777+00	.777+00	.777+00	.538+00	.538+00
1.4	-.249	-.459	.941	1.151	.563+00	.347+00	.873+01	.142+02	.662+00	.662+00	.662+00	.553+00	.553+00
1.6	-.324	-.519	1.081	1.276	.474+00	.302+00	.120+02	.189+02	.562+00	.562+00	.562+00	.568+00	.568+00
1.8	-.401	-.580	1.220	1.399	.397+00	.263+00	.166+02	.250+02	.476+00	.476+00	.476+00	.585+00	.585+00
2.0	-.481	-.641	1.359	1.519	.331+00	.228+00	.228+02	.331+02	.402+00	.402+00	.402+00	.604+00	.604+00
2.2	-.563	-.702	1.498	1.637	.273+00	.199+00	.315+02	.433+02	.338+00	.338+00	.338+00	.629+00	.629+00
2.4	-.651	-.761	1.639	1.749	.223+00	.173+00	.435+02	.561+02	.283+00	.283+00	.283+00	.660+00	.660+00
2.6	-.746	-.819	1.781	1.854	.180+00	.152+00	.604+02	.715+02	.235+00	.235+00	.235+00	.702+00	.702+00
2.8	-.852	-.875	1.925	1.948	.141+00	.133+00	.841+02	.887+02	.194+00	.194+00	.194+00	.759+00	.759+00
3.0	-.978	-.933	2.067	2.022	.105+00	.117+00	.117+03	.105+03	.157+00	.157+00	.157+00	.838+00	.838+00
3.2	-1.348	-1.086	2.314	2.052	.449-01	.821-01	.206+03	.113+03	.935-01	.935-01	.935-01	.107+01	.107+01
3.4	-1.952	-1.361	2.439	1.848	.112-01	.436-01	.275+03	.705+02	.450-01	.450-01	.450-01	.132+01	.132+01
4.0	-2.704	-1.729	2.471	1.496	.198-02	.186-01	.295+03	.313+02	.187-01	.187-01	.187-01	.147+01	.147+01
4.6	-3.496	-2.124	2.476	1.104	.319-03	.752-02	.299+03	.127+02	.752-02	.752-02	.752-02	.153+01	.153+01
5.0	-4.295	-2.523	2.477	.705	.507-04	.300-02	.300+03	.507+01	.300-02	.300-02	.300-02	.155+01	.155+01

EXACT ZIMM EIGENVALUES
 LI LN 1/(LN) SUM 1/(LP) SUM L1/LP RICAL RECIP SUM (1/LP)2 /LP)2 SUM(L1 JER PHI
 .795-03 .221+01 .453+00 .293+04 2.326 .430 .183+07 1.1573 .214 2.8556

N=300 M=.262

REDUCED DYNAMIC VISCOSITY AND MODULUS									
LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG	LOG
OMTI	ETAIR	ETA2R	GIR	ETAIR	ETA2R	GIR	G2R	ETAR	ARCTAN
-2.8	.367	-2.737	-5.537	.233+01	.183-02	.291-05	.369-02	.233+01	.789-03
-2.0	.367	-1.937	-3.937	.233+01	.116-01	.116-03	.233-01	.233+01	.498-02
-1.8	.367	-1.737	-3.537	.233+01	.183-01	.291-03	.369-01	.233+01	.788-02
-1.4	.366	-1.337	-2.737	.232+01	.460-01	.183-02	.925-01	.232+01	.198-01
-1.0	.365	-.940	-1.940	.232+01	.115+00	.115-01	.232+00	.232+01	.495-01
-.8	.362	-.746	-1.546	.230+01	.179+00	.284-01	.365+00	.231+01	.779-01
-.6	.355	-.560	-1.160	.226+01	.276+00	.692-01	.569+00	.228+01	.121+00
-.4	.339	-.392	-.792	.218+01	.406+00	.161+00	.869+00	.222+01	.184+00
-.2	.307	-.261	-.461	.203+01	.548+00	.346+00	.128+01	.210+01	.264+00
.0	.253	-.189	-.189	.179+01	.647+00	.647+00	.179+01	.190+01	.347+00
.2	.185	-.177	.023	.153+01	.665+00	.105+01	.243+01	.167+01	.410+00
.4	.115	-.202	.198	.130+01	.628+00	.158+01	.327+01	.145+01	.449+00
.6	.045	-.242	.358	.111+01	.573+00	.228+01	.442+01	.125+01	.477+00
.8	-.024	-.289	.511	.945+00	.514+00	.324+01	.596+01	.108+01	.498+00
1.0	-.095	-.341	.659	.804+00	.456+00	.456+01	.804+01	.924+00	.516+00
1.2	-.166	-.397	.803	.682+00	.401+00	.635+01	.108+02	.791+00	.531+00
1.4	-.239	-.455	.945	.577+00	.351+00	.881+01	.145+02	.675+00	.546+00
1.6	-.313	-.514	1.086	.487+00	.306+00	.122+02	.194+02	.575+00	.561+00
1.8	-.389	-.574	1.226	.408+00	.267+00	.168+02	.258+02	.488+00	.578+00
2.0	-.467	-.634	1.366	.341+00	.232+00	.232+02	.341+02	.413+00	.598+00
2.2	-.549	-.693	1.507	.282+00	.203+00	.322+02	.448+02	.348+00	.623+00
2.4	-.636	-.750	1.650	.231+00	.178+00	.447+02	.580+02	.292+00	.656+00
2.6	-.731	-.805	1.795	.186+00	.157+00	.624+02	.739+02	.243+00	.701+00
2.8	-.839	-.859	1.941	.145+00	.138+00	.872+02	.915+02	.200+00	.762+00
3.0	-.968	-.915	2.095	.108+00	.122+00	.122+03	.108+03	.162+00	.846+00
3.4	-1.352	-1.072	2.328	.444-01	.847-01	.213+03	.112+03	.956-01	.109+01
3.8	-1.973	-1.356	2.444	.106-01	.440-01	.278+03	.671+02	.453-01	.133+01
4.2	-2.732	-1.729	2.471	.185-02	.187-01	.296+03	.294+02	.188-01	.147+01
4.6	-3.525	-2.124	2.476	.1075	.752-02	.299+03	.119+02	.753-02	.153+01
5.0	-4.323	-2.523	2.477	.677	.300-02	.300+03	.475+01	.300-02	.155+01

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